

Announcements (Thurs. Aug. 31)

- \bigstar Homework #1 will be assigned next Tuesday
- * Office hours: see course Web page
 - Jun: TTH afternoon before class
 - Pradeep: MW afternoon
- ♦ Book
 - Read the email for details
 - Demo of Gradiance at the end of this lecture

Relational data model

- * A database is a collection of relations (or tables)
- * Each relation has a list of attributes (or columns)
- * Each attribute has a domain (or type)
- Set-valued attributes not allowed
- \clubsuit Each relation contains a set of tuples (or rows)
 - Each tuple has a value for each attribute of the relation
 - Duplicate tuples are not allowed
 Two tuples are identical if they agree on all attributes

☞ Simplicity is a virtue!

Example Student Course CID title SID name age GPA 142 Bart 10 2.3 CPS116 Intro. to Database Systems Milhous CPS130 Analysis of Algorithms 123 e 10 CPS114 Computer Networks 857 Lisa 456 Ralp Enroll SID CID Ordering of rows doesn't matter 142 CPS116 (even though the output is 142 CPS114 always in some order) 123 CPS116 357 CPS116 CPS130 357 CPS114

Schema versus instance

- Schema (metadata)
 - Specification of how data is to be structured logically
 - Defined at set-up
 - Rarely changes
- ✤ Instance
 - Content
 - Changes rapidly, but always conforms to the schema
- Compare to type and objects of type in a programming language

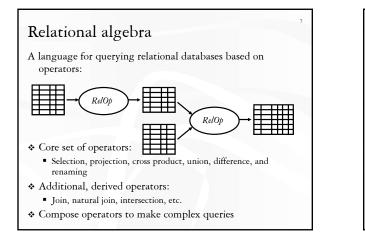
Example

✤ Schema

- Student (SID integer, name string, age integer, GPA float)
- Course (CID string, title string)
- Enroll (SID integer, CID integer)

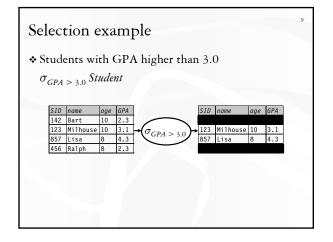
✤ Instance

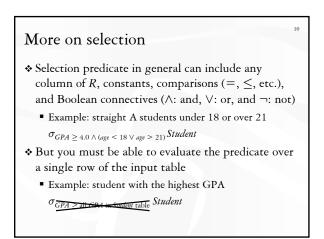
- { (142, Bart, 10, 2.3), (123, Milhouse, 10, 3.1), ...}
- { (CPS116, Intro. to Database Systems), ... }
- { (142, CPS116), (142, CPS114), ...}

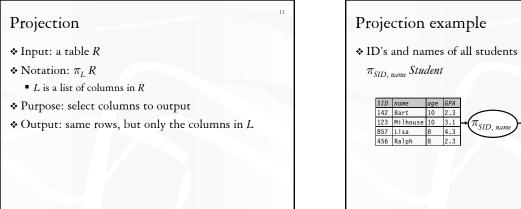


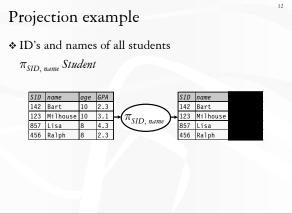
Selection

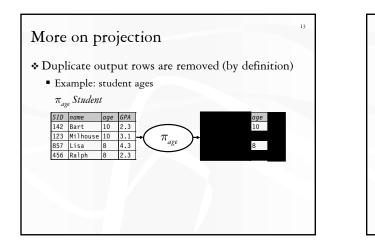
- Input: a table R
- * Notation: $\sigma_{p} R$
 - p is called a selection condition/predicate
- * Purpose: filter rows according to some criteria
- \diamond Output: same columns as *R*, but only rows of *R* that satisfy p





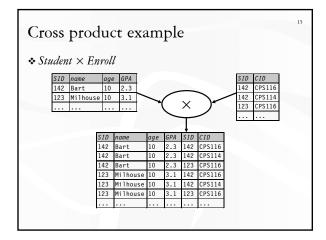






Cross product

- * Input: two tables R and S
- * Notation: $R \times S$
- Purpose: pairs rows from two tables
- Output: for each row r in R and each row s in S, output a row rs (concatenation of r and s)



