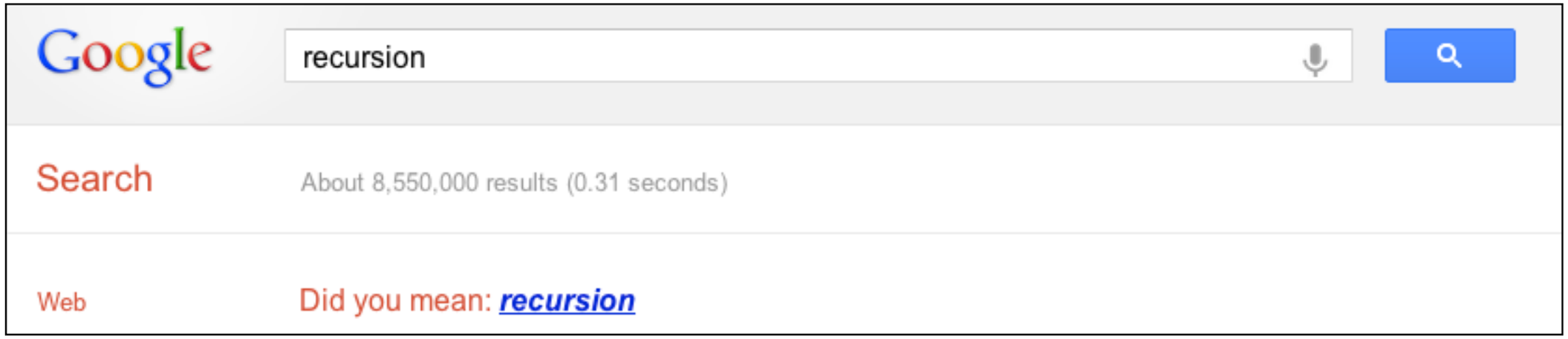
Recursion



(Why yes, I suppose I did.)

Last couple of days: *abstract*.

Today: code with code sauce.

A method defined...

```
long secret1(long i) {
  if (i == 1) {
    return 1;
  }

  long c = secret1(i-1);
  return i * c;
}
```

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Wait a minute...

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$$N! =$$

...in terms of itself.

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$$N! = N \cdot \underline{(N-1)!}$$

Not so new after all.

...in terms of itself.

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$$1! = 1$$

$$N! = N \cdot \underbrace{(N-1)!}_{\text{Not so new after all.}}$$

...in terms of itself.

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```

$$1! = 1$$

$$N! = N \cdot (N-1)!$$

Another one

```
long secret2(long i, long j) {
  if (j == 0) {
    return 1;
  }
  return i * secret2(i, j-1);
}
```

Another one

```
long secret2(int i, long j) {
  if (j == 0) {
    return 1;
  }
  return i * secret2(i, j-1);
}
```

$$m^0 = 1$$

$$m^n = m \cdot \left(m^{n-1}\right)$$

Another one

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long secret2(int i, long j) {
  if (j == 0) {
    return 1;
  }
  return i * secret2(i, j-1);
}
```

$$m^0 = 1$$

$$m^n = m \cdot \left(m^{n-1}\right)$$

Yet Another one

```
long secret3(int i, int[] values) {
  if (i == values.length) {
    return 0;
  }
  return values[i] + secret3(i+1, values);
}
```

A pattern emerges

```
long secret1(long i) {
    if (i == 1) {
        return 1;
    }

    long c = secret1(i-1);
    return i * c;
}
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long secret2(long i, long j) {
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```

if *some stopping condition*
  return a value
store the result of a *recursive call*
compute the answer using that value
return the answer

Terminology

```
long secret1(long i) {
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Base Case

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Recursive Step

Terminology

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```

Base Case

Recursive Step

if *some stopping condition*
  return a value
store the result of a *recursive call*
compute the answer using that value
return the answer

1. Figure out how your problem gets smaller

An integer gets smaller
or
You move one step further through an array
or
You move one step along a list.

Mac's Patented Human Algorithm for Writing Recursive Algorithms

Terminology

```
long secret1(long i) {
  if (i == 1) {
2.    return 1;
  }

  long c = secret1(i-1);
  return i * c;
}
```

Base Case

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  return a value
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2. What's the smallest that can get?

Often 0, or 1, or an empty list.

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3. That's your base case. *Write it!*

We grade on this. Also, demo coming up!

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Base Case

Recursive Step

if *some stopping condition*
  return a value
store the result of a *recursive call*
compute the answer using that value
return the answer

1. Figure out how your problem gets smaller

2. What's the smallest that can get?

3. That's your base case. *Write it!*

4. Compute the answer to the one-smaller problem.

An integer gets smaller
or
You move one step further through an array
or
You move one step along a list.

Often 0, or 1, or an empty list.

We grade on this. Also, demo coming up!

Recurse!

Mac's Patented Human Algorithm for Writing Recursive Algorithms

Terminology

```
long secret1(long i) {
  if (i == 1) {
2.    return 1;
3. }

  long c = secret1(i-1);    4.
5.  return i * c;
}
```

Base Case

Recursive Step

if *some stopping condition*
  return a value
store the result of a *recursive call*
compute the answer using that value
return the answer

Mac's Patented Human Algorithm for Writing Recursive Algorithms

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An integer gets smaller
or
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2. What's the smallest that can get?

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4. Compute the answer to the one-smaller problem.

Recurse!

5. Compute the answer to the this-sized problem.

Demo time!

countAs

isPalindrome

http://codingbat.com/java/Recursion-1