

# Announcements (September 12)

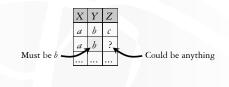
- ✤ Homework #1 due next Tuesday
- Help session this Wednesday
  - 4:30pm or 5:30pm?
  - D344 LSRC
  - Email reminder tonight
- \* Course project assigned today
  - Choice of "standard" or "open"
  - Milestone 1 right after fall break
     But plan/start early!!!

#### Motivation SID name CID 142 Bart CPS116 142 Bart CPS114 857 Lisa CPS116 857 Lisa CPS130 \* How do we tell if a design is bad, e.g., StudentEnroll (SID, name, CID)? This design has redundancy, because the name of a student is recorded multiple times, once for each course the student is taking \* How about a systematic approach to detecting and removing redundancy in designs?

Dependencies, decompositions, and normal forms

# Functional dependencies • A functional dependency (FD) has the form $X \to Y$ ,

- where X and Y are sets of attributes in a relation R
- \*  $X \rightarrow Y$  means that whenever two tuples in R agree on all the attributes in X, they must also agree on all attributes in Y



# FD examplesKeys rAddress (street\_address, city, state, zip) $\land$ street\_address, city, state, zip) $\diamond$ street\_address, city, state $\rightarrow$ zip $\land$ set of a $\diamond$ zip $\rightarrow$ city, state $\checkmark$ K $\rightarrow$ al $\diamond$ zip, state $\rightarrow$ zip? $\land$ that $\diamond$ This is a trivial FD $\diamond$ This is a trivial FD $\bullet$ Trivial FD: LHS $\supseteq$ RHS $\bullet$ That $\diamond$ zip $\rightarrow$ state, zip? $\bullet$ the state, zip?

- This is non-trivial, but not completely non-trivial
- Completely non-trivial FD: LHS  $\cap$  RHS =  $\varnothing$

# Keys redefined using FD's

- A set of attributes K is a key for a relation R if
- $\bigstar K \rightarrow$  all (other) attributes of R
  - That is, K is a "super key"
- \* No proper subset of K satisfies the above condition
  - That is, K is minimal

# Reasoning with FD's

Given a relation R and a set of FD's  $\mathcal{F}$ 

#### $\bullet$ Does another FD follow from $\mathcal{F}$ ?

- Are some of the FD's in  $\mathcal{F}$  redundant (i.e., they follow from the others)?
- \* Is K a key of R?
  - What are all the keys of R?

# Attribute closure

♦ Given *R*, a set of FD's  $\mathcal{F}$  that hold in *R*, and a set of attributes *Z* in *R*: The closure of *Z* (denoted *Z*<sup>+</sup>) with respect to  $\mathcal{F}$  is the set of all attributes {*A*<sub>1</sub>, *A*<sub>2</sub>, ...} functionally

determined by Z (that is,  $Z \rightarrow A_1 A_2 \dots$ )

- \* Algorithm for computing the closure
  - Start with closure = Z
  - If  $X \to Y$  is in  $\mathcal{F}$  and X is already in the closure, then also add Y to the closure
  - Repeat until no more attributes can be added

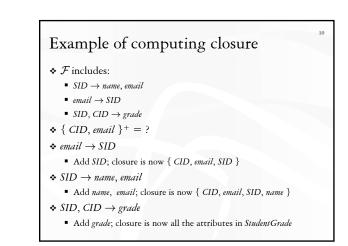
# A more complex example

StudentGrade (SID, name, email, CID, grade)

SID  $\rightarrow$  name, email

- $\bullet$  email  $\rightarrow$  SID
- SID, CID  $\rightarrow$  grade

(Not a good design, and we will see why later)



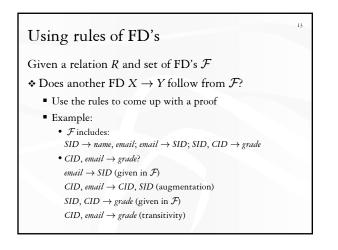
### Using attribute closure

#### Given a relation R and set of FD's ${\mathcal F}$

- \* Does another FD  $X \to Y$  follow from  $\mathcal{F}$ ?
  - Compute  $X^+$  with respect to  ${\mathcal F}$
  - If  $Y \subseteq X^+$ , then  $X \to Y$  follow from  $\mathcal{F}$
- $\bullet$  Is K a key of R?
  - Compute  $K^+$  with respect to  $\mathcal F$
  - If  $K^+$  contains all the attributes of R, K is a super key
  - Still need to verify that K is minimal (how?)

