## Query Processing

CPS 116
Introduction to Database Systems

## Announcements (November 10)

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* Course project milestone \#2 due today


## Overview

Many different ways of processing the same query

- Scan? Sort? Hash? Use an index?
- All have different performance characteristics and/or make different assumptions about data
* Best choice depends on the situation
- Implement all alternatives
- Let the query optimizer choose at run-time


## Notation

$\star$ Relations: $R, S$

* Tuples: $r$, $s$
* Number of tuples: $|R|,|S|$
* Number of disk blocks: $B(R), B(S)$
* Number of memory blocks available: $M$
* Cost metric
- Number of I/O's
- Memory requirement


## Table scan

* Scan table $R$ and process the query
- Selection over $R$
- Projection of $R$ without duplicate elimination
* I/O's: $B(R)$
- Trick for selection: stop early if it is a lookup by key
* Memory requirement: 2 ( +1 for double buffering)
$\star$ Not counting the cost of writing the result out
- Same for any algorithm!
- Maybe not needed—results may be pipelined into another operator


## Nested-loop join

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* $R \bowtie_{p} S$
* For each block of $R$, and for each $r$ in the block:
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For each block of $S$, and for each $s$ in the block: Output $r s$ if $p$ evaluates to true over $r$ and $s$ $\qquad$
- $R$ is called the outer table; $S$ is called the inner table
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* Memory requirement: 3 ( +1 for double buffering)
* Improvement:


## More improvements of nested-loop join

* Stop early if the key of the inner table is being matched
* Make use of available memory
- Stuff memory with as much of $R$ as possible, stream $S$ by, and join every $S$ tuple with all $R$ tuples in memory
- I/O's: $B(R)+\lceil B(R) /(M-2)\rceil \cdot B(S)$
- Or, roughly: $B(R) \cdot B(S) / M$
- Memory requirement: $M$ (as much as possible)
* Which table would you pick as the outer?


## External merge sort

Remember (internal-memory) merge sort?
Problem: sort $R$, but $R$ does not fit in memory

* Pass 0 : read $M$ blocks of $R$ at a time, sort them, and write out a level-0 run
- There are $\lceil B(R) / M\rceil$ level- 0 sorted runs
* Pass $i$ : merge ( $M-1$ ) level-( $i-1$ ) runs at a time, and write out a level- $i$ run
- ( $M-1$ ) memory blocks for input, 1 to buffer output
- \# of level- $i$ runs $=\lceil \#$ of level- $(i-1)$ runs $/(M-1)\rceil$
* Final pass produces 1 sorted run


## Example of external merge sort

* Input: 1, 7, 4, 5, 2, 8, 3, 6, 9
* Pass 0
- 1, 7, $4 \rightarrow 1,4,7$
- 5, 2, $8 \rightarrow 2,5,8$
- 9, 6, $3 \rightarrow 3,6,9$

Pass 1

- $1,4,7+2,5,8 \rightarrow 1,2,4,5,7,8$
- 3, 6, 9

Pass 2 (final)

- $1,2,4,5,7,8+3,6,9 \rightarrow 1,2,3,4,5,6,7,8,9$


## Performance of external merge sort

$\star$ Number of passes: $\left\lceil\log _{M-1}\lceil B(R) / M\rceil\right\rceil+1$

* I/O's
- Multiply by $2 \cdot B(R)$ : each pass reads the entire relation once and writes it once
- Subtract $B(R)$ for the final pass
- Roughly, this is $O\left(B(R) \cdot \log _{M} B(R)\right)$
* Memory requirement: $M$ (as much as possible)


## Some tricks for sorting

* Double buffering
- Allocate an additional block for each run
* Blocked I/O
- Instead of reading/writing one disk block at time, read/write a bunch ("cluster")
- More sequential I/O’s


## Sort-merge join

```
*R}\mp@subsup{\bowtie}{R.A = S.B}{}
```

* Sort $R$ and $S$ by their join attributes, and then merge $r, s=$ the first tuples in sorted $R$ and $S$ Repeat until one of $R$ and $S$ is exhausted: If $r . A>s . B$ then $s=$ next tuple in $S$ else if $r . A<s . B$ then $r=$ next tuple in $R$ else output all matching tuples, and

