

Announcements (November 10)

Course project milestone #2 due today

Overview

- * Many different ways of processing the same query
 - Scan? Sort? Hash? Use an index?
 - All have different performance characteristics and/or make different assumptions about data
- * Best choice depends on the situation
 - Implement all alternatives
 - Let the query optimizer choose at run-time

Notation

- * Relations: R, S
- ♦ Tuples: r, s
- Number of tuples: |R|, |S|
- * Number of disk blocks: B(R), B(S)
- * Number of memory blocks available: M
- Cost metric
 - Number of I/O's
 - Memory requirement

Table scan

- * Scan table R and process the query
 - Selection over R
 - Projection of R without duplicate elimination
- **♦** I/O's: *B*(*R*)
 - Trick for selection: stop early if it is a lookup by key
- Memory requirement: 2 (+1 for double buffering)
- * Not counting the cost of writing the result out
 - Same for any algorithm!
 - Maybe not needed—results may be pipelined into another operator

Nested-loop join

 $R \bowtie_p S$

- For each block of *R*, and for each *r* in the block:
 For each block of *S*, and for each *s* in the block:
 Output *rs* if *p* evaluates to true over *r* and *s*
- *R* is called the outer table; *S* is called the inner table
- I/O's: $B(R) + |R| \cdot B(S)$
- Memory requirement: 3 (+1 for double buffering)
- Improvement:

More improvements of nested-loop join

- Stop early if the key of the inner table is being matched
- * Make use of available memory
 - Stuff memory with as much of *R* as possible, stream *S* by, and join every *S* tuple with all *R* tuples in memory
 - I/O's: $B(R) + [B(R) / (M 2)] \cdot B(S)$ • Or, roughly: $B(R) \cdot B(S) / M$
 - Memory requirement: M (as much as possible)
- * Which table would you pick as the outer?

External merge sort

Remember (internal-memory) merge sort?

Problem: sort R, but R does not fit in memory

- Pass 0: read M blocks of R at a time, sort them, and write out a level-0 run
 - There are $\left\lceil B(R) / M \right\rceil$ level-0 sorted runs
- ◆ Pass *i*: merge (M 1) level-(i-1) runs at a time, and write out a level-*i* run
 - (M-1) memory blocks for input, 1 to buffer output
 - # of level-*i* runs = $\lceil \#$ of level-(*i*-1) runs / (*M* 1) \rceil
- ✤ Final pass produces 1 sorted run

Example of external merge sort

```
★ Input: 1, 7, 4, 5, 2, 8, 3, 6, 9
★ Pass 0
1, 7, 4 → 1, 4, 7
5, 2, 8 → 2, 5, 8
9, 6, 3 → 3, 6, 9
★ Pass 1
1, 4, 7 + 2, 5, 8 → 1, 2, 4, 5, 7, 8
3, 6, 9
★ Pass 2 (final)
1, 2, 4, 5, 7, 8 + 3, 6, 9 → 1, 2, 3, 4, 5, 6, 7, 8, 9
```

Performance of external merge sort

- ♦ Number of passes: $\lceil \log_{M-1} \lceil B(R) / M \rceil \rceil + 1$
- **◊** I/O's
 - Multiply by $2 \cdot B(R)$: each pass reads the entire relation once and writes it once
 - Subtract B(R) for the final pass
 - Roughly, this is $O(B(R) \cdot \log_M B(R))$
- Memory requirement: M (as much as possible)

Some tricks for sorting

- * Double buffering
 - Allocate an additional block for each run

✤ Blocked I/O

 Instead of reading/writing one disk block at time, read/write a bunch ("cluster") 11

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More sequential I/O's

Sort-merge join

 $\bigstar R \bowtie_{R.A = S.B} S$

.

