

(It's an 'O')



Duke Computer Science

A Digression



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```
if (false); {  
    System.out.println("THIS IS IMPOSSIBLE");  
}
```



A Digression

```
if (false); {  
    System.out.println("THIS IS IMPOSSIBLE");  
}
```

THIS IS IMPOSSIBLE
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(etc.)



ARGH

```
if (false); {  
    System.out.println("THIS IS IMPOSSIBLE");  
}
```

THIS IS IMPOSSIBLE
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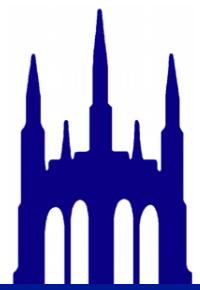
(etc.)

A Digression

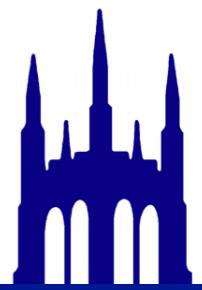


News!

Jotto extended until Wednesday

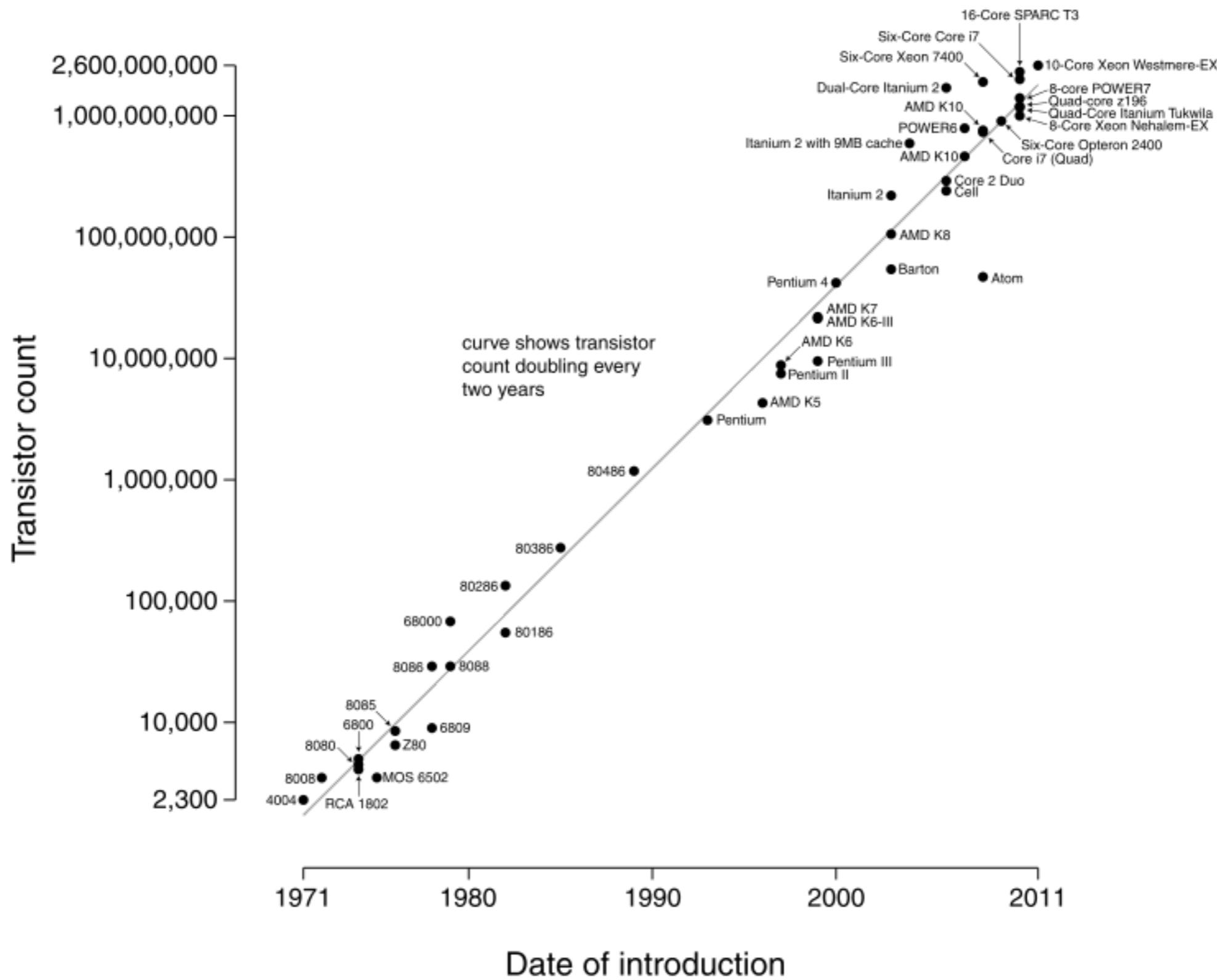


What's wrong with milliseconds?



What's wrong with milliseconds?

Microprocessor Transistor Counts 1971-2011 & Moore's Law



"Wait 18 months" is a terrible meta-algorithm for faster code!

Lessons from last time

Count *operations*, not ms

How it scales is the important thing



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How it scales is the important thing