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r, s=\text { next in } R \text { and } S
$$

$\%$ I/O's:
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| Example |  |  |  |
| :---: | :---: | :---: | :---: |
| $R:$ | $S:$ | $R \bowtie_{R \cdot A}=s_{1} S:$ |  |
| $\Rightarrow r_{1} \cdot A=1$ | $\Rightarrow s_{1} \cdot B=1$ | $r_{1} s_{1}$ |  |
| $\Rightarrow r_{2} \cdot A=3$ | $\Rightarrow s_{2} \cdot B=2$ | $r_{2} s_{3}$ |  |
| $r_{3} \cdot A=3$ | $\Rightarrow s_{3} \cdot B=3$ | $r_{2} s_{4}$ |  |
| $\Rightarrow r_{4} \cdot A=5$ | $s_{4} \cdot B=3$ | $r_{3} s_{3}$ |  |
| $\Rightarrow r_{5} \cdot A=7$ | $\Rightarrow s_{5} \cdot B=8$ | $r_{3} s_{4}$ |  |
| $\Rightarrow r_{6} \cdot A=7$ |  | $r_{7} s_{5}$ |  |
| $\Rightarrow r_{7} \cdot A=8$ |  |  |  |
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$$
\begin{array}{rcc}
R: & S: & R \bowtie_{R \cdot A}=s_{5} S: \\
\Rightarrow r_{1} \cdot A=1 & \Rightarrow s_{1} \cdot B=1 & r_{1} s_{1} \\
\Rightarrow r_{2} \cdot A=3 & \Rightarrow s_{2} \cdot B=2 & r_{2} s_{3} \\
r_{3} \cdot A=3 & \Rightarrow s_{3} \cdot B=3 & r_{2} s_{4} \\
\Rightarrow r_{4} \cdot A=5 & s_{4} \cdot B=3 & r_{3} s_{3} \\
\Rightarrow r_{5} \cdot A=7 & \Rightarrow s_{5} \cdot B=8 & r_{3} s_{4} \\
\Rightarrow r_{6} \cdot A=7 & & r_{7} s_{5} \\
\Rightarrow r_{7} \cdot A=8 & &
\end{array}
$$

## Optimization of SMJ

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* Idea: combine join with the merge phase of merge sort
$\star$ Sort: produce sorted runs of size $M$ for $R$ and $S$
$*$ Merge and join: merge the runs of $R$, merge the runs of $S$, and merge-join the result streams as they are generated!



## Performance of two-pass SMJ

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* I/O's: $3 \cdot(B(R)+B(S))$
$\star$ Memory requirement
- To be able to merge in one pass, we should have enough memory to accommodate one block from each run: $M>$ $B(R) / M+B(S) / M$
- $M>\operatorname{sqrt}(B(R)+B(S))$


## Other sort-based algorithms

* Union (set), difference, intersection
- More or less like SMJ
* Duplication elimination
- External merge sort
- Eliminate duplicates in sort and merge
* GROUP BY and aggregation
- External merge sort
- Produce partial aggregate values in each run
- Combine partial aggregate values during merge
- Partial aggregate values don't always work though - Examples: SUM (DISTINCT ...), MEDIAN(...)


## Hash join

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$\because R \bowtie_{R . A=S . B} S$
$*$ Main idea

- Partition $R$ and $S$ by hashing their join attributes, and then consider corresponding partitions of $R$ and $S$
- If $r . A$ and s. $B$ get hashed to different partitions, they don't join


Nested-loop join considers all slots
Hash join considers only those along the diagonal
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## Partitioning phase

Partition $R$ and $S$ according to the same hash function on their join attributes


## Probing phase

* Read in each partition of $R$, stream in the corresponding partition of $S$, join
- Typically build a hash table for the partition of $R$
- Not the same hash function used for partition, of course!



