



Recursion

snarf today's code



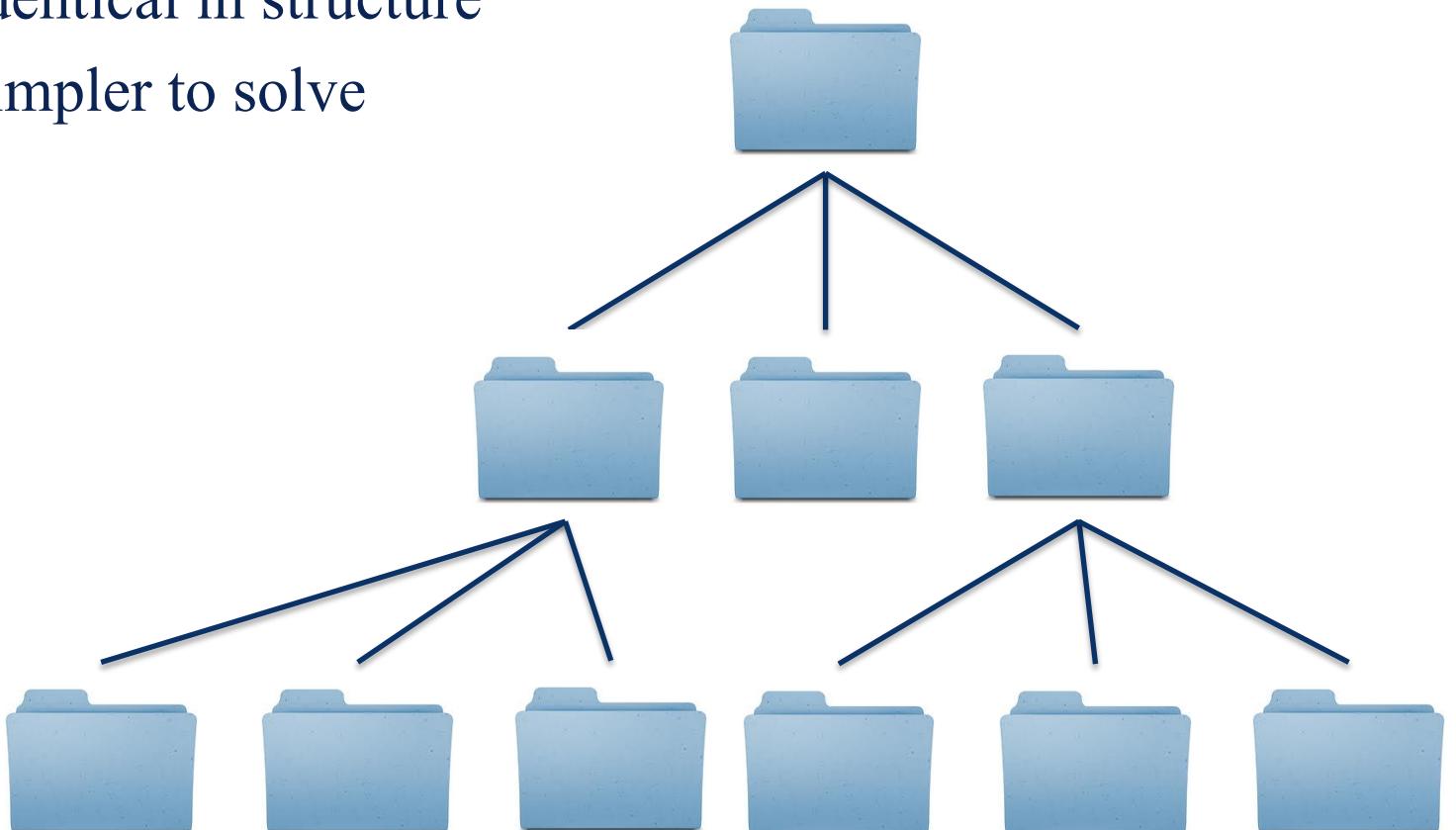
Announcements

- Apt 4 – Due Oct 17
- Quiz Friday– Linked Lists
 - Can increase exam grade
- DNA – Due Oct 23



Last time

- Directory search
 - Reduce it to a sub problem
 1. identical in structure
 2. simpler to solve





General Structure

- `void solve(ProblemClass instance) {`
 - `if(instance is simple) { // base case`
 - *solve instance directly}*
 - *divide into subinstance(s)*
 - *solve(subinstance)*
 - *reassemble problem*