A note on column ordering

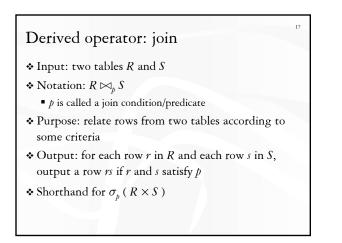
 The ordering of columns in a table is considered unimportant (as is the ordering of rows)

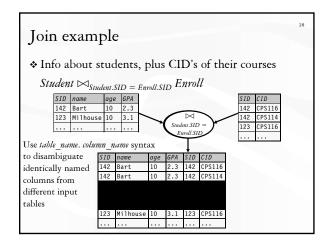
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| SID | name | age | GPA | SID | CID |
|-----|----------|-----|-----|-----|--------|
| 142 | Bart | 10 | 2.3 | 142 | CPS116 |
| 142 | Bart | 10 | 2.3 | 142 | CPS114 |
| 142 | Bart | 10 | 2.3 | 123 | CPS116 |
| 123 | Milhouse | 10 | 3.1 | 142 | CPS116 |
| 123 | Milhouse | 10 | 3.1 | 142 | CPS114 |
| 123 | Milhouse | 10 | 3.1 | 123 | CPS116 |
| | | | | | |

| SID | CID | SID | name | age | GPA |
|-----|--------|-----|----------|-----|-----|
| 142 | CPS116 | 142 | Bart | 10 | 2.3 |
| 142 | CPS114 | 142 | Bart | 10 | 2.3 |
| 123 | CPS116 | 142 | Bart | 10 | 2.3 |
| 142 | CPS116 | 123 | Milhouse | 10 | 3.1 |
| 142 | CPS114 | 123 | Milhouse | 10 | 3.1 |
| 123 | CPS116 | 123 | Milhouse | 10 | 3.1 |
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★ That means cross product is commutative, i.e., $R \times S = S \times R$ for any *R* and *S*

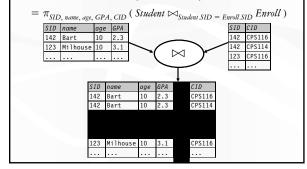




Derived operator: natural join

- * Input: two tables R and S
- * Notation: $R \bowtie S$
- * Purpose: relate rows from two tables, and
 - Enforce equality on all common attributes
 - Eliminate one copy of common attributes
- Shorthand for π_L ($R \bowtie_b S$), where
 - *p* equates all attributes common to *R* and *S*
 - *L* is the union of all attributes from *R* and *S*, with duplicate attributes removed

Natural join example \Rightarrow Student \bowtie Enroll = π , (Student \bowtie , Enroll)



Union

- \bullet Input: two tables R and S
- * Notation: $R \cup S$
- R and S must have identical schema
- Output:
 - Has the same schema as R and S
 - Contains all rows in *R* and all rows in *S*, with duplicate rows eliminated

Difference

- * Input: two tables R and S
- * Notation: R S
- R and S must have identical schema
- * Output:
 - Has the same schema as R and S
 - Contains all rows in R that are not found in S

Derived operator: intersection

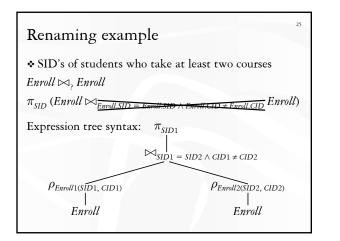
- \bullet Input: two tables *R* and *S*
- ♦ Notation: $R \cap S$
 - R and S must have identical schema
- ♦ Output:
 - Has the same schema as R and S
 - Contains all rows that are in both R and S
- Shorthand for R (R S)
- Also equivalent to S (S R)
- \Rightarrow And to $R \bowtie S$

