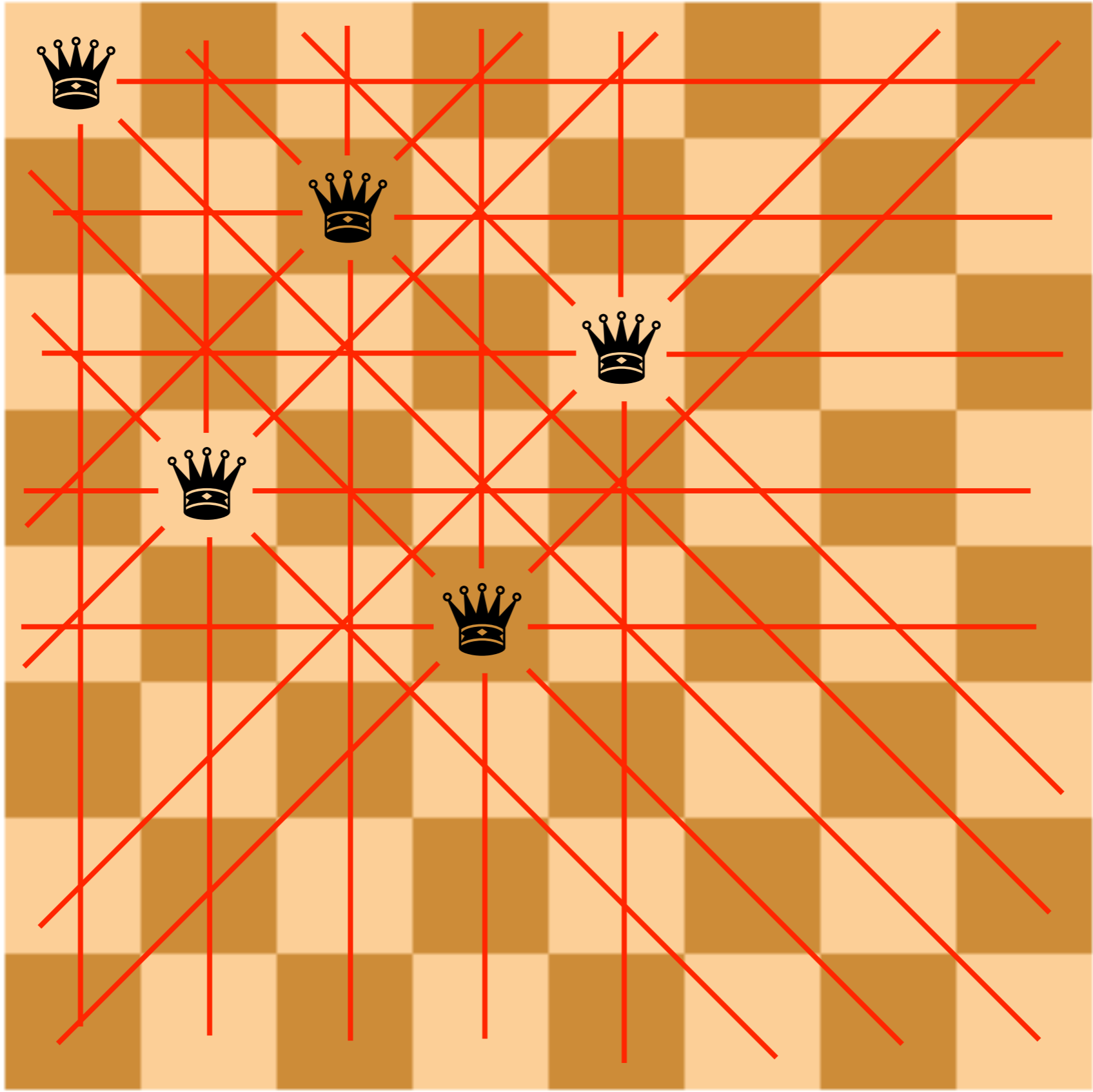


Recursive Backtracking, Round 2

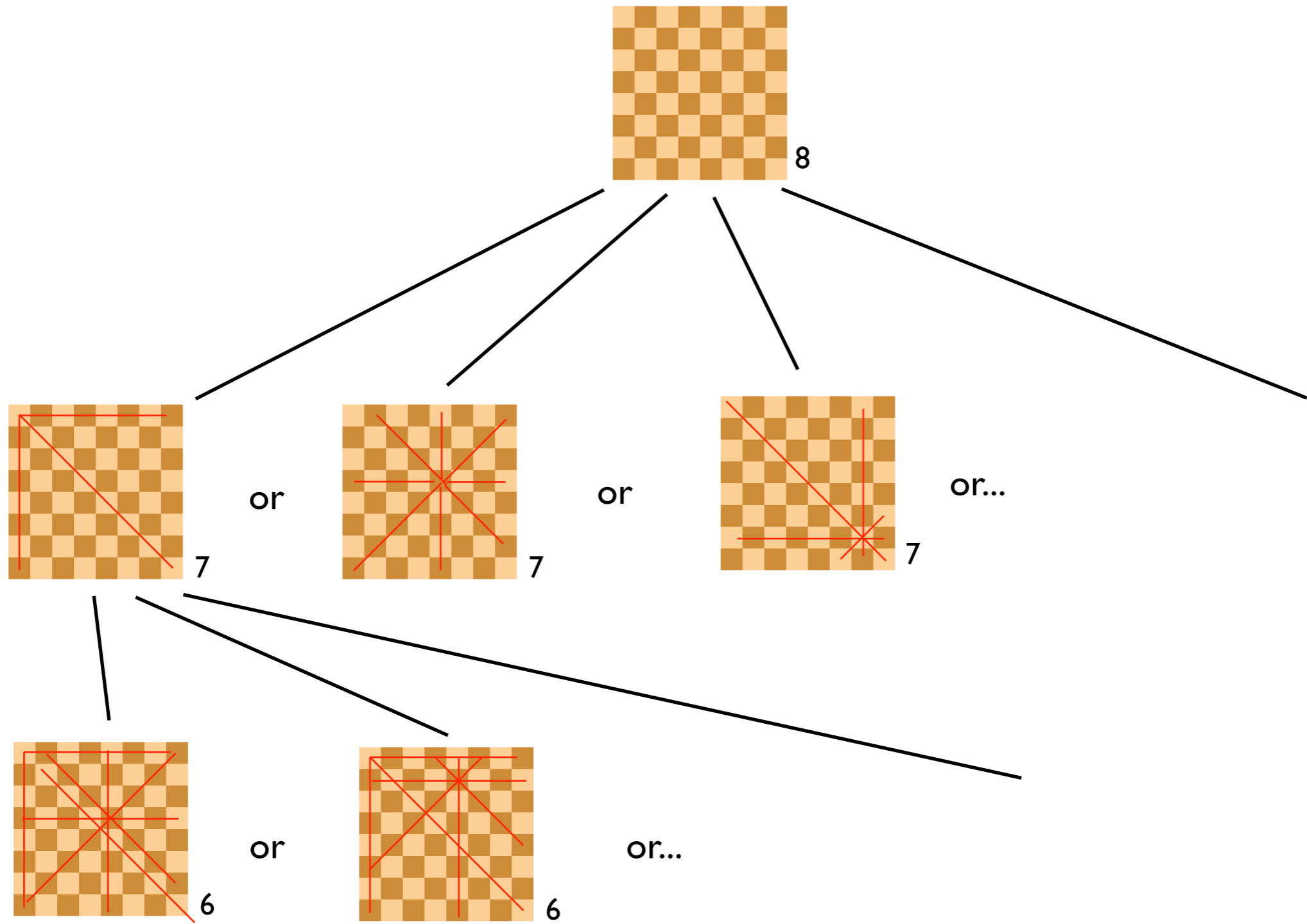
(And recursive backtracking with no “backtracking”)



Remember this?



Recursive Backtracking



The pattern

You have some *state*.

Chessboard
Sudoku board
Boggle board
(and non-board things)

The pattern

You have some *state*.

Chessboard
Sudoku board
Boggle board
(and non-board things)

If you're in a winning state, hooray! *Base Case*

For each action you can take:

- Take that action.
- Recurse.
- See what happened.

Place a queen
Pick a number
Try a direction
(your problem here)

mazeEscape

| | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 | X | X | . | X | X |
| 1 | X | . | . | . | . |
| 2 | X | X | X | X | X |

Can you escape from (r, c) in this maze in *exactly* n steps?

```
public boolean mazeEscape(char[][] map, int row, int col, int steps) {
```

mazeEscape

| | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 | X | X | . | X | X |
| 1 | X | . | . | . | . |
| 2 | X | X | X | X | X |

Can you escape from (r, c) in this maze in *exactly* n steps?

(1, 1, 3) => true

(1, 1, 4) => true

(1, 1, _) => false

```
public boolean mazeEscape(char[][] map, int row, int col, int steps) {
```

Hint: your state is all four of these parameters!

A variation

1

| | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 | X | X | . | X | X |
| 1 | X | • | . | . | . |
| 2 | X | X | X | X | X |

2

| | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 | X | X | . | X | X |
| 1 | X | X | • | . | . |
| 2 | X | X | X | X | X |

3

| | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 | X | X | • | X | X |
| 1 | X | X | X | . | . |
| 2 | X | X | X | X | X |

4

| | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 | X | X | . | X | X |
| 1 | X | X | • | . | . |
| 2 | X | X | X | X | X |

A variation

Original Recursive Backtracking:

- Check your base case
- For each move:
 - Copy the world
 - Modify the copy
 - Recurse
 - See what happened

New Recursive Backtracking:

- Check your base case
- For each move:
 - Modify the world
 - Recurse
 - See what happened
 - If you didn't win, *undo the modification!*

I always forget to do this part.