Today

- Recursion and the call stack
- More examples:
 - Sorting
 - Flood fill

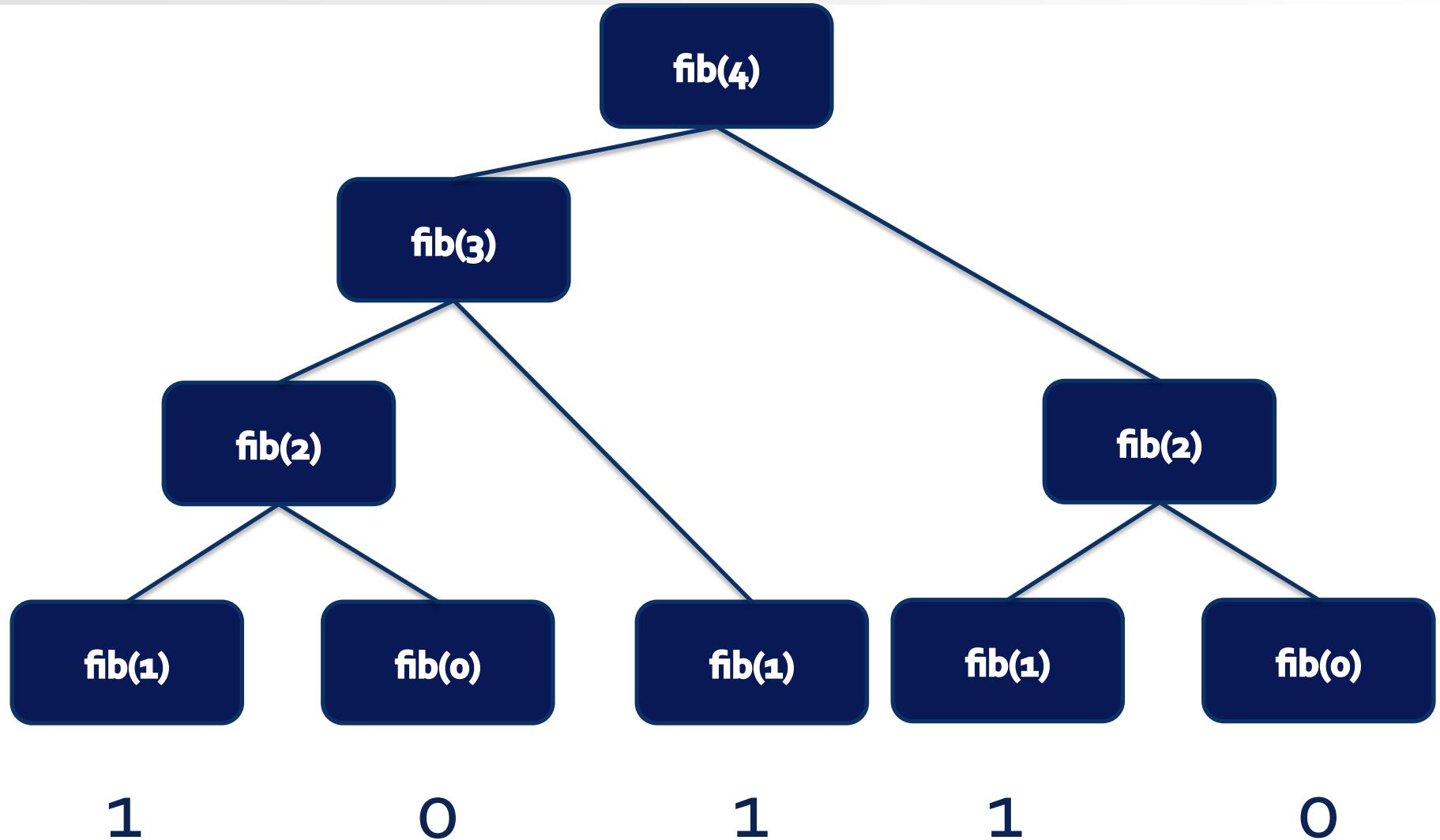


Fibonacci

- $\text{fib}(0) = 0$
- $\text{fib}(1) = 1$
- $\text{fib}(2) = 1$
- $\text{fib}(3) = 2$
- $\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$



Fibonacci





Fibonacci

- When a function is called it is pushed to the call stack

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

```
fib(3);
```



Fibonacci

- When a function is called it is pushed to the call stack

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

fib(3);

fib(3)



Fibonacci

- Run code on top of stack

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

fib(3)



Fibonacci

- Run code on top of stack

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

fib(2)
fib(3)



Fibonacci

- Run code on top of stack

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

```
fib(1)  
fib(2)  
fib(3)
```



Fibonacci

- Pop when function completes

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

fib(1) = 1

fib(2)

fib(3)



Fibonacci

- Continue from where you left off

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

fib(0)

fib(1) = 1

fib(2)

fib(3)



