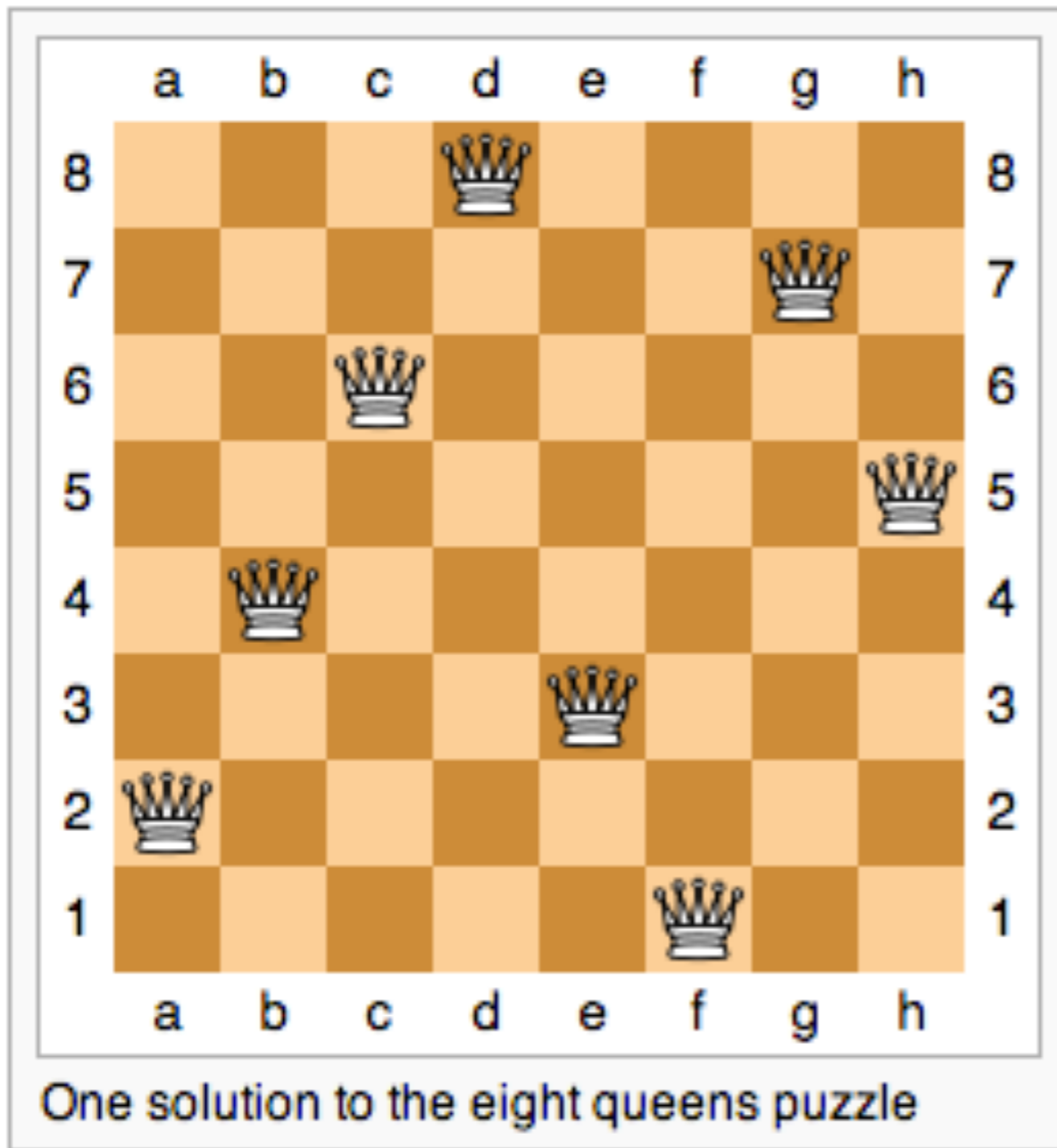


Problems recursion makes easier!

