

Relational Database Design Theory

Part I

CPS 116
Introduction to Database Systems

Announcements (September 12)

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- ❖ Homework #1 due next Tuesday
- ❖ Help session this Wednesday
 - 4:30pm or 5:30pm?
 - D344 LSRC
 - Email reminder tonight
- ❖ Course project assigned today
 - Choice of “standard” or “open”
 - Milestone 1 right after fall break
 - But plan/start early!!!

Motivation

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<i>SID</i>	<i>name</i>	<i>CID</i>
142	Bart	CPS116
142	Bart	CPS114
857	Lisa	CPS116
857	Lisa	CPS130
...

- ❖ How do we tell if a design is bad, e.g., *StudentEnroll* (*SID*, *name*, *CID*)?
 - This design has redundancy, because the name of a student is recorded multiple times, once for each course the student is taking
- ❖ How about a systematic approach to detecting and removing redundancy in designs?
 - Dependencies, decompositions, and normal forms

Functional dependencies

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- ❖ A functional dependency (FD) has the form $X \rightarrow Y$, where X and Y are sets of attributes in a relation R
- ❖ $X \rightarrow Y$ means that whenever two tuples in R agree on all the attributes in X , they must also agree on all attributes in Y

X	Y	Z
a	b	c
a	b	?
...

Must be b → ← Could be anything

FD examples

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Address (street_address, city, state, zip)

Keys redefined using FD's

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A set of attributes K is a key for a relation R if

- ❖ $K \rightarrow$ all (other) attributes of R
 - That is, K is a "super key"
- ❖ No proper subset of K satisfies the above condition
 - That is, K is minimal

Reasoning with FD's

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Given a relation R and a set of FD's \mathcal{F}

- ❖ Does another FD follow from \mathcal{F} ?
 - Are some of the FD's in \mathcal{F} redundant (i.e., they follow from the others)?
- ❖ Is K a key of R ?
 - What are all the keys of R ?

Attribute closure

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❖ Given R , a set of FD's \mathcal{F} that hold in R , and a set of attributes Z in R :

The closure of Z (denoted Z^+) with respect to \mathcal{F} is the set of all attributes $\{A_1, A_2, \dots\}$ functionally determined by Z (that is, $Z \rightarrow A_1 A_2 \dots$)

- ❖ Algorithm for computing the closure
 - Start with closure = Z
 - If $X \rightarrow Y$ is in \mathcal{F} and X is already in the closure, then also add Y to the closure
 - Repeat until no more attributes can be added

A more complex example

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StudentGrade (*SID*, *name*, *email*, *CID*, *grade*)

(Not a good design, and we will see why later)

Example of computing closure

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- ❖ \mathcal{F} includes:
 - $SID \rightarrow name, email$
 - $email \rightarrow SID$
 - $SID, CID \rightarrow grade$
- ❖ $\{CID, email\}^+ = ?$
- ❖ $email \rightarrow SID$
 - Add SID ; closure is now $\{CID, email, SID\}$
- ❖ $SID \rightarrow name, email$
 - Add $name, email$; closure is now $\{CID, email, SID, name\}$
- ❖ $SID, CID \rightarrow grade$
 - Add $grade$; closure is now all the attributes in *StudentGrade*

Using attribute closure

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Given a relation R and set of FD's \mathcal{F}

- ❖ Does another FD $X \rightarrow Y$ follow from \mathcal{F} ?
 - Compute X^+ with respect to \mathcal{F}
 - If $Y \subseteq X^+$, then $X \rightarrow Y$ follow from \mathcal{F}
- ❖ Is K a key of R ?

Rules of FD's

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- ❖ Armstrong's axioms
 - Reflexivity: If $Y \subseteq X$, then $X \rightarrow Y$
 - Augmentation: If $X \rightarrow Y$, then $XZ \rightarrow YZ$ for any Z
 - Transitivity: If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$
- ❖ Rules derived from axioms
 - Splitting: If $X \rightarrow YZ$, then $X \rightarrow Y$ and $X \rightarrow Z$
 - Combining: If $X \rightarrow Y$ and $X \rightarrow Z$, then $X \rightarrow YZ$

Using rules of FD's

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Given a relation R and set of FD's \mathcal{F}

❖ Does another FD $X \rightarrow Y$ follow from \mathcal{F} ?

▪ Use the rules to come up with a proof

▪ Example:

• \mathcal{F} includes:

$SID \rightarrow name, email; email \rightarrow SID; SID, CID \rightarrow grade$

• $CID, email \rightarrow grade?$

$email \rightarrow SID$ (given in \mathcal{F})

$CID, email \rightarrow CID, SID$ (augmentation)

$SID, CID \rightarrow grade$ (given in \mathcal{F})

$CID, email \rightarrow grade$ (transitivity)

Non-key FD's

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❖ Consider a non-trivial FD $X \rightarrow Y$ where X is not a super key

▪ Since X is not a super key, there are some attributes (say Z) that are not functionally determined by X

X	Y	Z
a	b	$c1$
a	b	$c2$
...

