

More recursion

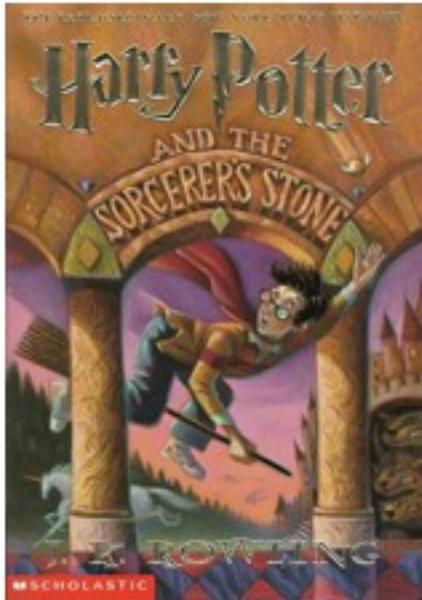


Duke Computer Science

What we are doing



- Intro to Markov (by request)
- More recursion
 - recursion()
 - recursion()



- Harry -> Potter
- Dark -> Lord -> Arts
- Magic -> Wand



gy independence on something firmer, and more honest in our battlefields may be Democrats and Republican nominee, John McCain, I will stop giving them to companies stop discriminating against those wi

Brute-Force



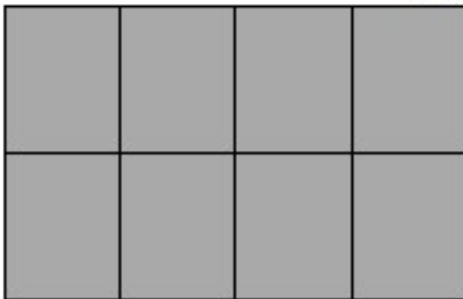
- seed = random k-character substring from the training text --- the *initial seed*
- repeat N times to generate N random letters
 - for each occurrence of seed in training text
 - record the letter that follows the occurrence of seed in a list
 - choose a random element of the list as the generated letter C
 - print or store C
 - seed = (last k-1 characters of seed) + C

5

Brute-Force



bbbabbabbbaba



```
public void bruter(int k, int numLetters) {  
    // pick random k-character substring as initial seed  
    int start = myRandom.nextInt(myString.length() - k + 1);  
    String seed = myString.substring(start, start + k);  
  
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    StringBuilder build = new StringBuilder();  
    ArrayList<Character> list = new ArrayList<Character>();  
  
    for (int i = 0; i < numLetters; i++) {  
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        int pick = myRandom.nextInt(list.size());  
        char ch = list.get(pick);  
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Look at code on your computer so you can read it!!!!!!

6

Brute-Force



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Brute-Force



bbbabbabbbaba

bba	b		

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Brute-Force



bbbabbbbbaba

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bab			

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Brute-Force



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Questions?



Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```


Factorial



```
long fact(long i) {          fact(5);
    if (i == 1) {
        return 1;
    }

    long c = fact(i-1);
    return i * c;
}
```

9

Factorial



```
long fact(long i) {          fact(5);
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```

Call Stack



10

Factorial



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```

Call Stack



11

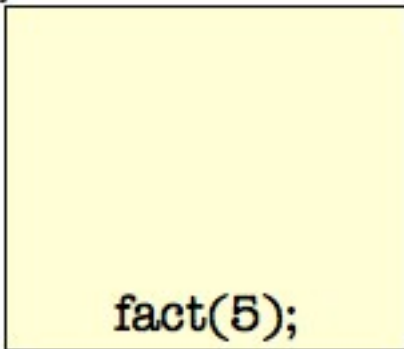
Factorial



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Call Stack



11

Factorial



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Call Stack

fact(5);

11

Factorial



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Call Stack

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Factorial



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    fact(5);  
}
```

```
long c = fact(i-1);  
return i * c;
```

Call Stack

fact(5);

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
    fact(5);  
    c = fact(4);  
}
```

```
long c = fact(i-1);  
return i * c;
```

Call Stack

fact(5);

11

Factorial



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long fact(long i) {  
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}
```

```
fact(5);  
    c = fact(4);
```

Call Stack

```
fact(4);  
fact(5);
```

11

Factorial



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long fact(long i) {  
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```

```
fact(5);  
    c = fact(4);
```

Call Stack

```
fact(4);  
fact(5);
```

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Factorial



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```
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```