♦ Sort R and S by their join attributes, and then merge r, s = the first tuples in sorted R and S Repeat until one of R and S is exhausted: If r.A > s.B then s = next tuple in S else if r.A < s.B then r = next tuple in R else output all matching tuples, and r, s = next in R and S
♦ I/O's:

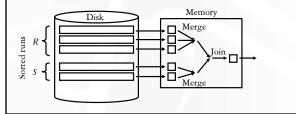
Example			13
$R:$ $r_1.A = 1$ $r_2.A = 3$ $r_3.A = 3$ $r_4.A = 5$ $r_5.A = 7$ $r_7.A = 8$	S: $\Rightarrow s_1.B = 1$ $\Rightarrow s_2.B = 2$ $\Rightarrow s_3.B = 3$ $s_4.B = 3$ $\Rightarrow s_5.B = 8$	$R \bowtie_{R,A} = s,B S:$ $r_{1}s_{1}$ $r_{2}s_{3}$ $r_{2}s_{4}$ $r_{3}s_{3}$ $r_{3}s_{4}$ $r_{7}s_{5}$	

Optimization of SMJ

- ✤ Idea: combine join with the merge phase of merge sort
- * Sort: produce sorted runs of size M for R and S
- Merge and join: merge the runs of *R*, merge the runs of *S*, and merge-join the result streams as they are generated!

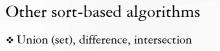
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Performance of two-pass SMJ

- \mathbf{I}/\mathbf{O} 's: $\mathbf{3} \cdot (B(R) + B(S))$
- Memory requirement
 - To be able to merge in one pass, we should have enough memory to accommodate one block from each run: M > B(R) / M + B(S) / M
 - $M > \operatorname{sqrt}(B(R) + B(S))$



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- More or less like SMJ
- * Duplication elimination
 - External merge sort
 Eliminate duplicates in sort and merge
- ✤ GROUP BY and aggregation

External merge sort

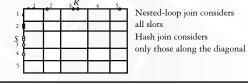
- Produce partial aggregate values in each run
- Combine partial aggregate values during mergePartial aggregate values don't always work though
- Examples: SUM(DISTINCT ...), MEDIAN(...)

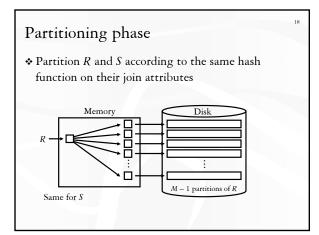
Hash join

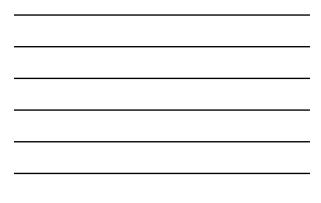
 $R \bowtie_{R,A = S,B} S$

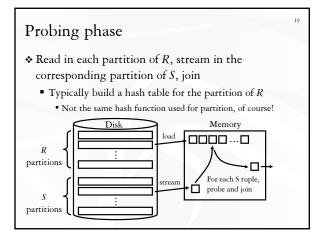
✤ Main idea

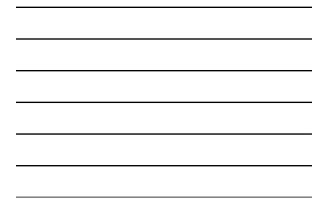
- Partition R and S by hashing their join attributes, and then consider corresponding partitions of R and S
- If *r*.*A* and *s*.*B* get hashed to different partitions, they don't join











Performance of hash join

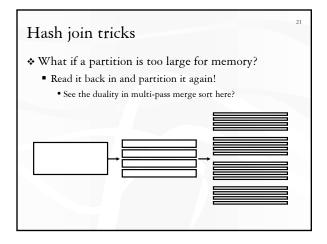
\mathbf{I} O's: 3 · (B(R) + B(S))

* Memory requirement:

• In the probing phase, we should have enough memory to fit one partition of $R: M - 1 \ge B(R) / (M - 1)$

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- $M > \operatorname{sqrt}(B(R))$
- We can always pick R to be the smaller relation, so:
 M > sqrt(min(B(R), B(S)))





