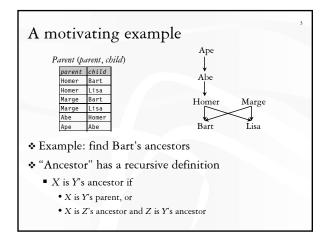
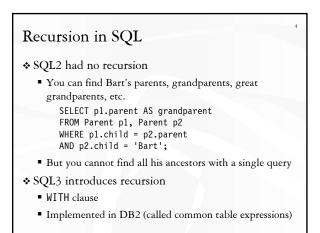


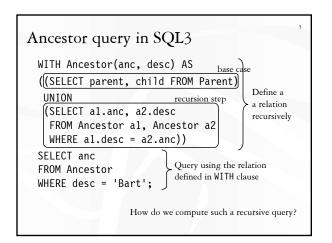
Announcements (October 3)

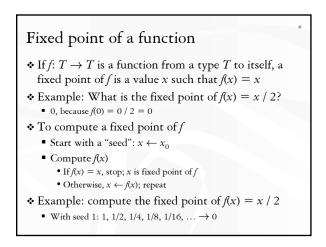
✤ Homework #2 graded

- Solution was emailed during weekend
- * Midterm in class this Thursday
 - Open book, open notes
 - Format similar to the sample midterm
 Solution was emailed during weekend
 - Optional Gradiance problem set for practice is available
 - Covers everything up to today's lecture
 - Emphasizes materials exercised in homeworks
- Project milestone #1 due next Thursday



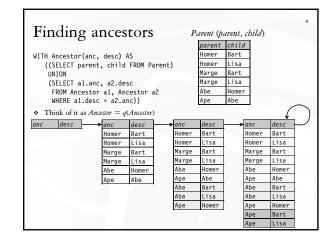






Fixed point of a query

- A query q is just a function that maps an input table to an output table, so a fixed point of q is a table T such that q(T) = T
- To compute fixed point of q
- Start with an empty table: $T \leftarrow \varnothing$
 - Evaluate q over T
 - If the result is identical to T, stop; T is a fixed point
 Otherwise, let T be the new result; repeat
 - Starting from Ø produces the unique minimal fixed point (assuming q is monotone)



Intuition behind fixed-point iteration

- Initially, we know nothing about ancestordescendent relationships
- In the first step, we deduce that parents and children form ancestor-descendent relationships
- In each subsequent steps, we use the facts deduced in previous steps to get more ancestor-descendent relationships
- * We stop when no new facts can be proven

Linear recursion

- With linear recursion, a recursive definition can make only one reference to itself
- Non-linear: WITH Ancestor(anc, desc) AS (SELECT parent, child FROM Parent) UNION (SELECT al.anc, a2.desc FROM Ancestor a1, Ancestor a2 WHERE al.desc = a2.anc))

Linear: WITH Ancestor(an (ISELECT papent)

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WITH Ancestor(anc, desc) AS ((SELECT parent, child FROM Parent) UNION (SELECT anc, child FROM Ancestor, Parent WHERE desc = parent))

Linear vs. non-linear recursion

- * Linear recursion is easier to implement
 - For linear recursion, just keep joining newly generated *Ancestor* rows with *Parent*
 - For non-linear recursion, need to join newly generated *Ancestor* rows with all existing *Ancestor* rows
- Non-linear recursion may take fewer steps to converge, but perform more work
 - Example: $a \to b \to c \to d \to e$
 - Linear recursion takes 4 steps
 - Non-linear recursion takes 3 steps
 More work: e.g., a → d has two different derivations

Mutual recursion example * Table Natural (n) contains 1, 2, ..., 100 * Which numbers are even/odd? An odd number plus 1 is an even number An even number plus 1 is an odd number 1 is an odd number WITH Even(n) AS (SELECT n FROM Natural WHERE n = ANY(SELECT n+1 FROM Odd)), Odd(n) AS (SELECT n FROM Natural WHERE n = 1) UNION (SELECT n FROM Natural WHERE n = ANY(SELECT n+1 FROM Even)))

