

CompSci 201, L14: Sorting

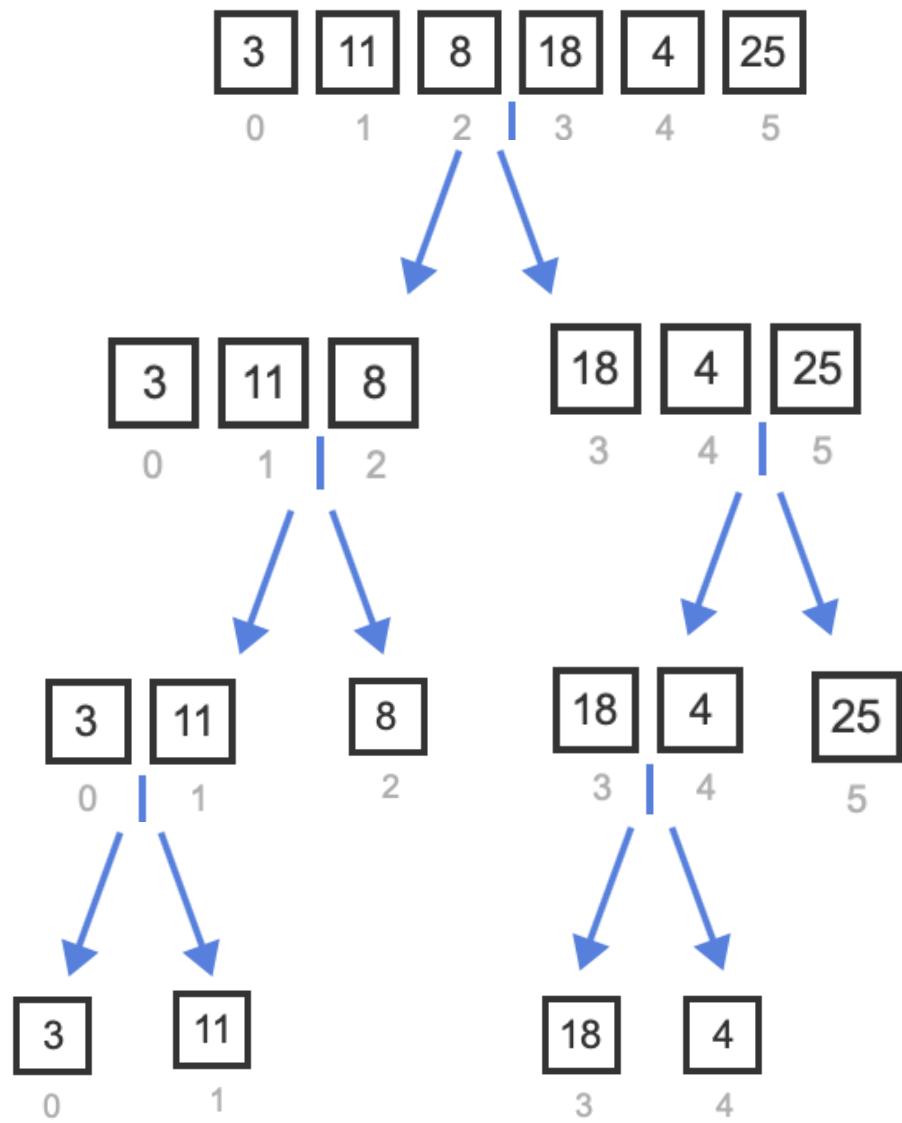
Logistics, Coming up

- Project 3: DNA due today 10/17
- Project 4: Autocomplete will release tomorrow, 10/18, will be due Monday after next 10/31.
- APT Quiz 1 due this Wednesday 10/19
 - Takes 2 hours, finish by 11:59
 - No regular APTs this week, just the quiz

Mergesort

High level idea:

- Base case: size 1
 - Return list
- Recursive case:
 - Mergesort(first half)
 - Mergesort(second half)
 - ...

