



*(It's an 'O')*



# A Digression



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if (false); {  
    System.out.println("THIS IS IMPOSSIBLE");  
}
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```
THIS IS IMPOSSIBLE  
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```

(etc.)



# A Digression

**ARGH**



```
if (false); {  
    System.out.println("THIS IS IMPOSSIBLE");  
}
```

```
THIS IS IMPOSSIBLE  
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```

(etc.)



# News!

Jotto extended until Wednesday



# What's wrong with milliseconds?







# Lessons from last time

Count *operations*, not ms

*How it scales* is the important thing



# Lessons from last time

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*How it scales* is the important thing

```
public void easyThing(String[] strings) {  
    System.out.println("Hello!");  
}
```

Of length N



# Lessons from last time

Count *operations*, not ms

*How it scales* is the important thing

```
public void easyThing(String[] strings) {  
    System.out.println("Hello!");  
}
```

Of length N

```
public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
    }  
}
```



# Lessons from last time

```
public void easyThing(String[] strings) {  
    System.out.println("Hello!");  
}
```

Suppose printing a string  
takes a constant  $C$  units of  
computation.

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public void harderThing(String[] strings) {  
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Suppose printing a string  
takes a constant  $C$  units of  
computation.

```
public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
    }  
}
```

```
public void harderThing2(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = 0 ; j < strings.length ; ++j) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```

*What's the cost of each method?*



# Constants

Many things take *constant time*:

- Any (single) operation on a primitive (+, -, =, etc.)
- Method calls
- Subscripting (i.e. foo[5])
- Conditionals
- Declaring Variables
- Pointer assignment

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public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
    }  
}
```

Of length N

Treat printing like it costs C, as well.



# Constants

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public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
    }  
}
```

Of length N

Treat printing like it costs C, as well.

1 variable declaration. 1 integer assignment.  $N+1$  integer comparisons.  $N$  integer increments.  $N$  method calls.  $N$  subscripts.



# Constants

```
public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
    }  
}
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I variable declaration. I integer assignment. N+I integer comparisons. N integer increments. N method calls. N subscripts.





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$$c_1 + c_2 + (n + 1)c_3 + nc_4 + nc_5 + nc_6$$



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$$c + nc$$



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$$c_1 + c_2 + (n + 1)c_3 + nc_4 + nc_5 + nc_6$$

$$c + nc$$

$$nc$$

$$O(N)$$



# An example

Calculate the running time of this method as a function of  $N$ .

```
public void trickyThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = i+1 ; j < strings.length ; ++j) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```



# An example

```
public void trickyThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = i+1 ; j < strings.length ; ++j) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```

$O(N)$



# An example

```
public void trickyThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = i+1 ; j < strings.length ; ++j) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```

$O(N)$

$O(N^2)$

**Notational note: constants are  $O(1)$**



# What about...

SandwichBar



IsoMorphicWords

BasketWithApples

commonCount  
(from Jotto)

My  
CirclesCountry  
Solution  
(on the calendar page)



# A hard one

```
public void trickyThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = 0 ; j < strings.length ; j *= 2) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```