Fibonacci

- Continue from where you left off

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

$\text{fib}(0) = 0$

$\text{fib}(1) = 1$

$\text{fib}(2)$

$\text{fib}(3)$



Fibonacci

- Continue from where you left off

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

$$\text{fib}(0) = 0$$

$$\text{fib}(1) = 1$$

$$\text{fib}(2) = 1 + 0$$

$$\text{fib}(3)$$



Fibonacci

- Continue from where you left off

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

fib(1)

fib(0) = 0

fib(1) = 1

fib(2) = 1 + 0

fib(3)



Fibonacci

- Continue from where you left off

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

$$\text{fib}(1) = 1$$

$$\text{fib}(0) = 0$$

$$\text{fib}(1) = 1$$

$$\text{fib}(2) = 1 + 0$$

$$\text{fib}(3)$$



Fibonacci

- Continue from where you left off

```
int fib(int n){  
    if(n==0) return 0;  
    if(n==1) return 1;  
    return fib(n-1) * fib(n-2);  
}
```

$$\text{fib}(1) = 1$$

$$\text{fib}(0) = 0$$

$$\text{fib}(1) = 1$$

$$\text{fib}(2) = 1 + 0$$

$$\text{fib}(3) = 1 + 1$$



Today

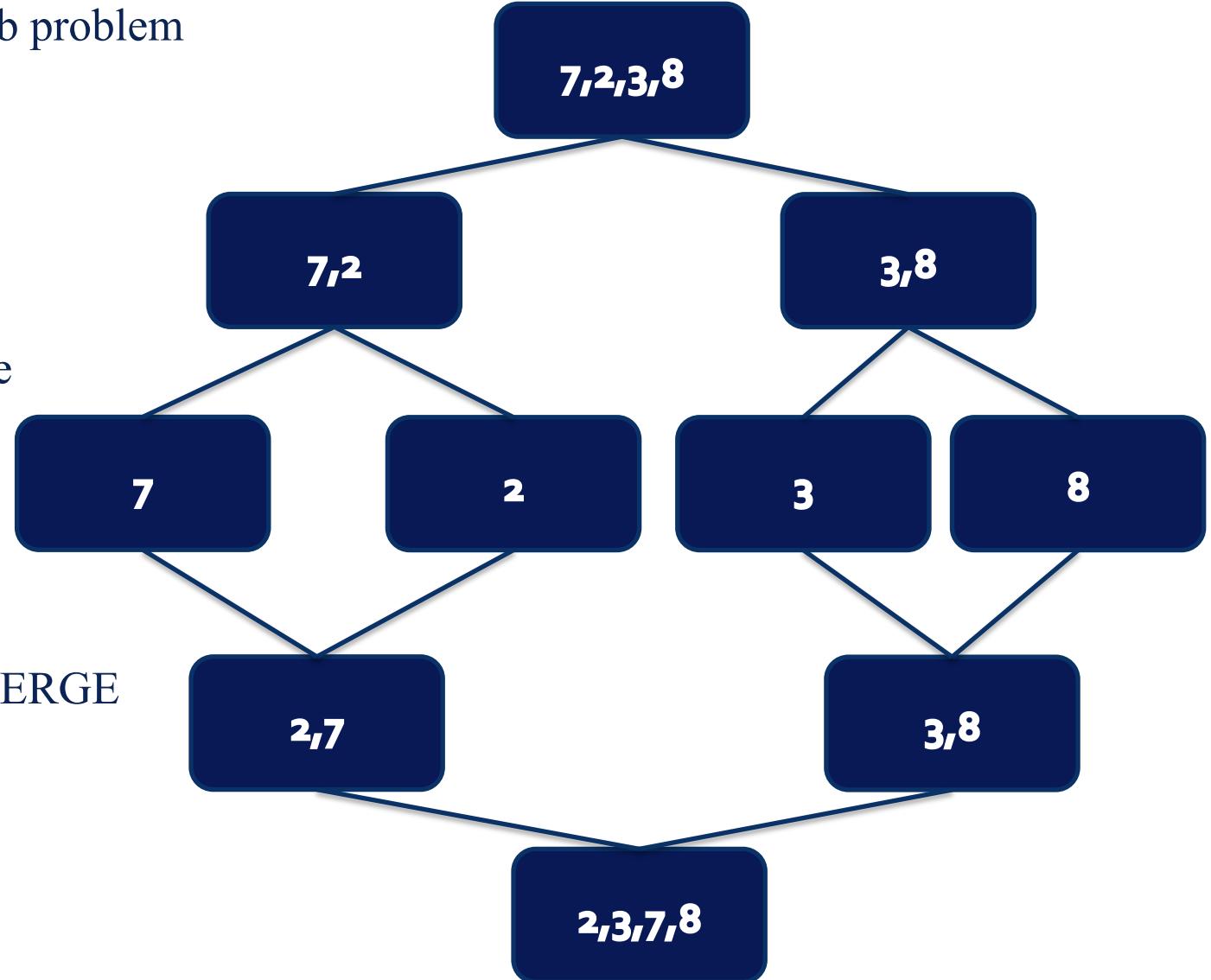
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MergeSort