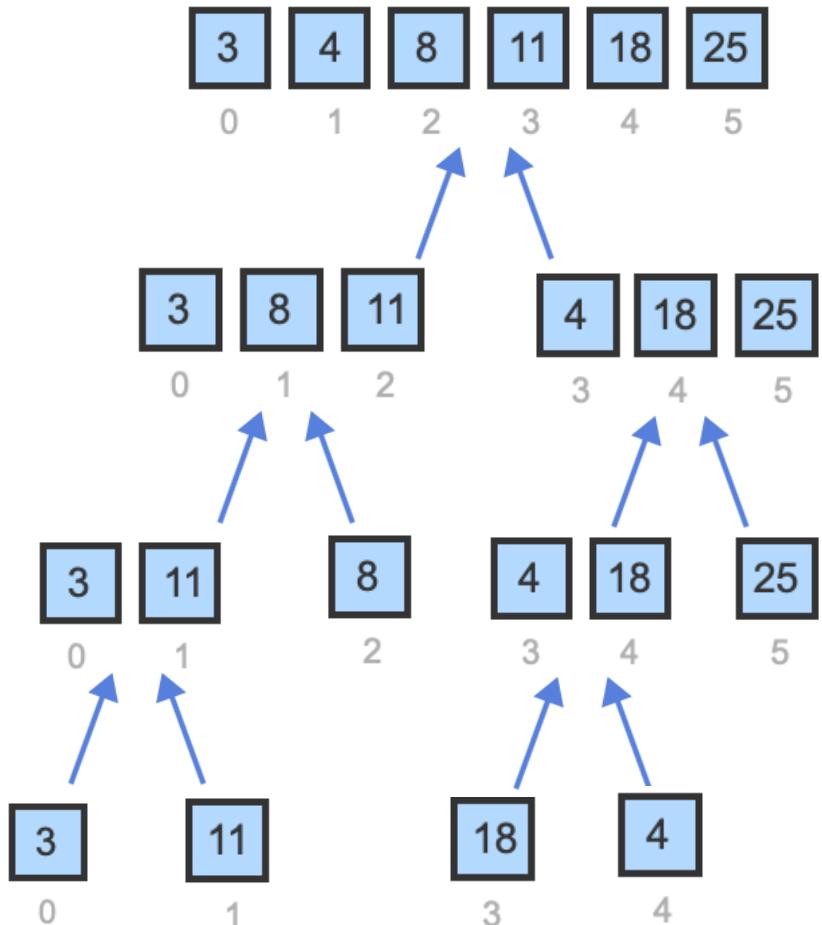


Mergesort

High level idea:

- Base case: size 1
 - Return list
- Recursive case:
 - Mergesort(first half)
 - Mergesort(second half)
 - Merge the sorted halves
 - Return sorted

Helper
method



Runtime complexity of mergesort?

```
19  public static List<String> mergeSortList(List<String> list) {  
20      if (list.size() <= 1) {  
21          return list;  
22      }  
23      int mid = list.size()/2;  
24      List<String> firstHalfSorted = mergeSortList(list.subList(0, mid));  
25      List<String> secondHalfSorted = mergeSortList(list.subList(mid, list.size()));  
26      return merge(firstHalfSorted, secondHalfSorted);  
27  }
```

$T(N) = \dots$

$T(N/2) + \dots$

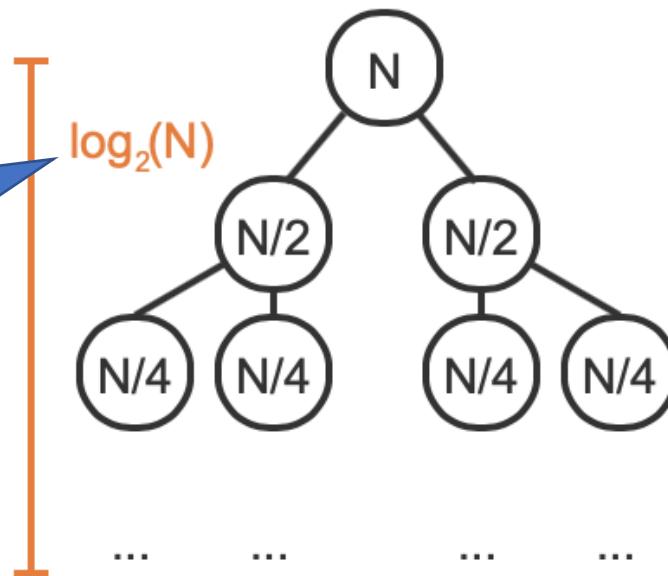
$O(N)$

$T(N/2) + \dots$

Recursion tree

$$T(N) = N + T(N / 2) + T(N / 2)$$

Depth of the recursion tree:
Number of recursive calls before base case.