```
fact(5);  
    c = fact(4);
```

Call Stack

```
fact(4);  
fact(5);
```

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Factorial



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Call Stack

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fact(4);  
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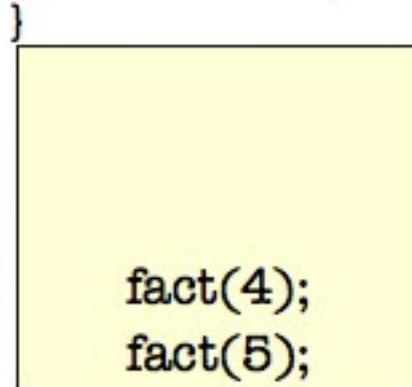
Factorial



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```

```
fact(5);  
    c = fact(4);  
    c = fact(3);
```

```
long c = fact(i-1);  
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Call Stack

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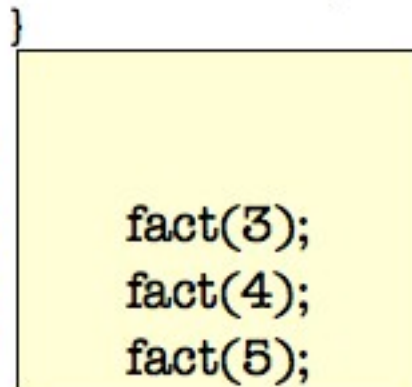
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long fact(long i) {  
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        return 1;  
    }  
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);
```

```
long c = fact(i-1);  
return i * c;
```



Call Stack

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);
```

Call Stack

```
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);
```

Call Stack

```
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

```
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);
```

Call Stack

```
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

```
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);  
    c = fact(2);
```

Call Stack

```
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

```
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);  
    c = fact(2);
```

Call Stack

```
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

```
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);  
    c = fact(2);
```

Call Stack

```
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);  
    c = fact(2);
```

Call Stack

```
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);  
    c = fact(2);
```

Call Stack

```
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

```
}
```

```
fact(5);
```

```
    c = fact(4);
```

```
    c = fact(3);
```

```
    c = fact(2);
```

```
    c = fact(1);
```

Call Stack

```
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

```
}
```

```
fact(5);
```

```
    c = fact(4);
```

```
    c = fact(3);
```

```
    c = fact(2);
```

```
    c = fact(1);
```

Call Stack

```
fact(1);  
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }
```

```
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);
```

```
    c = fact(4);
```

```
    c = fact(3);
```

```
    c = fact(2);
```

```
    c = fact(1);
```

Call Stack

```
fact(1);
```

```
fact(2);
```

```
fact(3);
```

```
fact(4);
```

```
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }
```

```
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);
```

```
    c = fact(4);
```

```
    c = fact(3);
```

```
    c = fact(2);
```

```
    c = fact(1);
```

Call Stack

```
fact(1);
```

```
fact(2);
```

```
fact(3);
```

```
fact(4);
```

```
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);  
  
    c = fact(4);  
    c = fact(3);  
  
    c = fact(2);  
    c = fact(1);
```

Call Stack

```
fact(1);  
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);  
  
    c = fact(4);  
    c = fact(3);  
  
    c = fact(2);  
    c = fact(1);  
  
    fact(1) = 1
```

Call Stack

```
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

```
}
```

Call Stack

```
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

```
fact(5);
```

```
c = fact(4);
```

```
c = fact(3);
```

```
c = fact(2);
```

```
c = fact(1);
```

```
fact(1) = 1
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

```
}
```

Call Stack

```
fact(2);  
fact(3);  
fact(4);  
fact(5);
```

```
fact(5);
```

```
c = fact(4);
```

```
c = fact(3);
```

```
c = fact(2);
```

```
c = fact(1);
```

```
fact(1) = 1
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);  
    c = fact(2);  
    c = fact(1);  
    fact(1) = 1  
    fact(2) = 2 * 1
```

Call Stack

```
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

```
fact(5);  
    c = fact(4);  
    c = fact(3);  
    c = fact(2);  
    c = fact(1);  
    fact(1) = 1  
    fact(2) = 2 * 1
```

Call Stack

```
fact(3);  
fact(4);  
fact(5);
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

Call Stack

```
fact(3);  
fact(4);  
fact(5);
```

```
fact(5);  
    c = fact(4);  
        c = fact(3);  
            c = fact(2);  
                c = fact(1);  
                    fact(1) = 1  
                        fact(2) = 2 * 1
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

Call Stack

```
fact(4);  
fact(5);
```

```
fact(5);  
    c = fact(4);  
        c = fact(3);  
            c = fact(2);  
                c = fact(1);  
                    fact(1) = 1  
                        fact(2) = 2 * 1  
                            fact(3) = 3 * 2 * 1
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

Call Stack