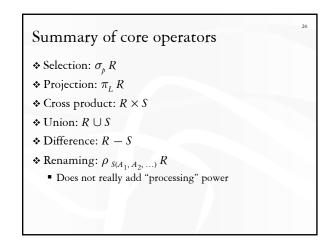
Renaming

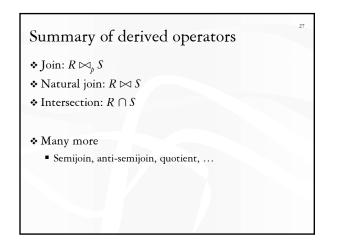
- * Input: a table R
- * Notation: $\rho_S R$, $\rho_{(A_1, A_2, \ldots)} R$ or $\rho_{S(A_1, A_2, \ldots)} R$
- * Purpose: rename a table and/or its columns
- \diamond Output: a renamed table with the same rows as R

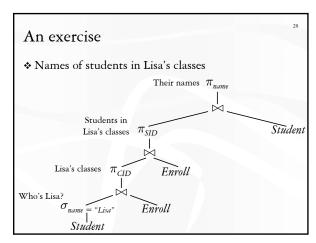
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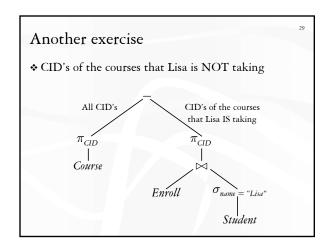
- ✤ Used to
 - Avoid confusion caused by identical column names
 - Create identical columns names for natural joins

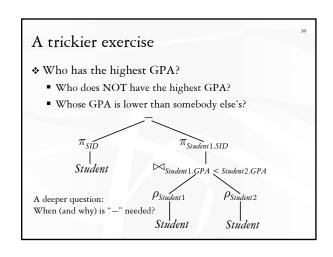


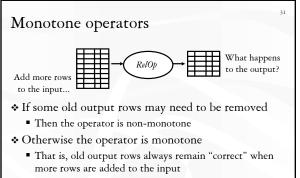












♦ Formally, for a monotone operator op: $R \subseteq R'$ implies $op(R) \subseteq op(R')$

Classification of relational operators

| • Selection: $\sigma_p R$ | Monotone |
|----------------------------------|--|
| • Projection: $\pi_L R$ | Monotone |
| * Cross product: $R \times S$ | Monotone |
| \bigstar Join: $R \bowtie_p S$ | Monotone |
| * Natural join: $R \bowtie S$ | Monotone |
| ♦ Union: $R \cup S$ | Monotone |
| ♦ Difference: $R - S$ | Monotone w.r.t. R ; non-monotone w.r.t S |
| ♦ Intersection: $R \cap S$ | Monotone |
| | |
| | |

Why is "-" needed for highest GPA?

- Composition of monotone operators produces a monotone query
 - Old output rows remain "correct" when more rows are added to the input
- Highest-GPA query is non-monotone
 - Current highest GPA is 4.1
 - Add another GPA 4.2
 - Old answer is invalidated
- ☞ So it must use difference!

Why do we need core operator X?

- Difference
 - The only non-monotone operator
- Cross product
 - The only operator that adds columns
- ✤ Union
 - The only operator that allows you to add rows?
 - A more rigorous argument?
- * Selection? Projection?
 - Homework problem ☺

Why is r.a. a good query language?

* Simple

- A small set of core operators who semantics are easy to grasp
- Declarative?
 - Yes, compared with older languages like CODASYL
 - Though operators do look somewhat "procedural"
- Complete?
 - With respect to what?

Relational calculus

 $\clubsuit \ \{ s.SID \ | \ s \in Student \ \land$

 $\neg(\exists s' \in Student: s.GPA < s'.GPA) \}, or \\ \{ s.SID \mid s \in Student \land \end{cases}$

$$\{\forall s' \in Student: s.GPA \ge s'.GPA\}$$

- Relational algebra = "safe" relational calculus
 - Every query expressible as a safe relational calculus query is also expressible as a relational algebra query
 - And vice versa
- * Example of an unsafe relational calculus query
 - { s.name $| \neg(s \in Student)$ }
 - Cannot evaluate this query just by looking at the database

Turing machine?

- * Relational algebra has no recursion
 - Example of something not expressible in relational algebra: Given relation *Parent(parent, child)*, who are Bart's ancestors?

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- * Why not Turing machine?
 - Optimization becomes undecidable
 - You can always implement it at the application level
- * Recursion is added to SQL nevertheless!