- Reduce to a sub problem
 - half the list

- Simple to solve
 - 1 element
- Once sorted MERGE lists together

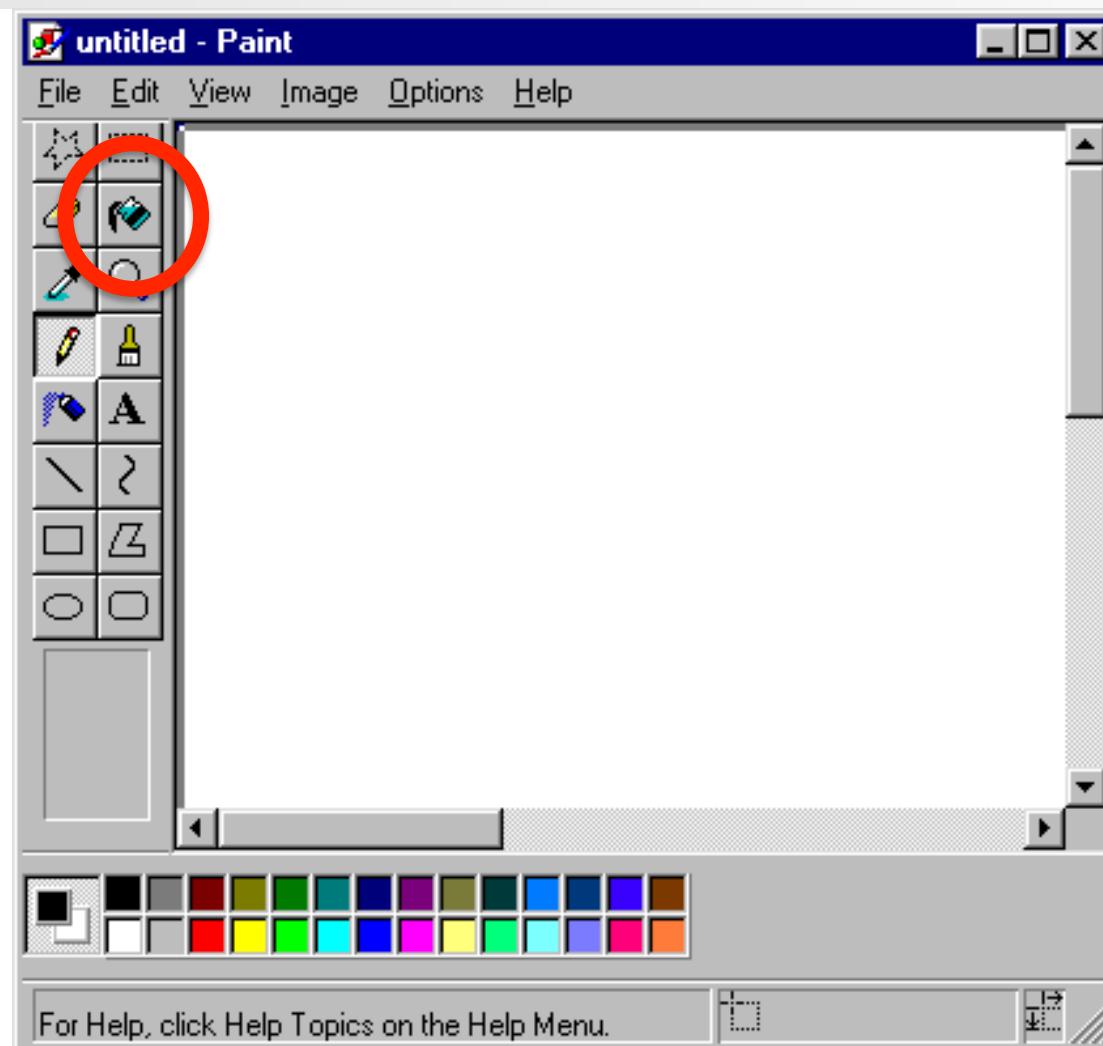




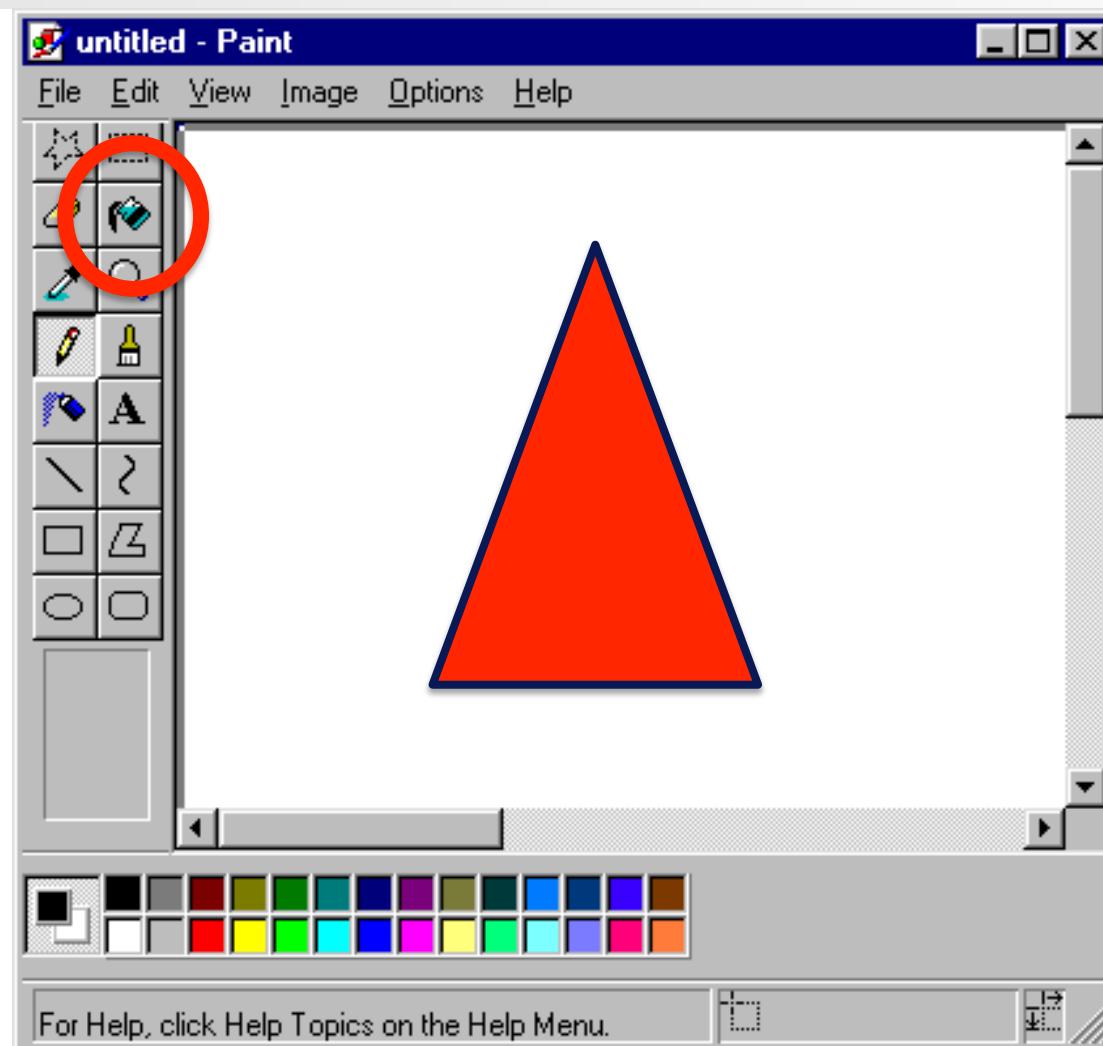
