Relational Model & Algebra

CPS 116
Introduction to Database Systems

Announcements (Thurs. Aug. 31)

- ❖ Homework #1 will be assigned next Tuesday
- * Office hours: see course Web page
 - Jun: TTH before class
 - Pradeep: MW afternoons
- ❖ Book
 - Read the email for details
 - Demo of Gradiance at the end of this lecture

Relational data model

- ❖ A database is a collection of relations (or tables)
- ❖ Each relation has a list of attributes (or columns)
- Each attribute has a domain (or type)
 - Set-valued attributes not allowed
- ❖ Each relation contains a set of tuples (or rows)
 - Each tuple has a value for each attribute of the relation
 - Duplicate tuples are not allowed
 - Two tuples are identical if they agree on all attributes
- ☞ Simplicity is a virtue!

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Example

Student

SID	name	age	GPA
142	Bart	10	2.3
123	Milhouse	10	3.1
857	Lisa	8	4.3
456	Ralph	8	2.3

CID CPS116

	title
CPS116	Intro. to Database Systems
CPS130	Analysis of Algorithms
CPS114	Computer Networks

Enroll

Ordering of rows doesn't matter (even though the output is always in *some* order)

SID	CID
142	CPS116
142	CPS114
123	CPS116
857	CPS116
857	CPS130
456	CPS114

Schema versus instance

- ❖ Schema (metadata)
 - Specification of how data is to be structured logically
 - Defined at set-up
 - Rarely changes
- ❖ Instance
 - Content
 - Changes rapidly, but always conforms to the schema
- Compare to type and objects of type in a programming language

Example

- ❖ Schema
 - Student (SID integer, name string, age integer, GPA float)
 - Course (CID string, title string)
 - Enroll (SID integer, CID integer)
- **❖** Instance
 - { \langle 142, Bart, 10, 2.3 \rangle, \langle 123, Milhouse, 10, 3.1 \rangle, ... \rangle
 - { (CPS116, Intro. to Database Systems), ...}
 - { (142, CPS116), (142, CPS114), ...}

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Relational algebra A language for querying relational databases based on operators: **Core set of operators: **Selection, projection, cross product, union, difference, and renaming

- * Additional, derived operators:
 - Join, natural join, intersection, etc.
- * Compose operators to make complex queries

Selection

- * Input: a table R
- ❖ Notation: $\sigma_p R$
 - lacksquare p is called a selection condition/predicate
- * Purpose: filter rows according to some criteria
- ❖ Output: same columns as *R*, but only rows of *R* that satisfy *p*

Selection example

❖ Students with GPA higher than 3.0

 $\sigma_{GPA>3.0}$ Student

SID	name	age	GPA		SID	name	age	GPA
142	Bart	10	2.3					
123	Milhouse	10	3.1	$\sigma_{GPA > 3.0}$	123	Milhouse	10	3.1
857	Lisa	8	4.3	GPA > 5.0	857	Lisa	8	4.3
456	Ralph	8	2.3					

More on selection

- ❖ Selection predicate in general can include any column of R, constants, comparisons (=, ≤, etc.), and Boolean connectives (\land : and, \lor : or, and \neg : not)
 - Example: straight A students under 18 or over 21 $\sigma_{GPA \, \geq \, 4.0 \, \land \, (age \, < \, 18 \, \lor \, age \, > \, 21)} Student$
- But you must be able to evaluate the predicate over a single row of the input table
 - Example: student with the highest GPA



Projection

❖ Input: a table R

❖ Notation: $\pi_L R$

• L is a list of columns in R

❖ Purpose: select columns to output

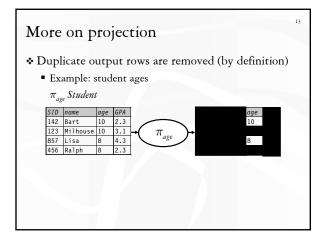
 \diamond Output: same rows, but only the columns in L

