Relational Model & Algebra

CPS 116 Introduction to Database Systems

Announcements (Thurs. September 1)

- Please sign up for mailing list and database (IBM DB2) accounts on the sign-up sheet (now circulating)
- ❖ Homework #1 will be assigned next Tuesday
- ❖ Office hours: see also course Web page
 - Jun: TTH afternoon
 - Ming: MW late afternoon
- Book update
 - \$101 (new) / \$75.75 (used) from Duke bookstore
 - Available possibly tomorrow and definitely by next Tuesday
 - \$86.15 (new, free shipping) from Amazon

Relational data model

- * A database is a collection of relations (or tables)
- ❖ Each relation has a list of attributes (or columns)
 - Set-valued attributes not allowed
- Each attribute has a domain (or type)
- * Each relation contains a set of tuples (or rows)
 - Duplicate tuples are not allowed
- Fimplicity is a virtue!

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Example Student Course SID name CID title CPS116 Intro. to Database Systems 123 Milhouse 10 CPS130 Analysis of Algorithms 857 Lisa 456 Ralph CPS114 Computer Networks Enroll SID CID Ordering of rows doesn't matter 142 CPS116 (even though the output is always in some order) 123 CPS116 CPS114

Schema versus instance

- ❖ Schema (metadata)
 - Specification of how data is to be structured logically
 - Defined at set-up
 - Rarely changes
- **❖** Instance
 - Content
 - Changes rapidly, but always conforms to the schema
- Compare to type and objects of type in a programming language

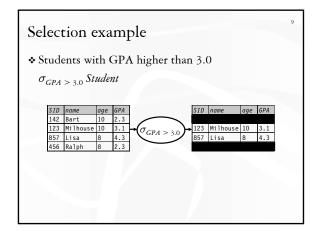
Example

- ❖ Schema
 - Student (SID integer, name string, age integer, GPA float)
 - Course (CID string, title string)
 - Enroll (SID integer, CID integer)
- ❖ Instance
 - { (142, Bart, 10, 2.3), (123, Milhouse, 10, 3.1), ...}
 - { ⟨CPS116, Intro. to Database Systems⟩, ...}
 - { $\langle 142, CPS116 \rangle$, $\langle 142, CPS114 \rangle$, ...}

Relational algebra A language for querying relational databases based on operators: **Core set of operators: **Selection, projection, cross product, union, difference, and renaming **Additional, derived operators: **Join, natural join, intersection, etc.

* Compose operators to make complex queries

Selection * Input: a table R * Notation: σ_p R • p is called a selection condition/predicate * Purpose: filter rows according to some criteria * Output: same columns as R, but only rows of R that satisfy p



More on selection

- ❖ Selection predicate in general can include any column of R, constants, comparisons (=, ≤, etc.), and Boolean connectives (\land : and, \lor : or, and \neg : not)
 - Example: straight A students under 18 or over 21 $\sigma_{GPA \, \geq \, 4.0 \, \land \, (age \, < \, 18 \, \lor \, age \, > \, 21)} Student$
- But you must be able to evaluate the predicate over a single row of the input table
 - Example: student with the highest GPA

σ_{GPA ≥ all GPA} : Student table Student

Projection

❖ Input: a table R

❖ Notation: $\pi_L R$

• L is a list of columns in R

* Purpose: select columns to output

 \diamond Output: same rows, but only the columns in L

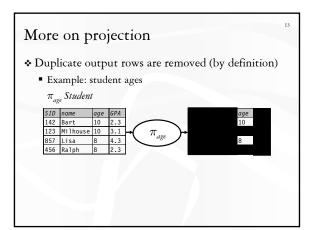
Projection example

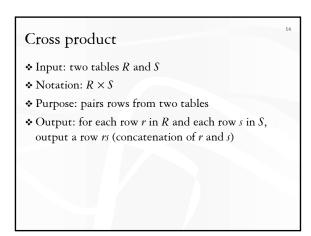
* ID's and names of all students

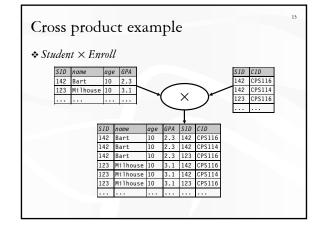
 $\pi_{SID,\;name}$ Student

SID	name	age	GPA		SID	name	
142	Bart	10	2.3		142	Bart	
123	Milhouse	10	3.1	$\rightarrow (\pi_{SID, name}) \rightarrow$	123	Milhouse	
857	Lisa	8	4.3	S1D, name	857	Lisa	
456	Ralph	8	2.3		456	Ralph	

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A note on column ordering

* The ordering of columns in a table is considered unimportant (as is the ordering of rows)

SID	name	age	GPA	SID	CID
142	Bart	10	2.3	142	CPS116
142	Bart	10	2.3	142	CPS114
142	Bart	10	2.3	123	CPS116
123	Milhouse	10	3.1	142	CPS116
123	Milhouse	10	3.1	142	CPS114
123	Milhouse	10	3.1	123	CPS116

	SID	CID	SID	name	age	GPA
	142	CPS116	142	Bart	10	2.3
	142	CPS114	142	Bart	10	2.3
_	123	CPS116	142	Bart	10	2.3
	142	CPS116	123	Milhouse	10	3.1
	142	CPS114	123	Milhouse	10	3.1
	123	CPS116	123	Milhouse	10	3.1

❖ That means cross product is commutative, i.e., $R \times S = S \times R$ for any R and S