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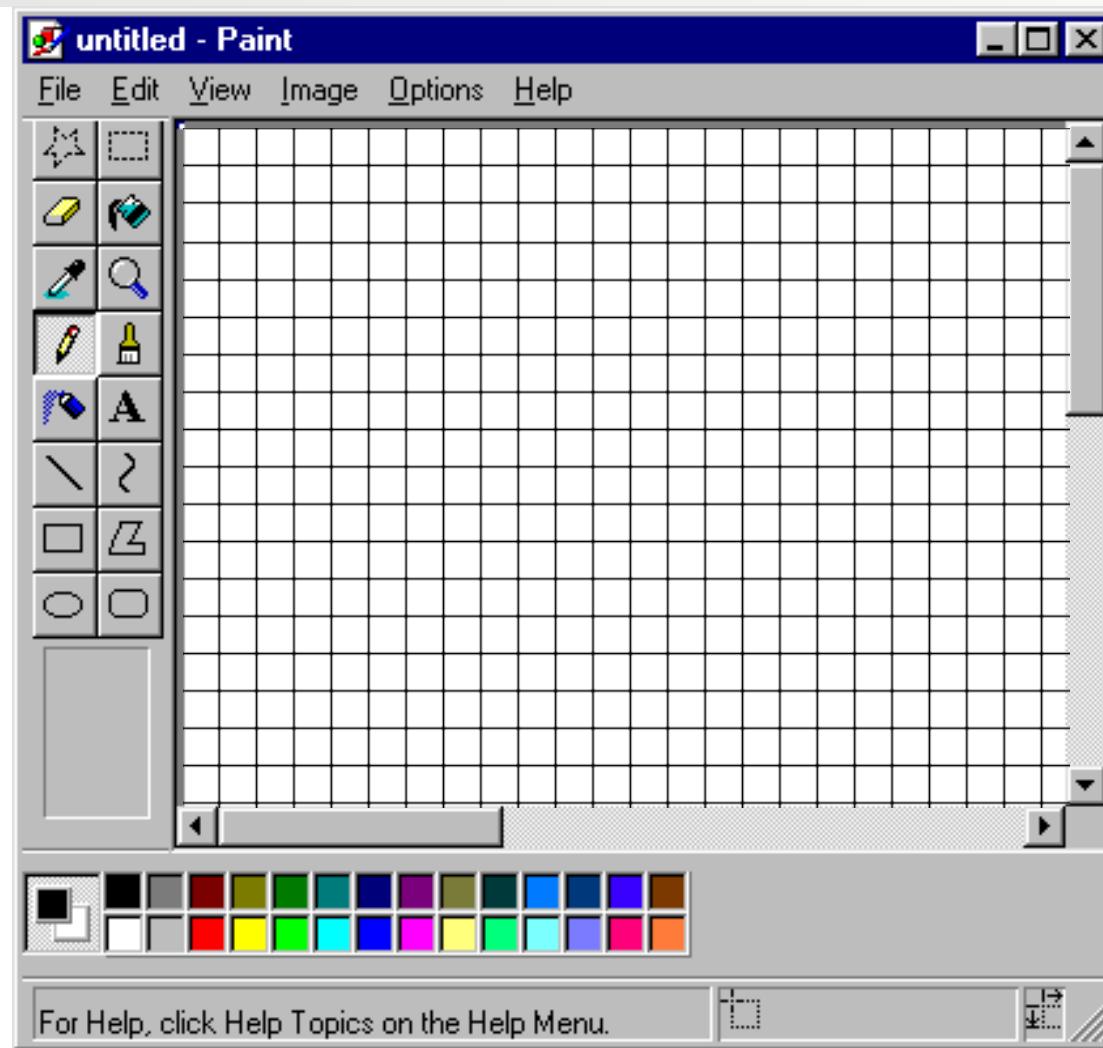
Flood Fill