# Rules of FD's \* Armstrong's axioms • Reflexivity: If $Y \subseteq X$ , then $X \to Y$ • Augmentation: If $X \to Y$ , then $XZ \to YZ$ for any Z • Transitivity: If $X \to Y$ and $Y \to Z$ , then $X \to Z$ \* Rules derived from axioms

- Splitting: If  $X \to YZ$ , then  $X \to Y$  and  $X \to Z$
- Combining: If  $X \to Y$  and  $X \to Z$ , then  $X \to YZ$

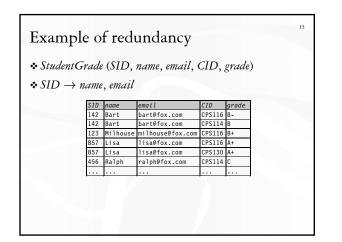


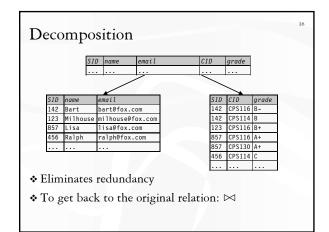
# Non-key FD's

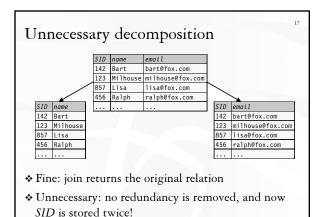
- ♦ Consider a non-trivial FD  $X \to Y$  where X is not a super key
  - Since *X* is not a super key, there are some attributes (say *Z*) that are not functionally determined by *X*

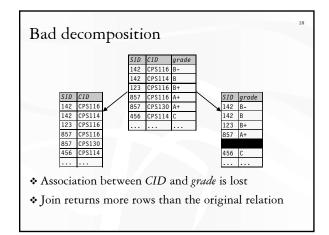
X	Y	Ζ
a	b	с1
d	b	с2

That a is always associated with b is recorded by multiple rows: redundancy, update anomaly, deletion anomaly







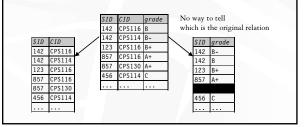


# Lossless join decomposition

- \* Decompose relation R into relations S and T
  - $attrs(R) = attrs(S) \cup attrs(T)$
  - $S = \pi_{attrs(S)}(R)$
  - $T = \pi_{attrs(T)}(R)$
- ♦ The decomposition is a lossless join decomposition if, given known constraints such as FD's, we can guarantee that  $R = S \bowtie T$
- Any decomposition gives R ⊆ S ⋈ T (why?)
  A lossy decomposition is one with R ⊂ S ⋈ T

# Loss? But I got more rows!

- $\boldsymbol{\diamond}$  "Loss" refers not to the loss of tuples, but to the loss of information
  - Or, the ability to distinguish different original relations



# Questions about decomposition When to decompose How to come up with a correct decomposition (i.e., lossless join decomposition)

# An answer: BCNF

- \* A relation R is in Boyce-Codd Normal Form if
  - For every non-trivial FD  $X \to Y$  in R, X is a super key

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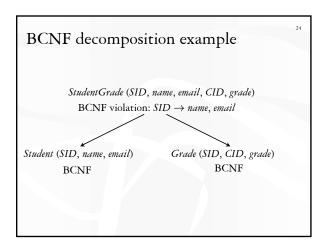
• That is, all FDs follow from "key  $\rightarrow$  other attributes"

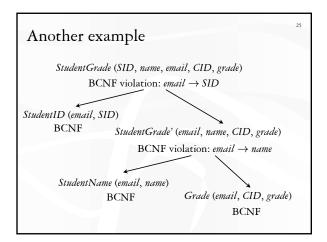
#### \* When to decompose

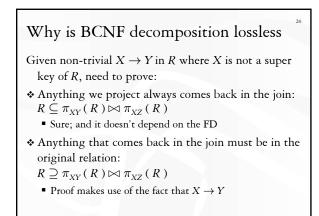
- As long as some relation is not in BCNF
- How to come up with a correct decomposition
  - Always decompose on a BCNF violation (details next)
  - Then it is guaranteed to be a lossless join decomposition!

# BCNF decomposition algorithm

- \* Find a BCNF violation
  - That is, a non-trivial FD  $X \to Y$  in R where X is not a super key of R
- \* Decompose R into  $R_1$  and  $R_2$ , where
  - $R_1$  has attributes  $X \cup Y$
  - $R_2$  has attributes  $X \cup Z$ , where Z contains all attributes of R that are in neither X nor Y
- \* Repeat until all relations are in BCNF







# Recap

Functional dependencies: a generalization of the key concept

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- Non-key functional dependencies: a source of redundancy
- BCNF decomposition: a method for removing redundancies
  - BNCF decomposition is a lossless join decomposition
- BCNF: schema in this normal form has no redundancy due to FD's