Hash join versus SMJ

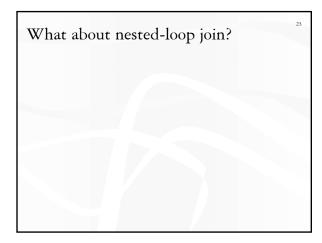
(Assuming two-pass)

- ✤ I/O's: same
- Memory requirement: hash join is lower
 - $\operatorname{sqrt}(\min(B(R), B(S)) < \operatorname{sqrt}(B(R) + B(S))$
 - Hash join wins when two relations have very different sizes

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* Other factors



Other hash-based algorithms

- Union (set), difference, intersection
 - More or less like hash join
- * Duplicate elimination
 - Check for duplicates within each partition/bucket
- ✤ GROUP BY and aggregation
 - Apply the hash functions to GROUP BY attributes
 - Tuples in the same group must end up in the same partition/bucket
 - Keep a running aggregate value for each group

Duality of sort and hash

- Divide-and-conquer paradigm
 - Sorting: physical division, logical combination
 - Hashing: logical division, physical combination
- Handling very large inputs
 - Sorting: multi-level merge
 - Hashing: recursive partitioning
- ✤ I/O patterns
 - Sorting: sequential write, random read (merge)Hashing: random write, sequential read (partition)

Selection using index

- Equality predicate: σ_{A = ν} (R)
 Use an ISAM, B⁺-tree, or hash index on R(A)
- * Range predicate: $\sigma_{A > v}(R)$
 - Use an ordered index (e.g., ISAM or B⁺-tree) on *R*(*A*)
 - Hash index is not applicable
- * Indexes other than those on R(A) may be useful
 - Example: B^+ -tree index on R(A, B)
 - How about B⁺-tree index on R(B, A)?

Index versus table scan

Situations where index clearly wins:

- Index-only queries which do not require retrieving actual tuples
 - Example: $\pi_A (\sigma_{A > v}(R))$
- Primary index clustered according to search key
 - One lookup leads to all result tuples in their entirety

Index versus table scan (cont'd)

BUT(!):

- ♦ Consider $\sigma_{A > v}(R)$ and a secondary, non-clustered index on R(A)
 - Need to follow pointers to get the actual result tuples
 - Say that 20% of R satisfies A > v
 Could happen even for equality predicates
 - I/O's for index-based selection: lookup + 20% |R|
 - I/O's for scan-based selection: B(R)
 - Table scan wins if a block contains more than 5 tuples

Index nested-loop join

- $R \bowtie_{R.A = S.B} S$
- * Idea: use the value of R.A to probe the index on S(B)

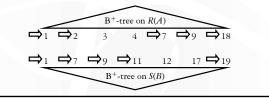
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- For each block of *R*, and for each *r* in the block: Use the index on S(B) to retrieve *s* with *s*.B = r.AOutput *rs*
- $I/O's: B(R) + |R| \cdot (index lookup)$
 - Typically, the cost of an index lookup is 2-4 I/O's
 - Beats other join methods if |R| is not too big
 - Better pick R to be the smaller relation
- Memory requirement: 2

Zig-zag join using ordered indexes

 $R \bowtie_{R.A = S.B} S$

- ✤ Idea: use the ordering provided by the indexes on *R*(*A*) and *S*(*B*) to eliminate the sorting step of sort-merge join
- Trick: use the larger key to probe the other indexPossibly skipping many keys that don't match



Summary of tricks

♦ Scan

- Selection, duplicate-preserving projection, nested-loop join
- ✤ Sort
 - External merge sort, sort-merge join, union (set), difference, intersection, duplicate elimination, GROUP BY and aggregation

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- **∻** Hash
 - Hash join, union (set), difference, intersection, duplicate elimination, GROUP BY and aggregation
- ✤ Index
 - Selection, index nested-loop join, zig-zag join