## Performance of hash join

* I/O's: $3 \cdot(B(R)+B(S))$
$\star$ Memory requirement:
- In the probing phase, we should have enough memory to fit one partition of $R: M-1 \geq B(R) /(M-1)$
- $M>\operatorname{sqrt}(B(R))$
- We can always pick $R$ to be the smaller relation, so: $M>\operatorname{sqrt}(\min (B(R), B(S))$


## Hash join tricks

*What if a partition is too large for memory?

- Read it back in and partition it again!
- See the duality in multi-pass merge sort here?



## Hash join versus SMJ

(Assuming two-pass)

* I/O's: same
* Memory requirement: hash join is lower
- $\operatorname{sqrt}(\min (B(R), B(S))<\operatorname{sqrt}(B(R)+B(S))$
- Hash join wins when two relations have very different sizes
* Other factors
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## What about nested-loop join?

## Other hash-based algorithms

※ Union (set), difference, intersection

- More or less like hash join
* Duplicate elimination
- Check for duplicates within each partition/bucket

GROUP BY and aggregation

- Apply the hash functions to GROUP BY attributes
- Tuples in the same group must end up in the same partition/bucket
- Keep a running aggregate value for each group
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## Duality of sort and hash

* Divide-and-conquer paradigm
- Sorting: physical division, logical combination
- Hashing: logical division, physical combination
$\star$ Handling very large inputs
- Sorting: multi-level merge
- Hashing: recursive partitioning
* I/O patterns
- Sorting: sequential write, random read (merge)
- Hashing: random write, sequential read (partition)


## Selection using index

Equality predicate: $\sigma_{A=v}(R)$

- Use an ISAM, $\mathrm{B}^{+}$-tree, or hash index on $R(A)$

Range predicate: $\sigma_{A>v}(R)$

- Use an ordered index (e.g., ISAM or $\mathrm{B}^{+}$-tree) on $R(A)$
- Hash index is not applicable
* Indexes other than those on $R(A)$ may be useful
- Example: $\mathrm{B}^{+}$-tree index on $R(A, B)$
- How about $\mathrm{B}^{+}$-tree index on $R(B, A)$ ?


## Index versus table scan

Situations where index clearly wins:

* Index-only queries which do not require retrieving actual tuples
- Example: $\pi_{A}\left(\sigma_{A>v}(R)\right)$
* Primary index clustered according to search key
- One lookup leads to all result tuples in their entirety


## Index versus table scan (cont'd)

BUT(!):

* Consider $\sigma_{A>v}(R)$ and a secondary, non-clustered index on $R(A)$
- Need to follow pointers to get the actual result tuples
- Say that $20 \%$ of $R$ satisfies $A>v$
- Could happen even for equality predicates
- I/O's for index-based selection: lookup $+20 \%|R|$
- I/O's for scan-based selection: $B(R)$
- Table scan wins if a block contains more than 5 tuples


## Index nested-loop join

$* R \bowtie_{R . A=S . B} S$

* Idea: use the value of $R . A$ to probe the index on $S(B)$
$\star$ For each block of $R$, and for each $r$ in the block:
Use the index on $S(B)$ to retrieve $s$ with $s . B=r . A$ Output $r s$
* I/O's: $B(R)+|R| \cdot($ index lookup)
- Typically, the cost of an index lookup is 2-4 I/O's
- Beats other join methods if $|R|$ is not too big
- Better pick $R$ to be the smaller relation
* Memory requirement: 2


## Zig-zag join using ordered indexes

$* R \bowtie_{R . A=S . B} S$

* Idea: use the ordering provided by the indexes on $R(A)$ and $S(B)$ to eliminate the sorting step of sort-merge join
* Trick: use the larger key to probe the other index
- Possibly skipping many keys that don't match

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## Summary of tricks

* Scan
- Selection, duplicate-preserving projection, nested-loop join
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* Sort
- External merge sort, sort-merge join, union (set), difference, intersection, duplicate elimination, GROUP BY and aggregation
* Hash $\qquad$
- Hash join, union (set), difference, intersection, duplicate elimination, GROUP BY and aggregation
* Index
- Selection, index nested-loop join, zig-zag join