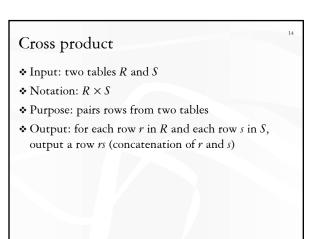
Projection example

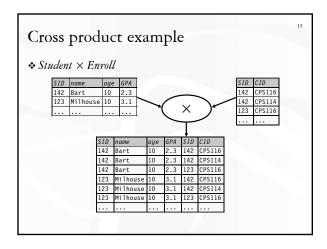
* ID's and names of all students

 $\pi_{SID,\;name}\;Student$

SID	name	age	GPA		SID	name
142	Bart	10	2.3		142	Bart
123	Milhouse	10	3.1	$\rightarrow (\pi_{SID, name}) \rightarrow$	123	Milhouse
857	Lisa	8	4.3	SID, name	857	Lisa
456	Ralph	8	2.3		456	Ralph







A note on column ordering

* The ordering of columns in a table is considered unimportant (as is the ordering of rows)

SID	name	age	GPA	SID	CID
142	Bart	10	2.3	142	CPS116
142	Bart	10	2.3	142	CPS114
142	Bart	10	2.3	123	CPS116
123	Milhouse	10	3.1	142	CPS116
123	Milhouse	10	3.1	142	CPS114
123	Milhouse	10	3.1	123	CPS116

SID	CID	SID	name	age	GPA
142	CPS116	142	Bart	10	2.3
142	CPS114	142	Bart	10	2.3
123	CPS116	142	Bart	10	2.3
142	CPS116	123	Milhouse	10	3.1
142	CPS114	123	Milhouse	10	3.1
123	CPS116	123	Milhouse	10	3.1

* That means cross product is commutative, i.e., $R \times S = S \times R$ for any R and S

Derived operator: join

 \star Input: two tables R and S

❖ Notation: $R \bowtie_{b} S$

p is called a join condition/predicate

❖ Purpose: relate rows from two tables according to some criteria

• Output: for each row r in R and each row s in S, output a row rs if r and s satisfy p

***** Shorthand for σ_p ($R \times S$)

Join example

❖ Info about students, plus CID's of their courses

Student \square \quad \text{Student QID} = Fnroll \quad \text{Enroll} Enroll

SID name age GPA SID CI	D							
142 Bart 10 2.3 142 CP	S116							
	\$114							
Student_SID = 123 CP	S116							
Enroll SID								
Use table_name. column_name syntax								

to disambiguate identically named columns from different input tables

in_name syntax								
SID	name	age	GPA	SID	CID			
142	Bart	10	2.3	142	CPS116			
142	Bart	10	2.3	142	CPS114			
123	Milhouse	10	3.1	123	CPS116			

Derived operator: natural join

 \diamond Input: two tables R and S

❖ Notation: $R \bowtie S$

* Purpose: relate rows from two tables, and

■ Enforce equality on all common attributes

■ Eliminate one copy of common attributes

***** Shorthand for π_L ($R \bowtie_b S$), where

• p equates all attributes common to R and S

■ *L* is the union of all attributes from *R* and *S*, with duplicate attributes removed

Union

 \diamond Input: two tables R and S

❖ Notation: $R \cup S$

 \blacksquare R and S must have identical schema

❖ Output:

■ Has the same schema as R and S

 Contains all rows in R and all rows in S, with duplicate rows eliminated

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 \diamond Input: two tables R and S

❖ Notation: R - S

R and S must have identical schema

❖ Output:

 \blacksquare Has the same schema as R and S

• Contains all rows in *R* that are not found in *S*

Derived operator: intersection

 \diamond Input: two tables R and S

❖ Notation: $R \cap S$

R and S must have identical schema

❖ Output:

• Has the same schema as R and S

Contains all rows that are in both R and S

Renaming

❖ Input: a table R

* Notation: $\rho_{S} R$, $\rho_{(A_1, A_2, ...)} R$ or $\rho_{S(A_1, A_2, ...)} R$