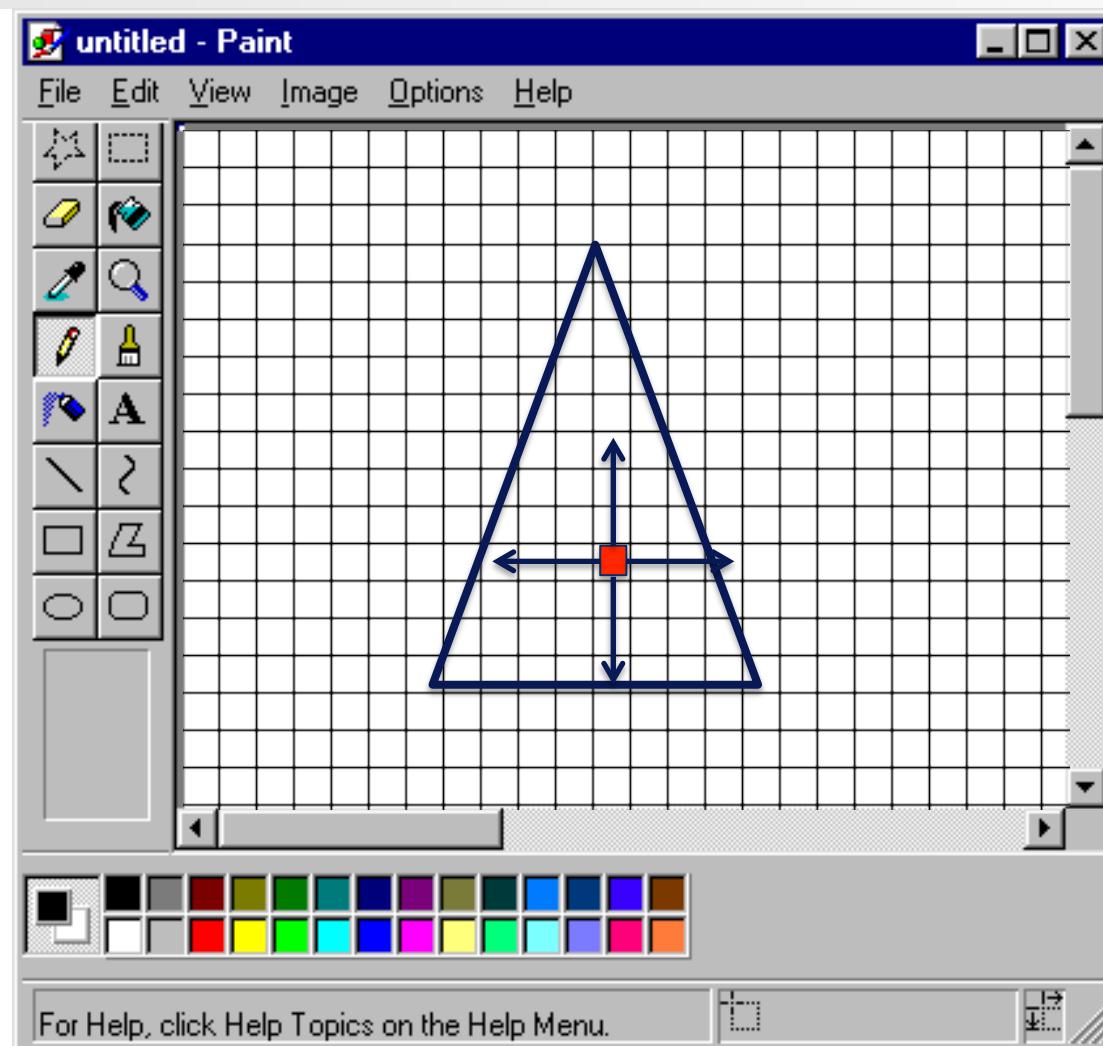
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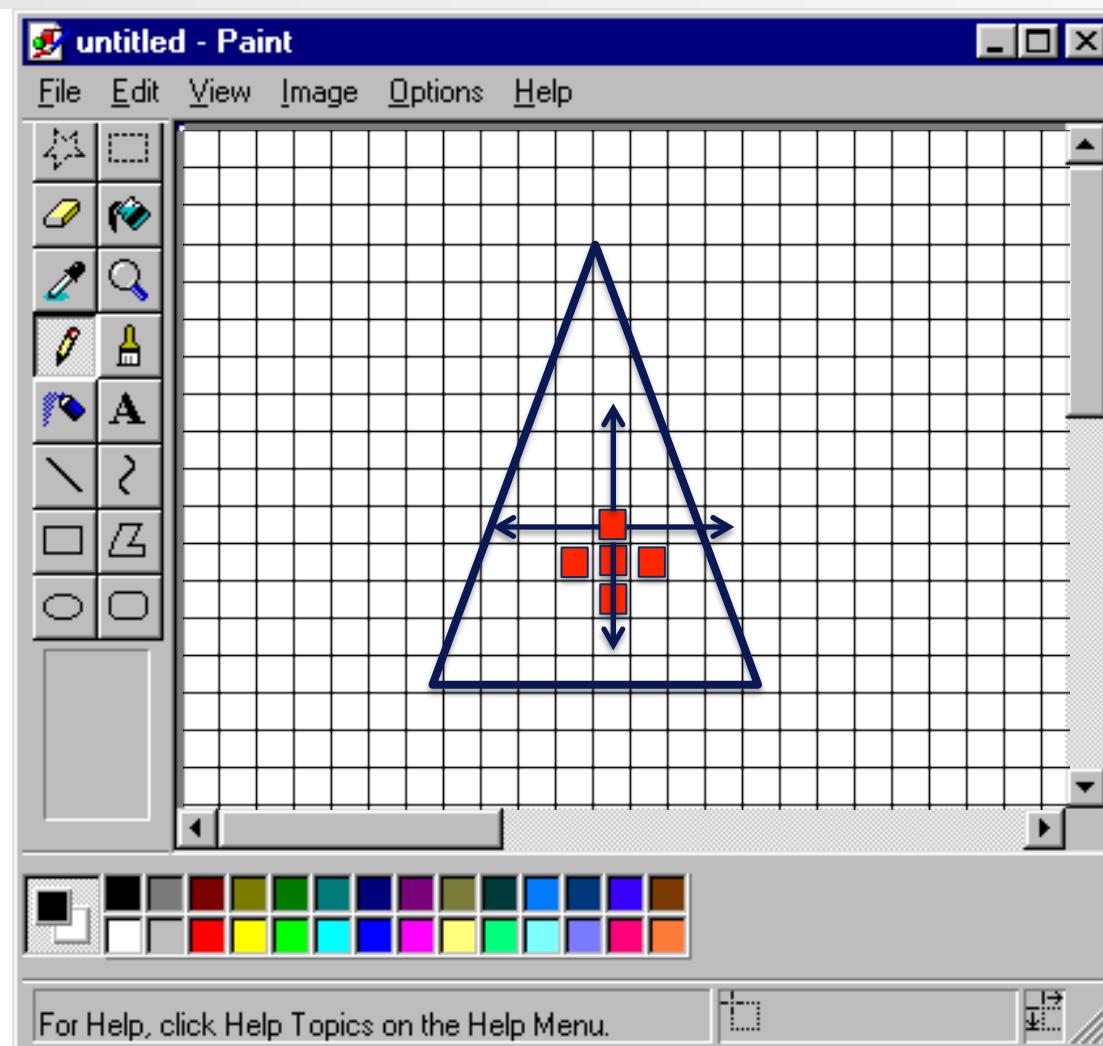
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