

Searching

&

Sorting

The Plan

- ❖ **Searching**
- ❖ **Sorting**
- ❖ **Java Context**

Search (Retrieval)

- ❖ **“Looking it up”**
- ❖ **One of most fundamental operations**
- ❖ **Without computer**
 - ❑ **Indexes**
 - ❑ **Tables of content**
 - ❑ **Card Catalogue**
 - ❑ **Reference books**
- ❖ **Fundamental part of many computer algorithms**

Linear (Sequential) Search

- ❖ Plod through material, one item at a time
- ❖ Always works
- ❖ Can be slow
- ❖ Sometimes the *only* way
- ❖ Phone Book Example
 - ❑ 660-6567
 - ❑ Whose number is it?
- ❖ (How could this be done faster?)

Binary Search

Often can do better than linear search:

- ❖ **Phone Book again (Predates Computer!)**

- ☐ Find midpoint
- ☐ Decide before or after (or direct hit)
- ☐ Discard half of uncertainty
- ☐ Repeat until there

- ❖ **Fast! (Don't even need computer!)**

- ❖ ***What does it require* (why not use all the time)?**

- ❖ **How man extra steps if double sized book?**

Hashing

A way of storing info so we can *go directly* there to retrieve

- ❖ Mail boxes in a mail room (know exactly where number 33 is.)
- ❖ Hashing is a way of transforming some part of info to allow such straight-forward storage
- ❖ What to use for students in classroom
 - ❑ Age? Last name? SSN?

Hashing

- ❖ **Use extra space to allow for faster operation**
- ❖ **Collision Handling**
 - ❑ **What to do if two different items map to the same bin?**
 - ❑ **Many different solutions...**

Search Performance

- ❖ **Linear Search** (*brute force, plodding*)
 - ❑ Proportional to amount $\sim N$
- ❖ **Binary Search** (*telephone book*)
 - ❑ Proportional to log of amount $\sim \log(N)$
- ❖ **Hashing** (*go directly to ...*)
 - ❑ Independent of amount! $\sim \text{constant}$

Sorting (Motivation)

Fundamental part of many algorithms and procedures

- ❖ **Required before other operations possible**
 - ❑ E.g., binary search
- ❖ **Often a user requirement for manual use**
 - ❑ E.g., phone book, dictionary, directory, index...
- ❖ **Get lower Postal Rates if sorted by Zip Code**
- ❖ **Implicit requirement for “orderly” operation**

Selection Sort

- ❑ N items in an array named Data
[2 | 4 | 7 | 3 | 1 | 8 | 5]
- ❑ Find smallest of elements 0 thru N-1 of Data
- ❑ Interchange this with 1st element of array Data
[_ | _ | _ | _ | _ | _ | _]
- ❑ Find smallest of elements 1 thru N-1 of Data
- ❑ Interchange this with 2nd element of array Data
[_ | _ | _ | _ | _ | _ | _]
- ❑ ...
- ❑ Find smallest of elements k-1 thru N-1 of Data
- ❑ Interchange this with kth element of array Data
[_ | _ | _ | _ | _ | _ | _]
[_ | _ | _ | _ | _ | _ | _]
[_ | _ | _ | _ | _ | _ | _]
- ❑ Done when k-1 = N-1
[_ | _ | _ | _ | _ | _ | _]

Selection Sort

- ❑ N items in an array named Data
[2 | 4 | 7 | 3 | 1 | 8 | 5]
- ❑ Find smallest of elements 0 thru N-1 of Data
- ❑ Interchange this with 1st element of array Data
[1 | 4 | 7 | 3 | 2 | 8 | 5]
- ❑ Find smallest of elements 1 thru N-1 of Data
- ❑ Interchange this with 2nd element of array Data
[1 | 2 | 7 | 3 | 4 | 8 | 5]
- ❑ ...
- ❑ Find smallest of elements k-1 thru N-1 of Data
- ❑ Interchange this with kth element of array Data
[1 | 2 | 3 | 7 | 4 | 8 | 5]
[1 | 2 | 3 | 4 | 7 | 8 | 5]
[1 | 2 | 3 | 4 | 5 | 8 | 7]
- ❑ Done when $k-1 = N-1$
[1 | 2 | 3 | 4 | 5 | 7 | 8]

Selection Sort Performance (N^2)

- ❖ Assume there are N items to be sorted
- ❖ Notice that with each pass we have to make N comparisons
 - (actually $N/2$ on average)
- ❖ Notice that we have to make N passes
 - (actually $N-1$)
- ❖ Therefore requires $N \times N$ comparisons
 - (actually $N*(N-1)/2$)
- ❖ Performance proportional to N^2 or $\sim N^2$

Other Simple Sorts (N^2)

❖ 2 More simple sorts like Selection Sort

- ❑ Insertion Sort

- ❑ Bubble Sort

❖ All 3 have common properties

- ❑ *Easy* to write

- ❑ Fairly *slow* for large amounts of data

Industrial Quality Sorts

- ❖ Can do much better than simple sorts
- ❖ *Selection Sort* is often used
 - ❑ Divide and conquer strategy
 - ❑ Partitions data into two parts
 - ❑ Partitions each of these parts into subparts
 - ❑ Etc.
- ❖ Performance greatly improved over previous
 - ❑ Can handle any *real* job

Other Fast Sorts

❖ Merge Sort

- ❑ Stable
- ❑ Requires extra memory

❖ Binary Tree Sort

❖ Heap Sort

❖ Shell Sort

❖ Bucket Sort

- ❑ Can be extremely fast under special circumstances
- ❑ (Analogy to Hashing)

Sort Performance

- ❖ **Slowest: $\sim N^2$**
 - ❑ Selection Sort
 - ❑ Insertion Sort , Bubble Sort
- ❖ **Very Fast: $\sim N \log N$**
 - ❑ QuickSort, Binary Tree Sort
 - ❑ Merge Sort, Heap Sort
- ❖ **Quite Fast**
 - ❑ Shell Sort
- ❖ **Fastest (*limited* situations): $\sim N$**
 - ❑ Bucket Sort

Java Context (writing your own?)

Don't need to write your own -- Java includes:

❖ **For *Collections***

```
static void sort(List list)
```

- ❑ **stable**

```
static int binarySearch(List list, Object key)
```

❖ **For *Arrays* (?? = int, double, ..., and Object)**

```
static void sort(?? [ ] a)
```

- ❑ **Uses quicksort (not stable)**

```
static int binarySearch( ?? [ ] a, ?? key)
```

Practice

1. In a class you design, create an array of ints, initialise with some numeric data and print it out.
2. Utilize the sort method found in the **Arrays** class. Sort your array and print it out again.
3. Write your own version of **selection sort** and add it to your class. Compare to the sort of the **Arrays** class.