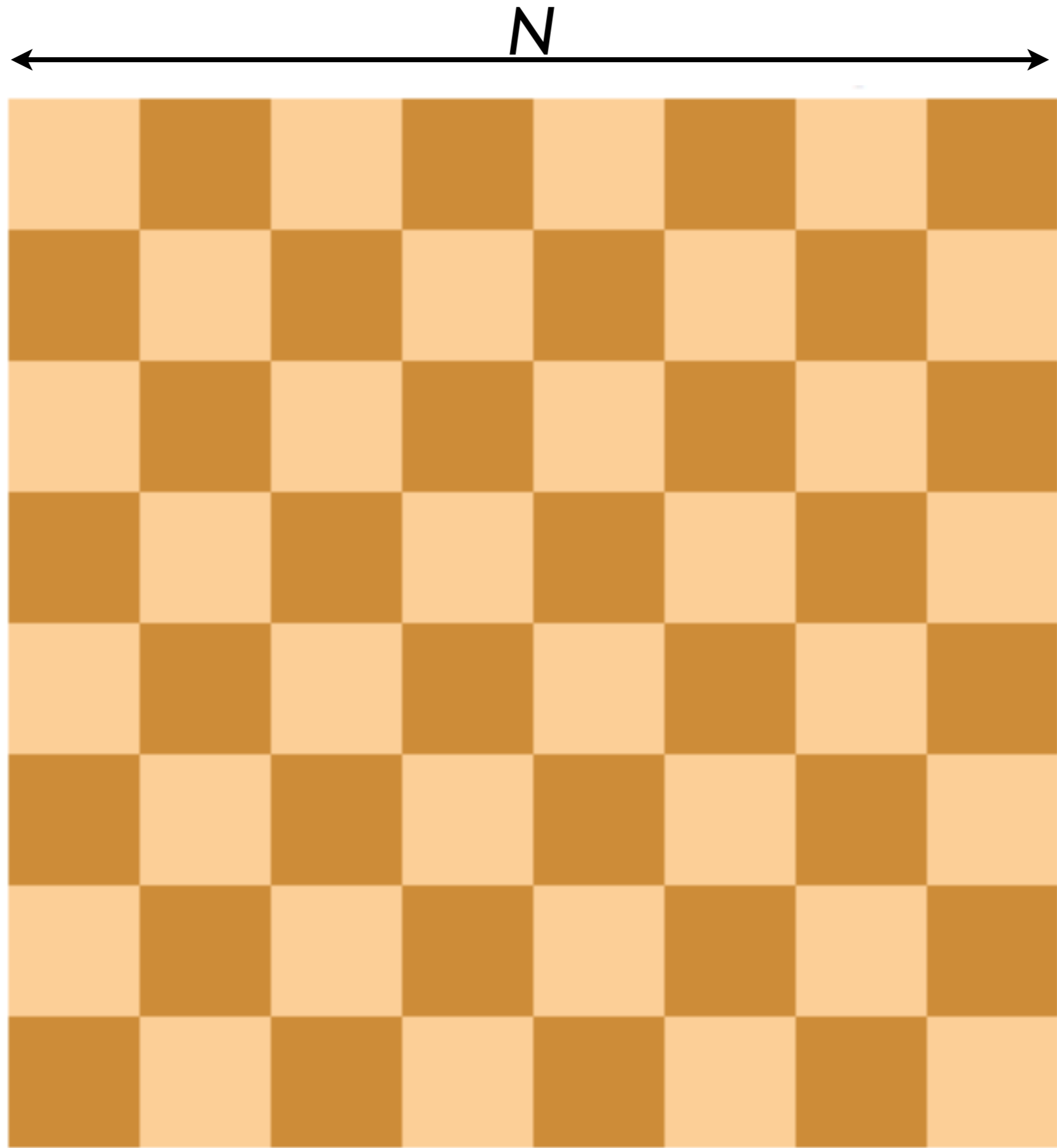
(or possible)



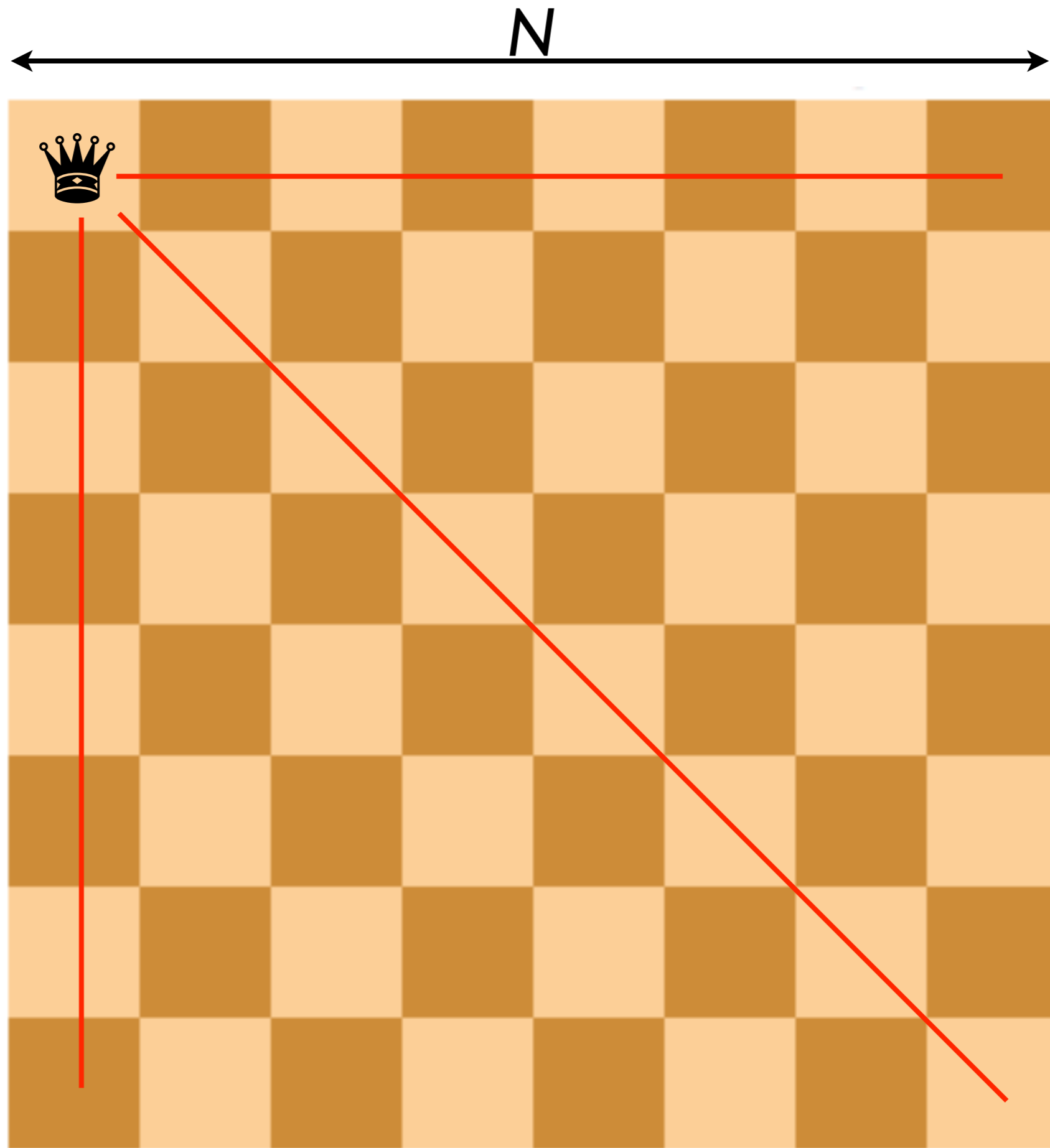
5	3			7				
6			1	9	5			
	9	8					6	
8				6				3
4			8		3			1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9