Derived operator: join

 \diamond Input: two tables R and S

* Notation: $R_{p} S$

p is called a join condition/predicate

- * Purpose: relate rows from two tables according to some criteria
- * Output: for each row r in R and each row s in S, output a row rs if r and s satisfy p
- ❖ Shorthand for

Join example

❖ Info about students, plus CID's of their courses

Student Student.SID = Enroll.SID Enroll

	SID	name	age	GPA			
	142	Bart	10	2.3			
	123	Milhouse	10	3.1			
					Student SID =		
Use table_name. column_name syntax							

to disambiguate identically named columns from different input tables

12	iaeni.	310 -	Enrou.31	D					
	age	e GPA						SID	CID
	10	2.3	/	_	_			142	CPS116
us	e 10	3.1				\ ~	_	142	CPS114
			٦		ent SIE			123	CPS116
	Enroll SID								
u	$nn_{-}n$	ame sy	ntax		1				
	SID	name	age	GPA	SID	CID			
	142	Bart	10	2.3	142	CPS116			
	142	Bart	10	2.3	142	CPS114			

123	Milhouse	10	3.1	123	CPS116

Derived operator: natural join

 \star Input: two tables R and S

❖ Notation: R S

* Purpose: relate rows from two tables, and

■ Enforce equality on all common attributes

■ Eliminate one copy of common attributes

***** Shorthand for π_L ($R = {}_p S$), where

• p equates all attributes common to R and S

L is the union of all attributes from R and S, with duplicate attributes removed

Union

 \diamond Input: two tables R and S

❖ Notation: $R \cup S$

 \blacksquare R and S must have identical schema

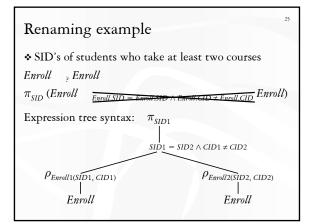
Output:

 \blacksquare Has the same schema as R and S

 Contains all rows in R and all rows in S, with duplicate rows eliminated

• Two rows are identical if they agree on all attributes

Difference	
\diamond Input: two tables R and S	
❖ Notation: $R - S$	
 R and S must have identical schema 	
❖ Output:	
• Has the same schema as R and S	
 Contains all rows in <i>R</i> that are not found in <i>S</i> 	
	_
Derived operator: intersection	23
\diamond Input: two tables R and S	
❖ Notation: $R \cap S$	
 R and S must have identical schema 	
❖ Output:	
 Has the same schema as R and S Contains all rows that are in both R and S 	
• Shorthand for	
❖ Also equivalent to	
• And to	
* And to	
Renaming	24
❖ Input: a table <i>R</i>	
• Notation: $\rho_S R$, or $\rho_{S(A_1, A_2,)} R$	
❖ Purpose: rename a table and/or its columns	
\diamond Output: a renamed table with the same rows as R	
❖ Used to	
Avoid confusion caused by identical column names	
 Create identical columns names for natural joins 	



Summary of core operators
❖ Selection: $\sigma_p R$
❖ Projection: $\pi_L R$
\star Cross product: $R \times S$
❖ Union: $R \cup S$
❖ Difference: $R - S$
* Renaming: $\rho_{S(A_1, A_2,)} R$
 Does not really add to processing power

Summary of derived operators	27
❖ Join: R _b S	
❖ Natural join: R S	
❖ Intersection: $R \cap S$	
❖ Many more	
■ Semijoin, anti-semijoin, quotient,	

An exercise	28
❖ Names of students in Lisa's classes	
Another exercise	29
❖ CID's of the courses that Lisa is NOT taking	
A trickier exercise	30
❖ Who has the highest GPA?	

Monotone operators What happens RelOp to the output? Add more rows to the input... * If some old output rows may need to be removed ■ Then the operator is non-monotone * Otherwise the operator is monotone ■ That is, old output rows always remain "correct" when more rows are added to the input • Formally, for a monotone operator *RelOp*: $R \subseteq R'$ implies $RelOp(R) \subseteq RelOp(R')$ Classification of relational operators ❖ Selection: $\sigma_p R$ • Projection: $\pi_L R$ ❖ Cross product: $R \times S$ ❖ Join: R _p S Natural join: R ❖ Union: $R \cup S$ ❖ Difference: R - S❖ Intersection: $R \cap S$ Why is "-" needed for highest GPA? * Composition of monotone operators produces a monotone query • Old output rows remain "correct" when more rows are added to the input ❖ Highest-GPA query is

Why do we need core operator X? Difference ❖ Cross product ❖ Union Selection? Projection? ■ Homework problem ③ Why is r.a. a good query language? ❖ Simple ■ A small set of core operators who semantics are easy to * Declarative? Yes, compared with older languages like CODASYL ■ Though operators do look somewhat "procedural" ❖ Complete? ■ With respect to what? Relational calculus **♦** $\{s.SID \mid s \in Student \land$ $\neg (\exists s' \in Student: s.GPA < s'.GPA) \}$, or $\{ s.SID \mid s \in Student \land \}$ $(\forall s' \in Student: s.GPA \ge s'.GPA)$ ❖ Relational algebra = "safe" relational calculus • Every query expressible as a safe relational calculus query is also expressible as a relational algebra query And vice versa * Example of an unsafe relational calculus query $\blacksquare \ \{ \ s.name \ \big| \ \neg (s \in Student) \ \}$ · Cannot evaluate this query just by looking at the database

Turing machine?	
❖ Relational algebra has no recursion	
 Example of something not expressible in relational 	-
algebra: Given relation Parent(parent, child), who are	
Bart's ancestors?	
❖ Why not Turing machine?	
Optimization becomes undecidable	
 You can always implement it at the application level 	
❖ Recursion is added to SQL nevertheless!	