```
fact(4);  
fact(5);
```

```
fact(5);
```

```
c = fact(4);
```

```
c = fact(3);
```

```
c = fact(2);
```

```
c = fact(1);
```

```
fact(1) = 1
```

```
fact(2) = 2 * 1
```

```
fact(3) = 3 * 2 * 1
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

Call Stack

```
fact(4);  
fact(5);
```

```
fact(5);
```

```
c = fact(4);
```

```
c = fact(3);
```

```
c = fact(2);
```

```
c = fact(1);
```

```
fact(1) = 1
```

```
fact(2) = 2 * 1
```

```
fact(3) = 3 * 2 * 1
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

Call Stack

fact(5);

```
fact(5);  
    c = fact(4);  
    c = fact(3);  
    c = fact(2);  
    c = fact(1);  
    fact(1) = 1  
    fact(2) = 2 * 1  
    fact(3) = 3 * 2 * 1
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
  
    long c = fact(i-1);  
    return i * c;  
}
```

Call Stack

fact(5);

```
fact(5);  
    c = fact(4);  
    c = fact(3);  
    c = fact(2);  
    c = fact(1);  
    fact(1) = 1  
    fact(2) = 2 * 1  
    fact(3) = 3 * 2 * 1  
    fact(4) = 4 * 3 * 2 * 1
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

Call Stack

```
fact(5);
```

```
fact(5);
```

```
    c = fact(4);
```

```
    c = fact(3);
```

```
    c = fact(2);
```

```
    c = fact(1);
```

```
    fact(1) = 1
```

```
    fact(2) = 2 * 1
```

```
    fact(3) = 3 * 2 * 1
```

```
    fact(4) = 4 * 3 * 2 * 1
```

11

Factorial



```
long fact(long i) {  
    if (i == 1) {  
        return 1;  
    }  
}
```

```
long c = fact(i-1);  
return i * c;
```

Call Stack

```
fact(5);
```

```
    c = fact(4);
```

```
    c = fact(3);
```

```
    c = fact(2);
```

```
    c = fact(1);
```

```
    fact(1) = 1
```

```
    fact(2) = 2 * 1
```

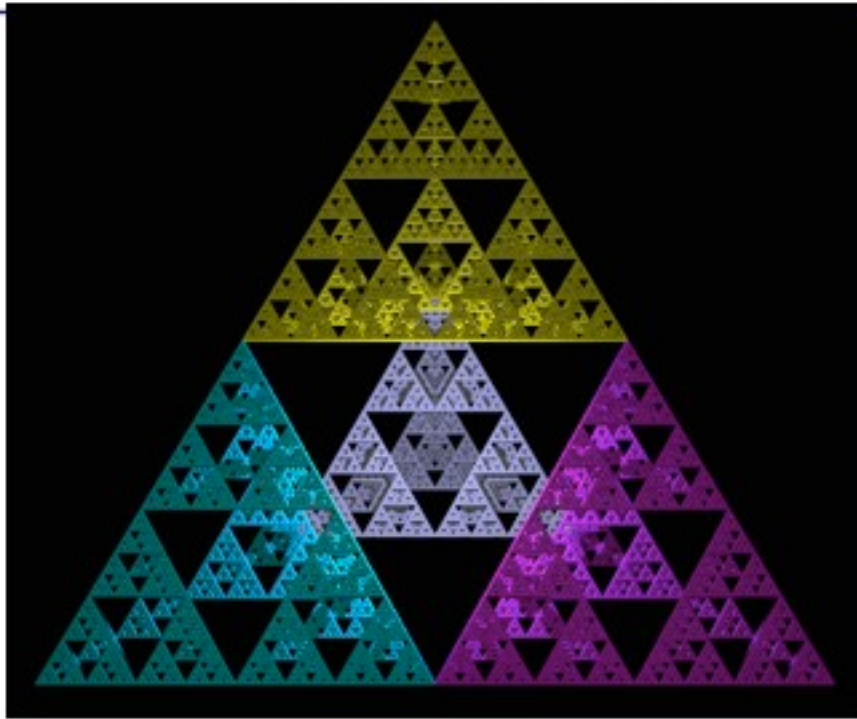
```
    fact(3) = 3 * 2 * 1
```

```
    fact(4) = 4 * 3 * 2 * 1
```

```
    fact(5) = 5 * 4 * 3 * 2 * 1
```

11

Fractals



fractals.chat.ru

Code time



Practice



- <http://codingbat.com/java/Recursion-1>
 - triangle
 - sumDigits
 - countHi
 - hint: look at Java String functions
- Put all three methods in ONE java file names Recitation5.java and submit via ambient.