That a is always associated with b is recorded by multiple rows:
redundancy, update anomaly, deletion anomaly

Example of redundancy

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❖ *StudentGrade* ($SID, name, email, CID, grade$)

❖ $SID \rightarrow name, email$

SID	$name$	$email$	CID	$grade$
142	Bart	bart@fox.com	CPS116	B-
142	Bart	bart@fox.com	CPS114	B
123	Milhouse	milhouse@fox.com	CPS116	B+
857	Lisa	lisa@fox.com	CPS116	A+
857	Lisa	lisa@fox.com	CPS130	A+
456	Ralph	ralph@fox.com	CPS114	C
...

Decomposition

SID	name	email	CID	grade
...

SID	name	email
142	Bart	bart@fox.com
123	Milhouse	milhouse@fox.com
857	Lisa	lisa@fox.com
456	Ralph	ralph@fox.com
...

SID	CID	grade
142	CPS116	B-
142	CPS114	B
123	CPS116	B+
857	CPS116	A+
857	CPS130	A+
456	CPS114	C
...

- ❖ Eliminates redundancy
- ❖ To get back to the original relation:

Unnecessary decomposition

SID	name	email
142	Bart	bart@fox.com
123	Milhouse	milhouse@fox.com
857	Lisa	lisa@fox.com
456	Ralph	ralph@fox.com
...

SID	name
142	Bart
123	Milhouse
857	Lisa
456	Ralph
...	...

SID	email
142	bart@fox.com
123	milhouse@fox.com
857	lisa@fox.com
456	ralph@fox.com
...	...

Bad decomposition

SID	CID	grade
142	CPS116	B-
142	CPS114	B
123	CPS116	B+
857	CPS116	A+
857	CPS130	A+
456	CPS114	C
...

SID	CID
142	CPS116
142	CPS114
123	CPS116
857	CPS116
857	CPS130
456	CPS114
...	...

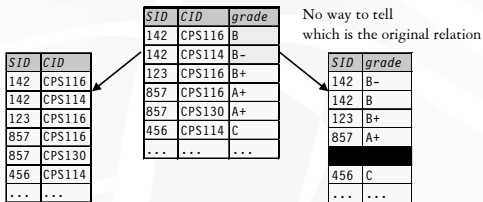
SID	grade
142	B-
142	B
123	B+
857	A+
456	C
...	...

Lossless join decomposition

- ❖ Decompose relation R into relations S and T
 - $attrs(R) = attrs(S) \cup attrs(T)$
 - $S = \pi_{attrs(S)}(R)$
 - $T = \pi_{attrs(T)}(R)$
- ❖ The decomposition is a lossless join decomposition if, given known constraints such as FD's, we can guarantee that $R = S \bowtie T$
- ❖ Any decomposition gives $R \subseteq S \bowtie T$ (why?)
 - A lossy decomposition is one with $R \subset S \bowtie T$

Loss? But I got more rows!

- ❖ "Loss" refers not to the loss of tuples, but to the loss of information
 - Or, the ability to distinguish different original relations



Questions about decomposition

- ❖ When to decompose
- ❖ How to come up with a correct decomposition (i.e., lossless join decomposition)

An answer: BCNF

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- ❖ A relation R is in Boyce-Codd Normal Form if
 - For every non-trivial FD $X \rightarrow Y$ in R , X is a super key
 - That is, all FDs follow from “key \rightarrow other attributes”
- ❖ When to decompose
 - As long as some relation is not in BCNF
- ❖ How to come up with a correct decomposition
 - Always decompose on a BCNF violation (details next)
 - ☞ Then it is guaranteed to be a lossless join decomposition!

BCNF decomposition algorithm

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- ❖ Find a BCNF violation
 - That is, a non-trivial FD $X \rightarrow Y$ in R where X is not a super key of R
- ❖ Decompose R into R_1 and R_2 , where
 - R_1 has attributes $X \cup Y$
 - R_2 has attributes $X \cup Z$, where Z contains all attributes of R that are in neither X nor Y
- ❖ Repeat until all relations are in BCNF

BCNF decomposition example

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StudentGrade (*SID*, *name*, *email*, *CID*, *grade*)
BCNF violation: $SID \rightarrow name, email$

Another example

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StudentGrade (*SID*, *name*, *email*, *CID*, *grade*)

BCNF violation: *email* \rightarrow *SID*

Why is BCNF decomposition lossless

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Given non-trivial $X \rightarrow Y$ in R where X is not a super key of R , need to prove:

❖ Anything we project always comes back in the join:

$$R \subseteq \pi_{XY}(R) \bowtie \pi_{XZ}(R)$$

- Sure; and it doesn't depend on the FD

❖ Anything that comes back in the join must be in the original relation:

$$R \supseteq \pi_{XY}(R) \bowtie \pi_{XZ}(R)$$

- Proof makes use of the fact that $X \rightarrow Y$

Recap

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- ❖ Functional dependencies: a generalization of the key concept
- ❖ Non-key functional dependencies: a source of redundancy
- ❖ BCNF decomposition: a method for removing redundancies
 - BNCf decomposition is a lossless join decomposition
- ❖ BCNF: schema in this normal form has no redundancy due to FD's