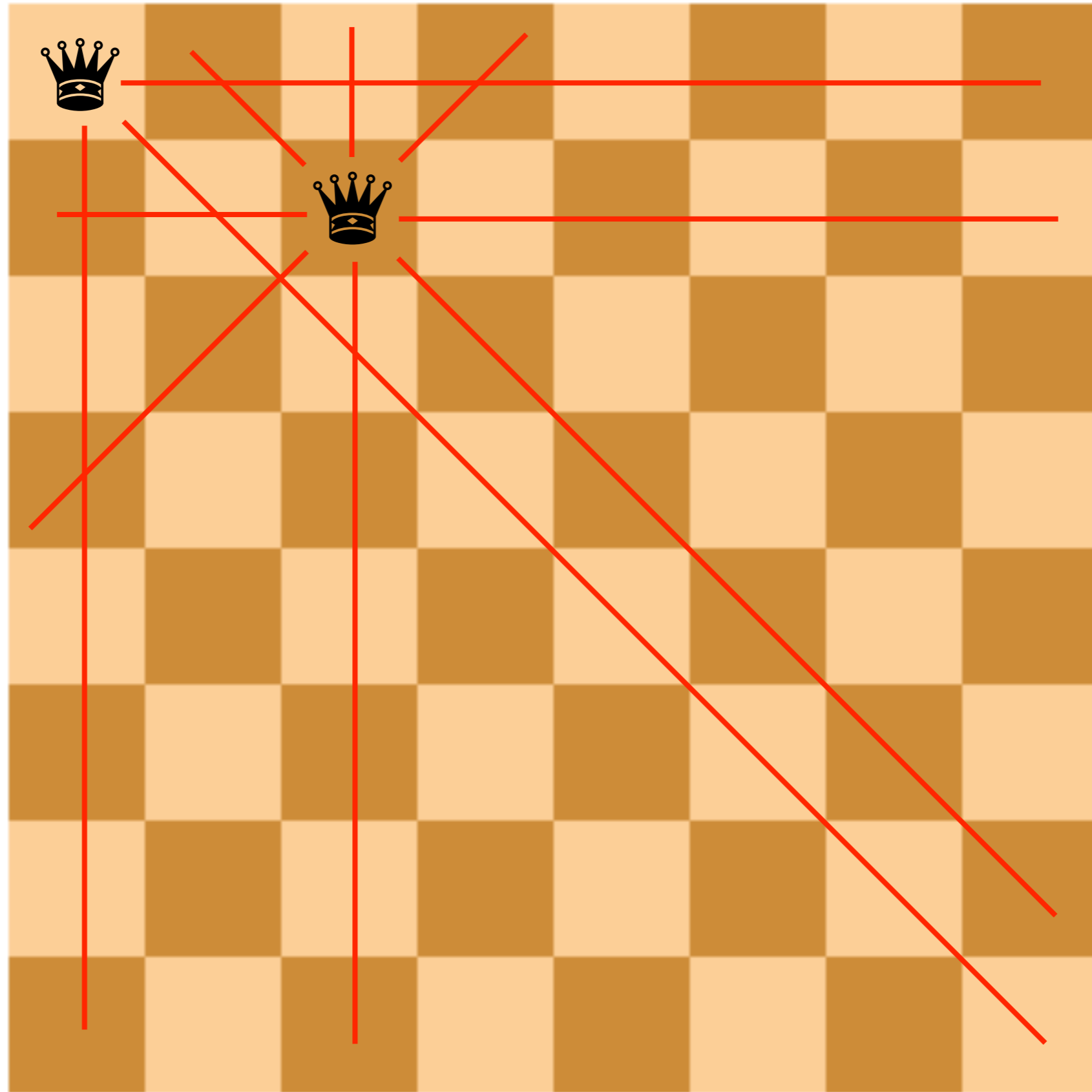
N Queens



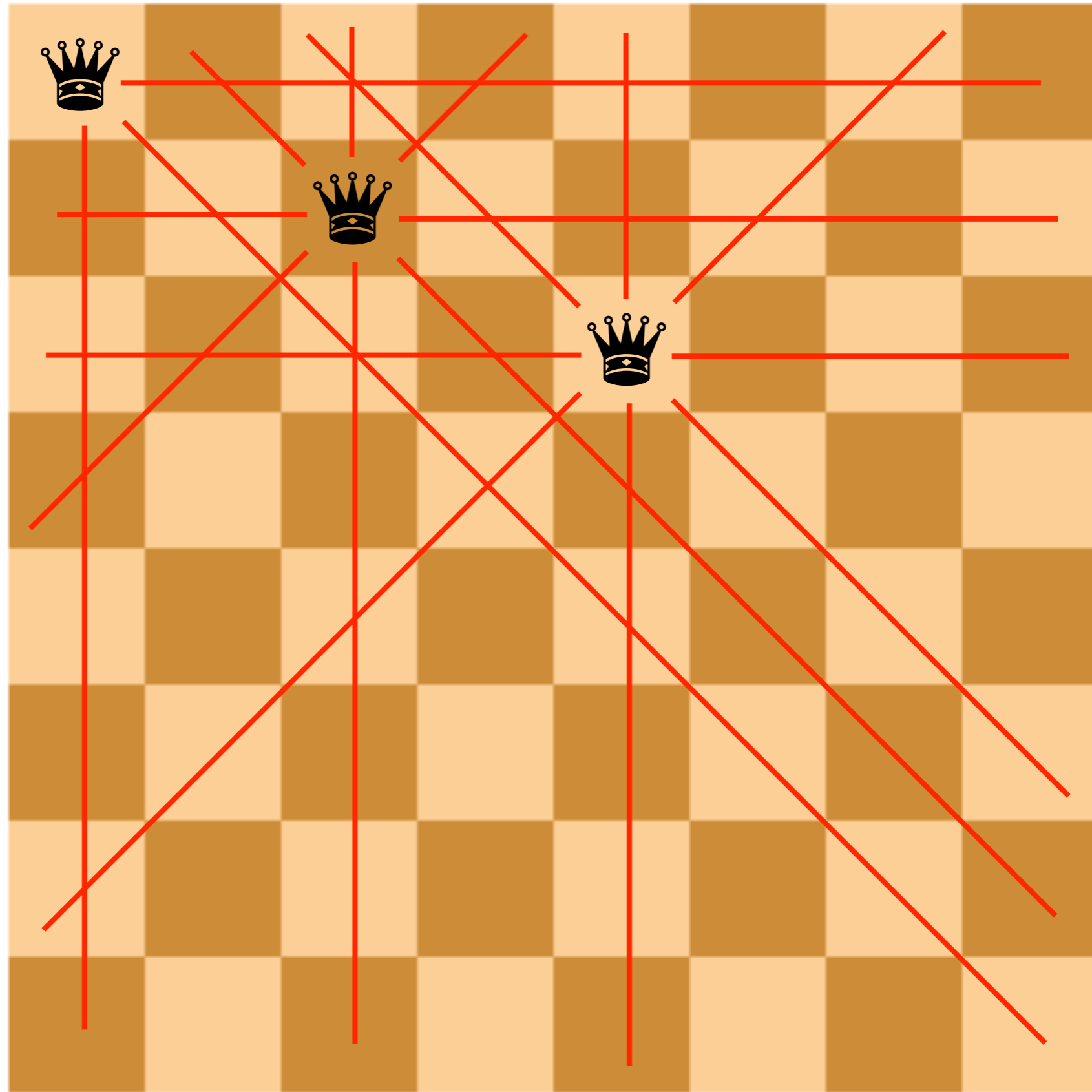
N Queens



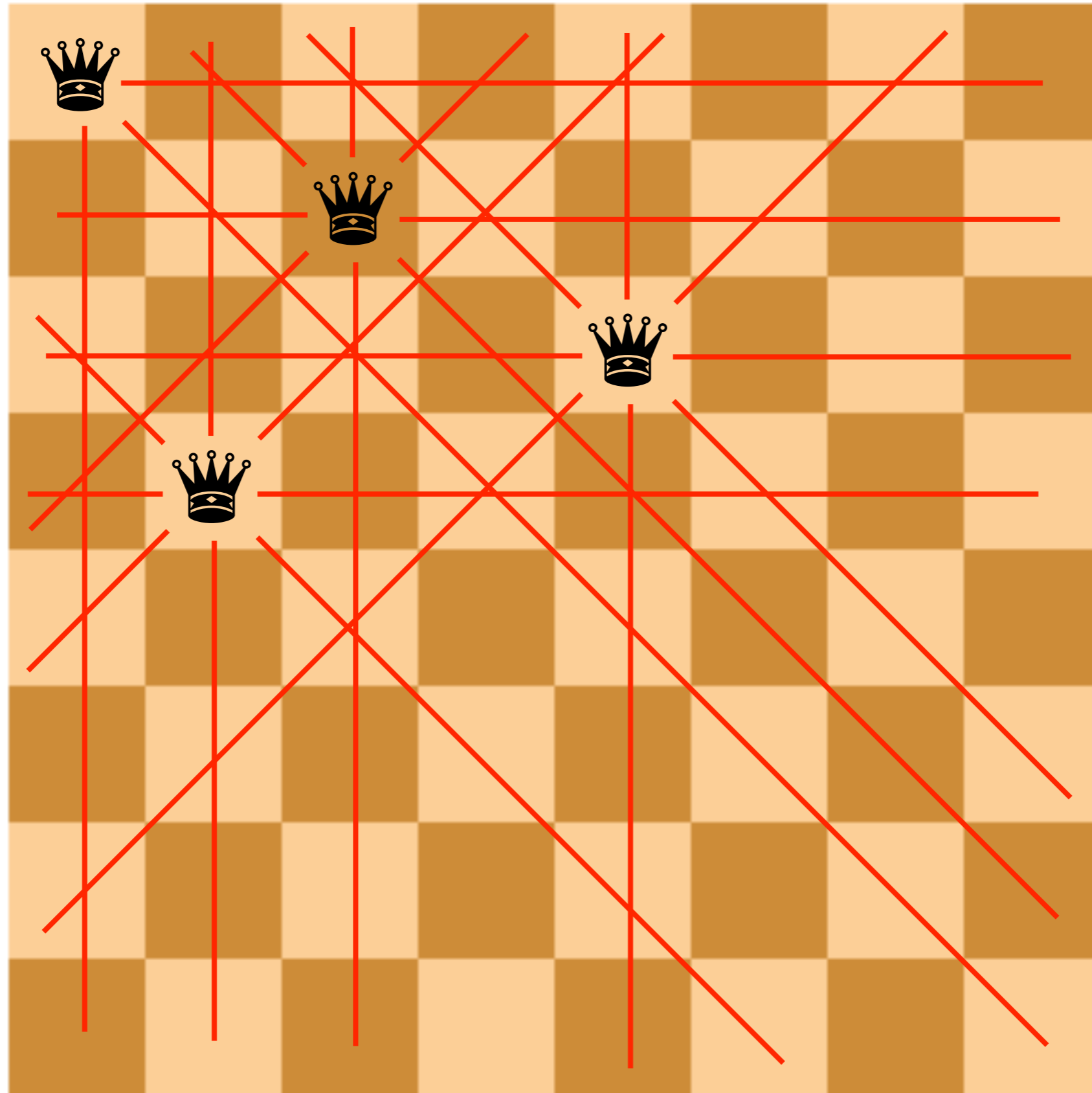
N Queens



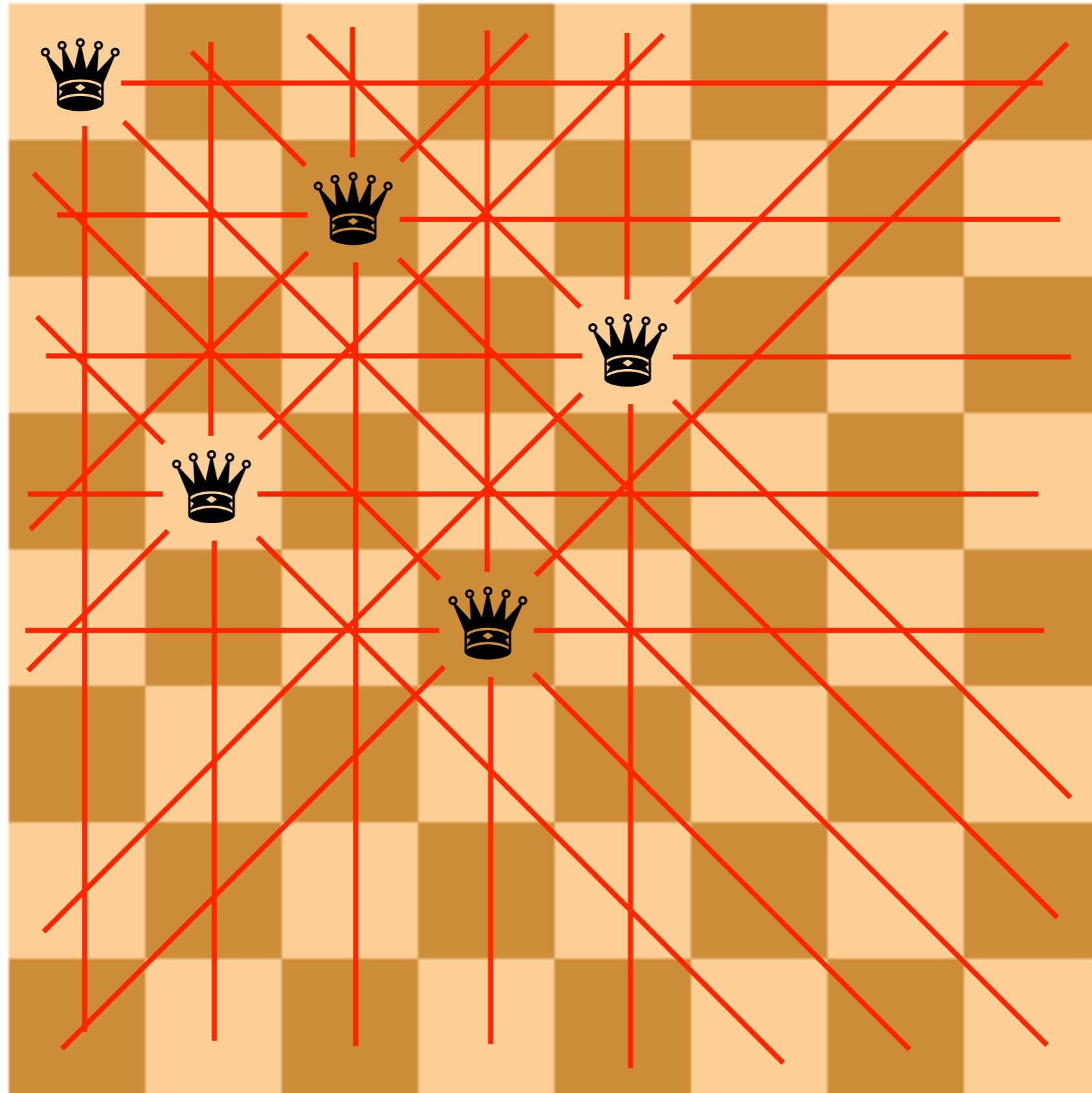
N Queens



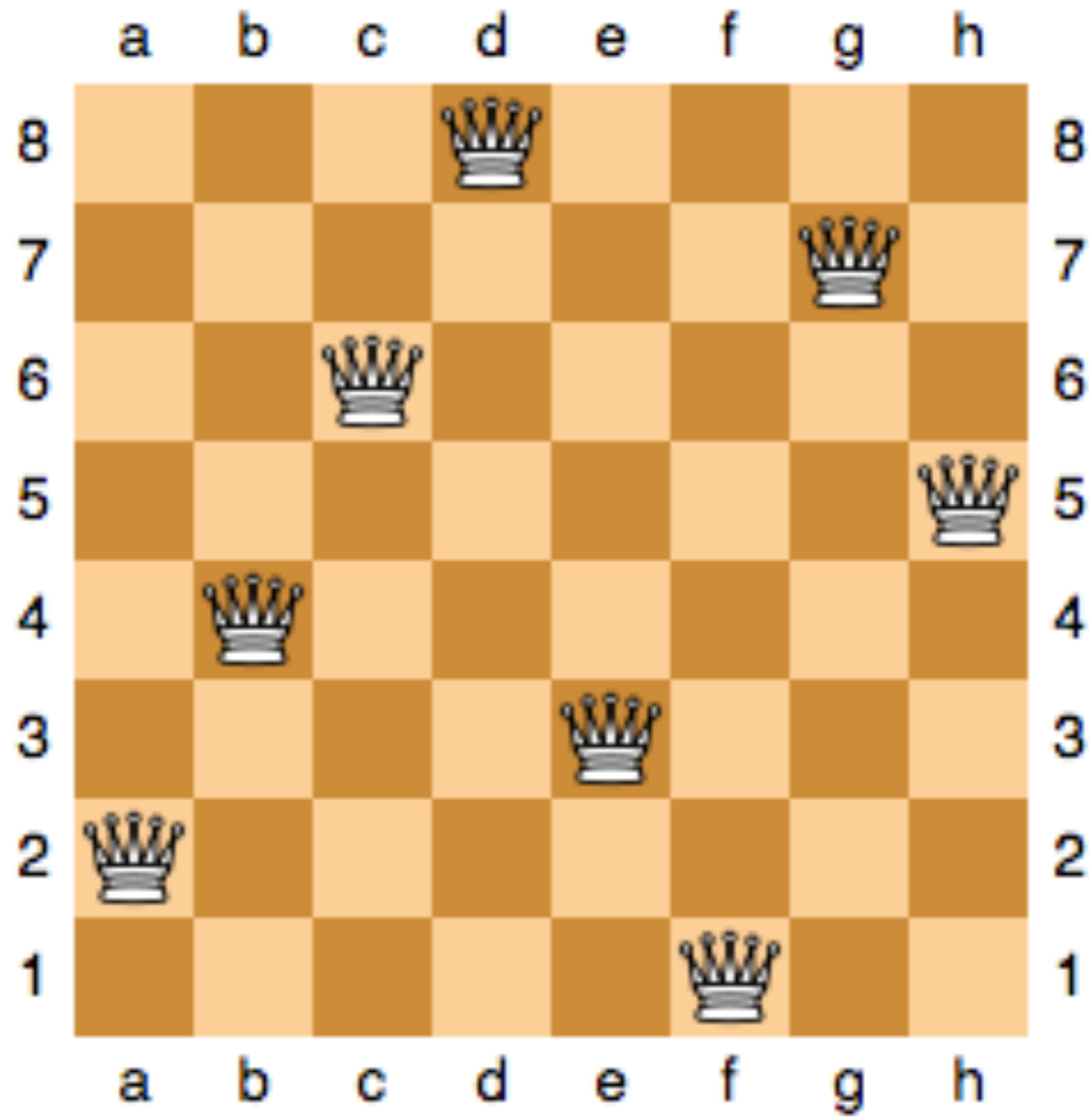
N Queens



N Queens

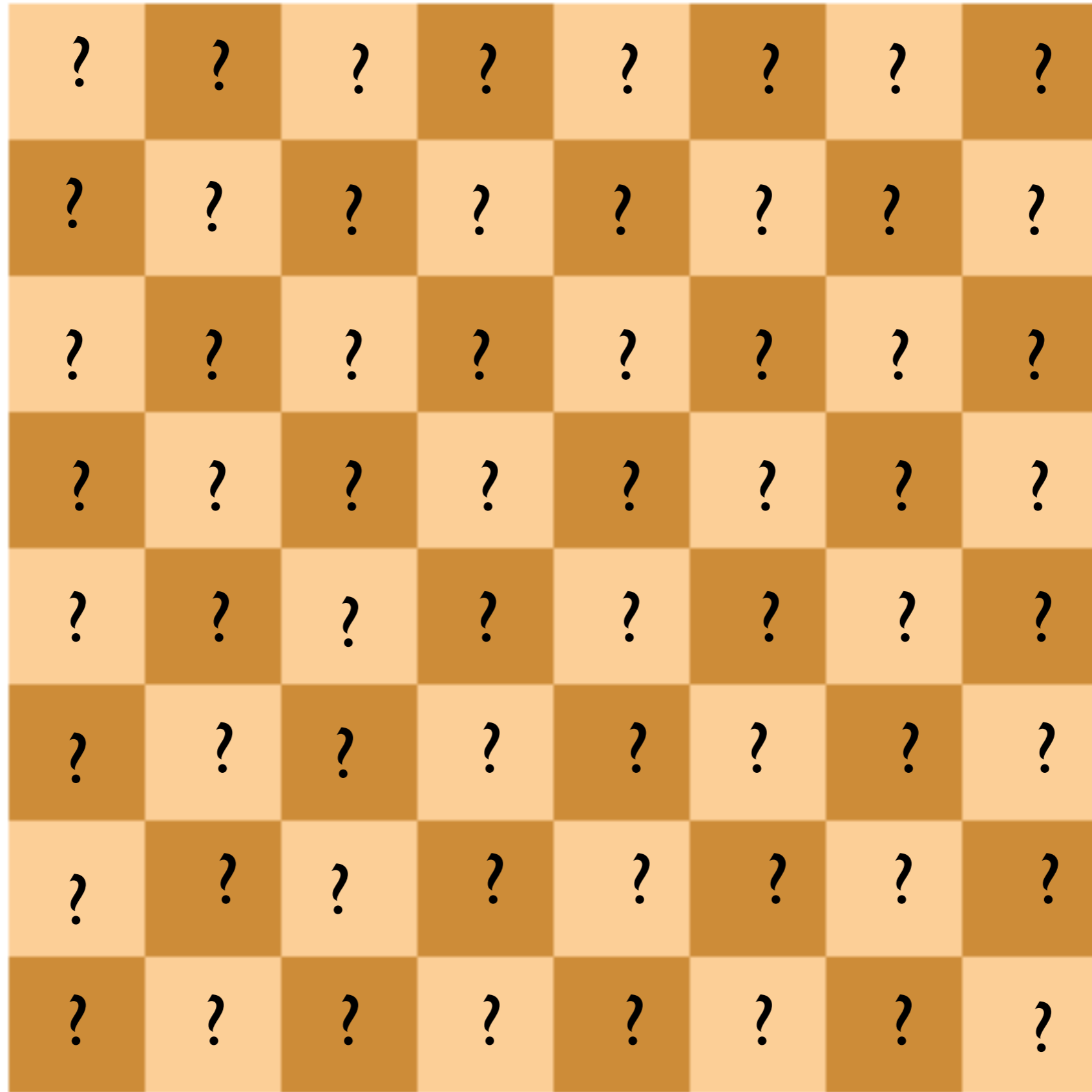


N Queens

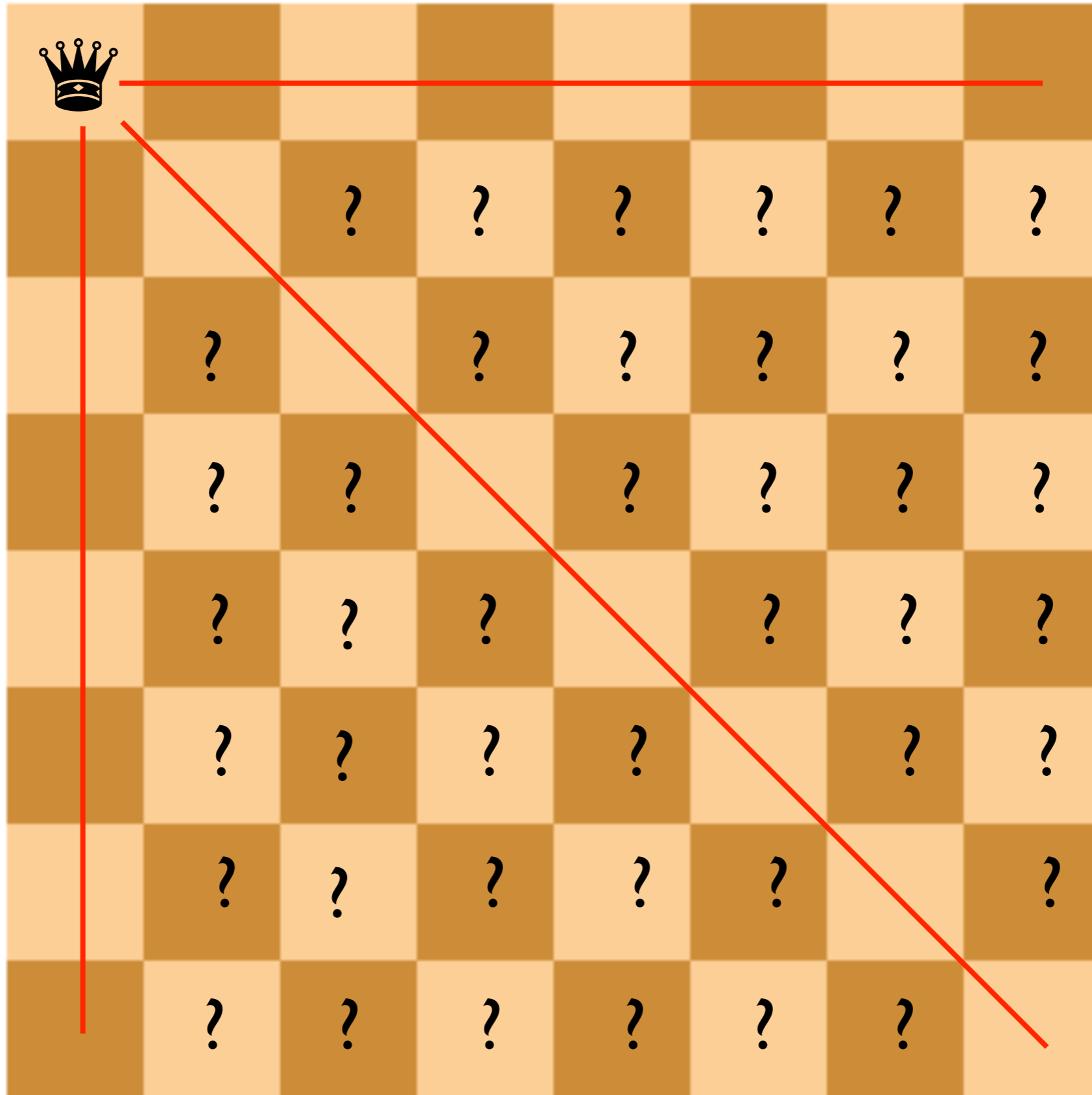


One solution to the eight queens puzzle

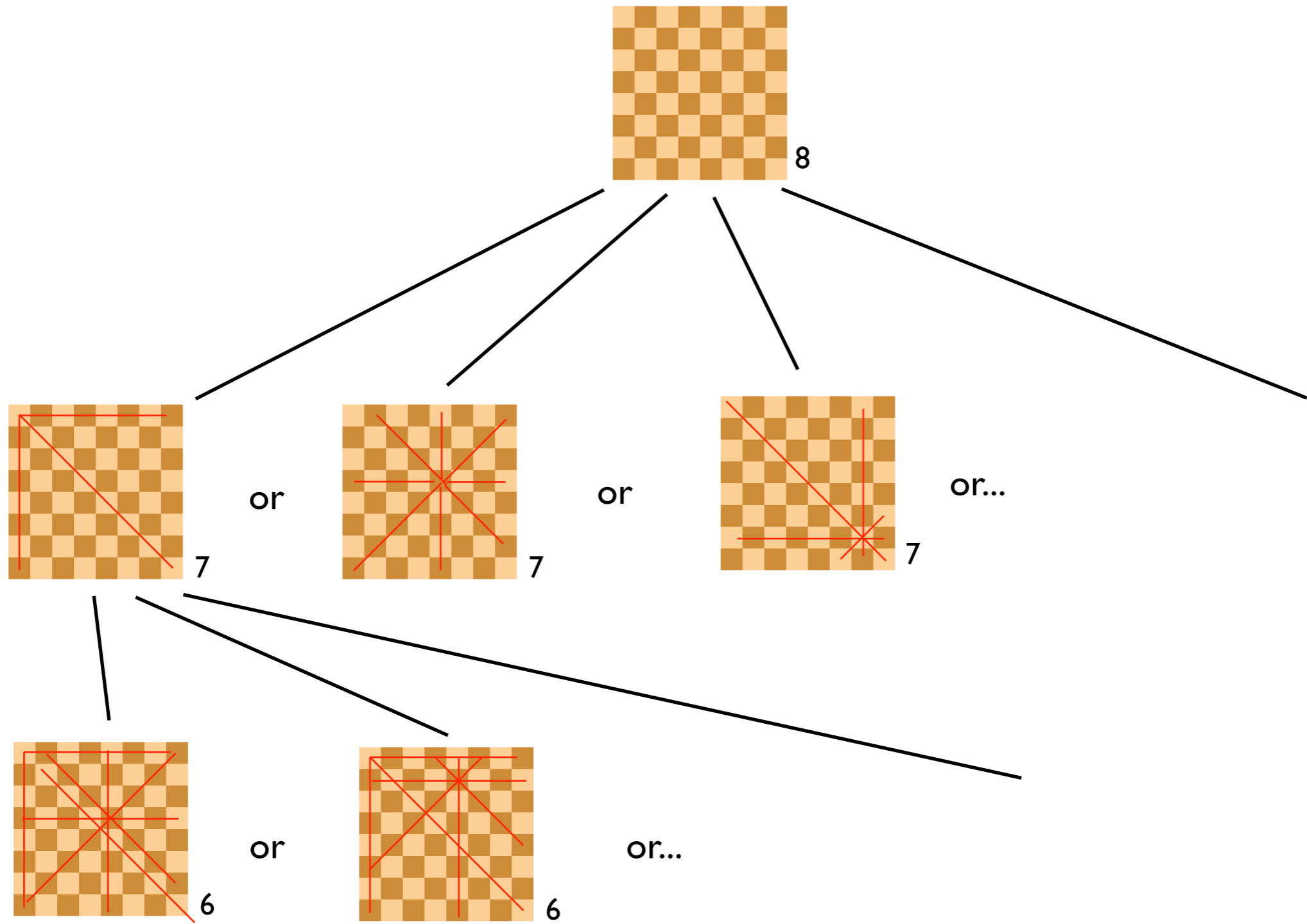