❖ Purpose: rename a table and/or its columns

❖ Output: a renamed table with the same rows as *R*

❖ Used to

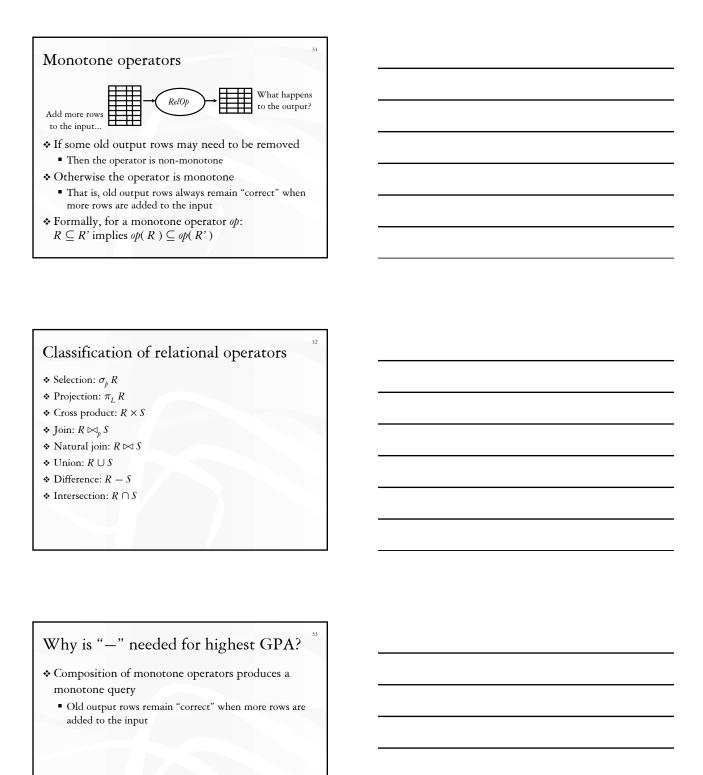
Avoid confusion caused by identical column names

■ Create identical columns names for natural joins

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Renaming example	
SID's of students who take at least two courses	
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Summary of core operators	
\diamond Selection: $\sigma_p R$	
❖ Projection: $\pi_L R$ ❖ Cross product: $R \times S$	
❖ Union: $R \cup S$	
❖ Difference: $R - S$ ❖ Renaming: $\rho_{S(A_1, A_2,)} R$	
■ Does not really add "processing" power	
	<u> </u>
	٦
Summary of derived operators	
❖ Join: $R\bowtie_p S$	
❖ Natural join: $R \bowtie S$ ❖ Intersection: $R \cap S$	
* Intersection: A + 15	
Many moreSemijoin, anti-semijoin, quotient,	
- semijoni, and-semijoni, quotient,	

An exercise	28		
❖ Names of students in Lisa's classes			
Their names			
Students in Lisa's classes			
Lisa's classes			
Who's Lisa?			
Another exercise	29		
* CID's of the courses that Lisa is NOT taking			
. 22 5 57 the courses that Lisa is IVI taking			
	30		
A trickier exercise			
❖ Who has the highest GPA?			
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Why do we need core operator X ?	
❖ Difference	
❖ Cross product	
❖ Union	
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Selection? Projection?	
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Why is r.a. a good query language?	
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Relational calculus	
{ s.SID s ∈ Student ¬(∃s' ∈ Student: s.GPA < s'.GPA) }, or	
$\{s.SID \mid s \in Student \land (\forall s' \in Student : s.GPA \ge s'.GPA)\}$	
❖ Relational algebra = "safe" relational calculus	
Every query expressible as a safe relational calculus query is also expressible as a relational algebra query	
 And vice versa Example of an unsafe relational calculus query 	
 { s.name ¬(s ∈ Student) } Cannot evaluate this query just by looking at the database 	

Turing machine?	
❖ Relational algebra has no recursion	
 Example of something not expressible in relational algebra: Given relation Parent(parent, child), who are 	-
Bart's ancestors? Why not Turing machine?	
Optimization becomes undecidableYou can always implement it at the application level	
* Recursion is added to SQL nevertheless!	