```
public void easyThing(String[] strings) {  
    System.out.println("Hello!");  
}
```

Of length N



Lessons from last time

Count *operations*, not ms

How it scales is the important thing

```
public void easyThing(String[] strings) {  
    System.out.println("Hello!");  
}
```

Of length N

```
public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
    }  
}
```



Lessons from last time

```
public void easyThing(String[] strings) {  
    System.out.println("Hello!");  
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```

Suppose printing a string takes a constant C units of computation.

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public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
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Lessons from last time

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public void easyThing(String[] strings) {  
    System.out.println("Hello!");  
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```

Suppose printing a string takes a constant C units of computation.

```
public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
    }  
}
```

```
public void harderThing2(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = 0 ; j < strings.length ; ++j) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```

What's the cost of each method?



Constants

Many things take *constant time*:

- Any (single) operation on a primitive (+, -, =, etc.)
- Method calls
- Subscripting (i.e. `foo[5]`)
- Conditionals
- Declaring Variables
- Pointer assignment

```
public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
    }  
}
```

Of length N

Treat printing like it
costs C , as well.



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Of length N

Treat printing like it
costs C , as well.

I variable declaration. I integer assignment. $N+1$ integer comparisons. N integer increments. N method calls. N subscripts.



Constants

```
public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        System.out.println(strings[i]);  
    }  
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I variable declaration. I integer assignment. N+I integer comparisons. N integer increments. N method calls. N subscripts.



Constants

```
public void harderThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
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1 variable declaration. 1 integer assignment. N+1 integer comparisons. N integer increments. N method calls. N subscripts.

$$c_1 + c_2 + (n + 1)c_3 + nc_4 + nc_5 + nc_6$$



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$$c + nc$$

$$\begin{matrix} nc \\ O(N) \end{matrix}$$



An example

Calculate the running time of this method as a function of N .

```
public void trickyThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = i+1 ; j < strings.length ; ++j) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```



An example

```
public void trickyThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = i+1 ; j < strings.length ; ++j) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```

 $O(N)$ 

An example

```
public void trickyThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = i+1 ; j < strings.length ; ++j) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```

$O(N)$

$O(N^2)$

Notational note: constants are $O(1)$



What about...

SandwichBar



IsoMorphicWords

BasketWithApples

commonCount
(from Jotto)

My
CirclesCountry
Solution
(on the calendar page)



A hard one

```
public void trickyThing(String[] strings) {  
    for (int i = 0; i < strings.length; ++i) {  
        for (int j = 0 ; j < strings.length ; j *= 2) {  
            System.out.println(strings[j]);  
        }  
    }  
}
```