Recursive Backtracking



Recursive Backtracking



Recursive Backtracking



Recursive Backtracking

Base Case?

Remember the human algorithm for writing recursive algorithms!

Recursive Backtracking

Base Case?

Zero Queens

Recursive step?

Recursive Backtracking

Base Case?

Zero Queens

Recursive step?

For every free space:

- *Copy the board & add a queen there*
- *Recurse on $n-1$ queens*
- *If that worked:*
 - *return true*
- *else:*
 - *return false*

Helper Functions

```
public static void main(String[] args) {  
    NQueensBoard b = nQueens(8);  
    if (b != null) {  
        System.out.println(b);  
    } else {  
        System.out.println("No solution!");  
    }  
}
```

Helper Functions

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public static void main(String[] args) {  
    NQueensBoard b = nQueens(8);  
    if (b != null) {  
        System.out.println(b);  
    } else {  
        System.out.println("No solution!");  
    }  
}
```

```
public static NQueensBoard nQueensHelper(NQueensBoard b,  
                                          int n) {  
    // code!  
}
```

Helper functions should take everything you could possibly need as arguments.

Helper Functions

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public static void main(String[] args) {  
    NQueensBoard b = nQueens(8);  
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```

```
public static NQueensBoard nQueensHelper(NQueensBoard b,  
                                         int n) {  
    // code!  
}
```

Helper functions should take everything you could possibly need as arguments.

```
public static NQueensBoard nQueens(int n) {  
    NQueensBoard b = new NQueensBoard(n);  
    return nQueensHelper(b, n);  
}
```

SpreadingNews

Is hard!

Here's a hint.

Suppose you know how long all of your subordinates take to do their work. You will always call the slowest person first, the second-slowest person second, and so on.

See also: `Collections.sort` & `Collections.reverse`.

RatRoute

Base Case?

•	R	•	•	•
•	•	X	•	•
•	•	•	•	X
X	•	X	•	X
•	•	•	C	•

RatRoute

Base Case?

```
  . R . . .  
  . . X . .  
  . . . . X  
 X . X . X  
  . . . C .
```

Recursive step?