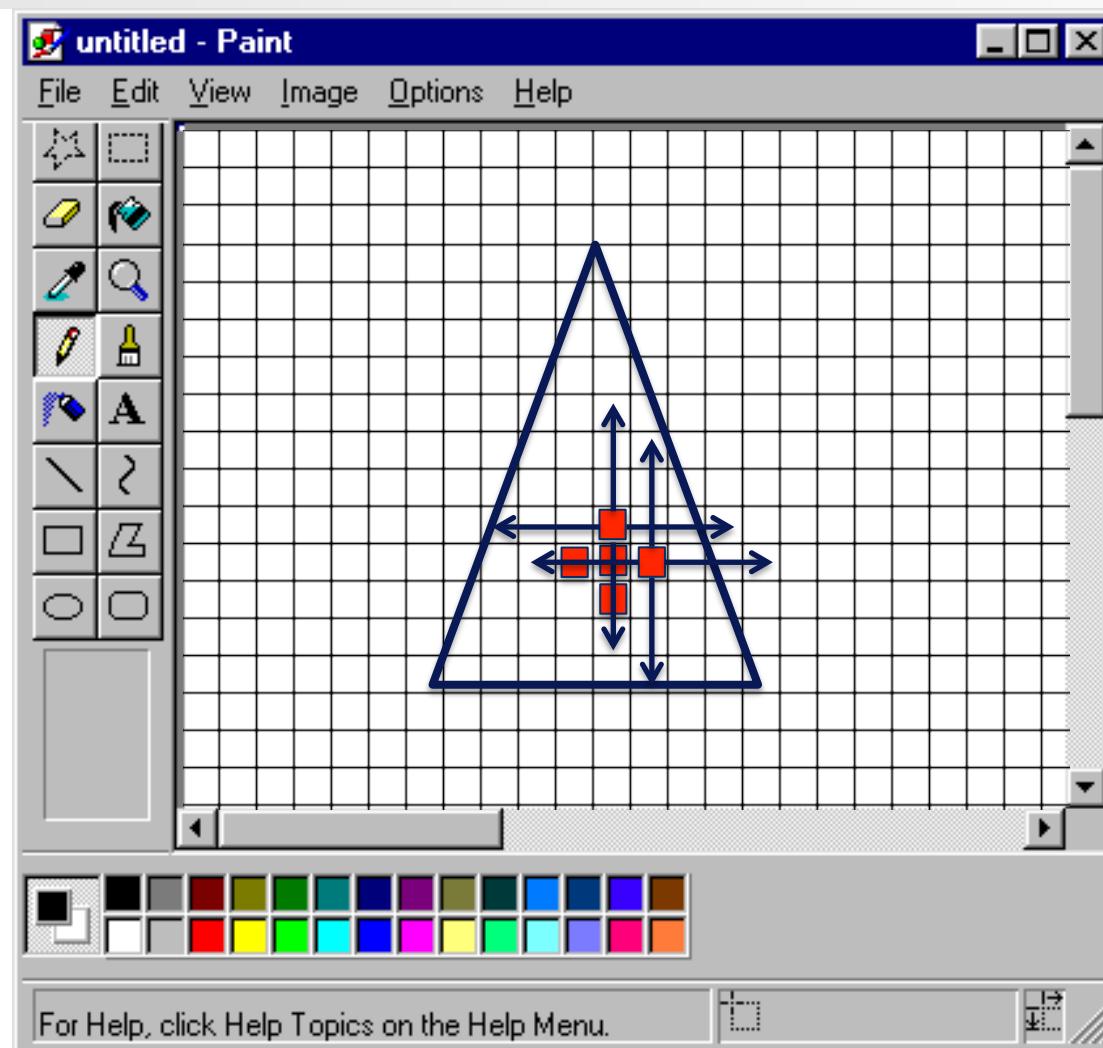
Flood Fill



Flood Fill



Flood Fill





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