What if you don't backtrack?

| | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 | X | . | . | X | X |
| 1 | . | . | . | X | . |
| 2 | . | X | X | X | . |
| 3 | . | X | . | . | . |
| 4 | . | X | X | X | X |
| 5 | . | . | . | . | . |

Remind you of an APT? This should remind you of an APT...

What if you don't backtrack?

| | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 | X | . | . | X | X |
| 1 | . | . | . | X | . |
| 2 | . | X | X | X | . |
| 3 | . | X | . | . | . |
| 4 | . | X | X | X | X |
| 5 | . | . | . | . | . |

Replace every '.' on the board with a number. Every 1 should only be adjacent to other 1s, each 2 only adjacent to other 2s, and so on.

Remind you of an APT? This should remind you of an APT...

What if you don't backtrack?

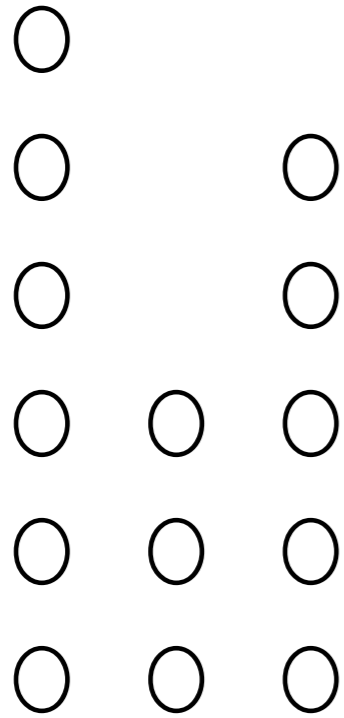
| | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 | X | 1 | 1 | X | X |
| 1 | 1 | 1 | 1 | X | 2 |
| 2 | 1 | X | X | X | 2 |
| 3 | 1 | X | 2 | 2 | 2 |
| 4 | 1 | X | X | X | X |
| 5 | 1 | 1 | 1 | 1 | 1 |

Replace every '.' on the board with a number. Every 1 should only be adjacent to other 1s, each 2 only adjacent to other 2s, and so on.

```
public void reachability(char[][] map) {
```

Remind you of an APT? This should remind you of an APT...

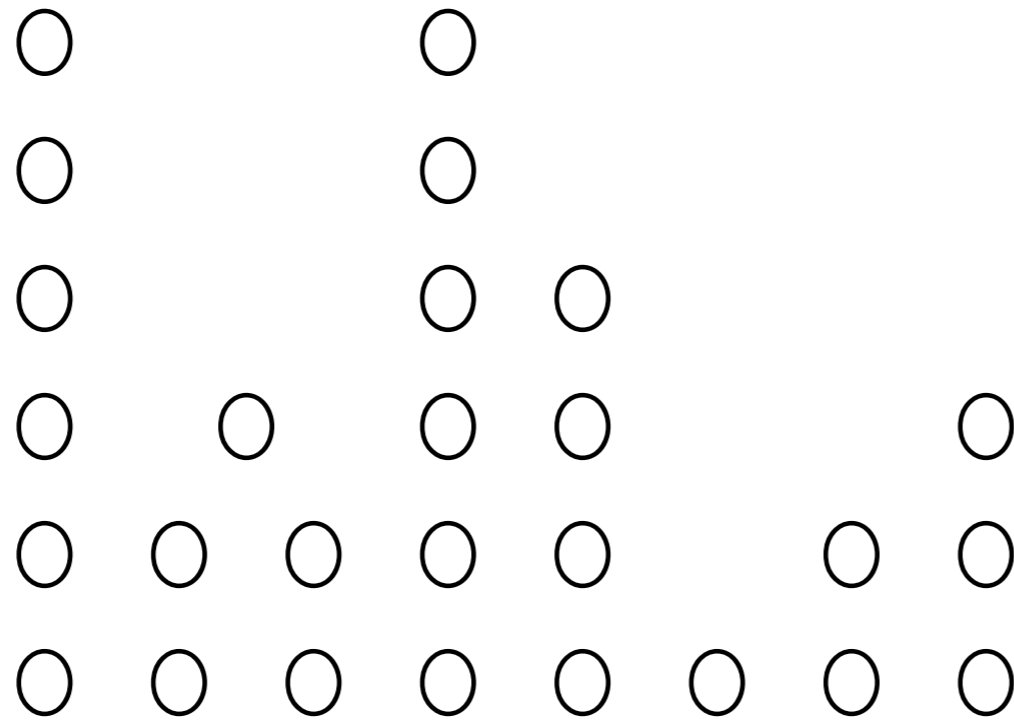
Multi-Heap Nim



```
public void multiHeapNim(ArrayList<Integer> piles) {
```

Remind you of an APT? This should remind you of an APT...

Multi-Heap Nim



```
public void multiHeapNim(ArrayList<Integer> piles) {
```

Remind you of an APT? This should remind you of an APT...

Democracy is a binary tree!

With nine states undecided:

Obama has **431** ways to win **5** ties **Romney has 76** ways to win
84.2% of paths 1% of paths 14.8% of paths