N

$$(N / 2) * 2 = N$$

$$(N / 4) * 4 = N$$

Total complexity of each level across all of the recursive calls.

$$T(N) = O(N \log N)$$

Sorting in Java: Comparable, Comparator

Java API Sort Algorithms

- `Collections.sort` (for a List)
- `Arrays.sort` (for an Array)
- Both implement *Timsort* a variant of Mergesort.
 - $O(N \log(N))$, *nearly* linear runtime complexity.
 - Sorts in-place, mutates the input rather than return a new List/Array.
 - `Collections.sort(myList);` causes `myList` to be sorted.
 - Stable, does not reorder elements if not needed (e.g., if two elements are equal).

What can be compared and sorted in Java?

- Class objects that implement the Comparable interface. Has a naturalOrder.
- Requires implementing a `.compareTo()` method

Should return an int:

- < 0 if `this` comes before the parameter.
- 0 if `this` and the parameter are equal.
- > 0 if `this` comes after the parameter.

```
private static class Person implements Comparable<Person> {  
    String first;  
    String last;  
    public Person(String s) {...}  
    public String getLast() { return last; }  
    public String getFirst() { return first; }  
    public String toString() { return first + " " + last; }  
    @Override  
    public int compareTo(Person p){  
        int diff = last.compareTo(p.last);  
        if (diff != 0) return diff;  
        return first.compareTo(p.first);  
    }  
}
```

Strings are Comparable

- What is the equivalent of `<` for Strings?
- Use the `compareTo` method for the natural lexicographic (dictionary/sorted) ordering.

```
[jshell> "a".compareTo("b");  
$30 ==> -1
```

Negative for “less than”

```
[jshell> "b".compareTo("b");  
$31 ==> 0
```

Zero for “equal”

```
[jshell> "b".compareTo("a");  
$32 ==> 1
```

Positive for “less than”

```
[jshell> "az".compareTo("cb");  
$37 ==> -2
```

Lexicographic, check first character,
second if equal, third if still equal, ...

Comparable for other classes?

- Can implement Comparable interface and compareTo method when defining your own class.
 - Defines a natural ordering, can sort
 - Collections.sort, Arrays.sort
- What if it's someone else's class and they didn't implement Comparable?
- Or what if you want to sort by something *other* than the “natural order” defined by Comparable?

Comparable vs. Comparator

- `a.compareTo(b)`
 - What is method signature? One parameter
 - Method in class of which object a is an instance
 - a is `this`, b is a parameter
- Create a `Comparator` `c`, use `c.compare(a, b)`
 - Method has two parameters
 - Part of [Comparator](#) (Java API link)
 - Returns an int:
 - < 0 (means a comes before b)
 - == 0 (means a equals b)
 - > 0 (means a comes after b)

java.util.Comparator Examples

- `Comparator.naturalOrder`

```
jshell> Comparator<String> c = Comparator.naturalOrder()  
c ==> INSTANCE
```

```
jshell> c.compare("a", "b")  
$12 ==> -1
```

Must be Comparable

```
jshell> c.reversed().compare("a", "b")  
$13 ==> 1
```

- `Comparator.comparing`

```
jshell> Comparator<String> c = Comparator.comparing(String::length)  
c ==> java.util.Comparator$$Lambda$27/0x0000000800b97c402b71fc7e
```

```
jshell> c.compare("this", "is")  
$15 ==> 1
```

```
jshell> c.compare("is", "it")  
$16 ==> 0
```

Syntax is: <Type>::<method name> to sort something of the Type by the result of some getter method that returns something Comparable.

Sorting Comparable objects by naturalOrder

[**sloth, house, owl, ant, mice, kelp**]

[**ant, house, kelp, mice, owl, sloth**]

- naturalOrder for Strings is lexicographic (alphabetical or dictionary order)

```
String[] a = {"sloth", "house", "owl", "ant", "mice", "kelp"};
System.out.println(Arrays.toString(a));

String[] copy = Arrays.copyOf(a, a.length);
Arrays.sort(copy);
System.out.println(Arrays.toString(copy));
```

Comparator to sorting strings by length

[**sloth**, **house**, **owl**, **ant**, **mice**, **kelp**]

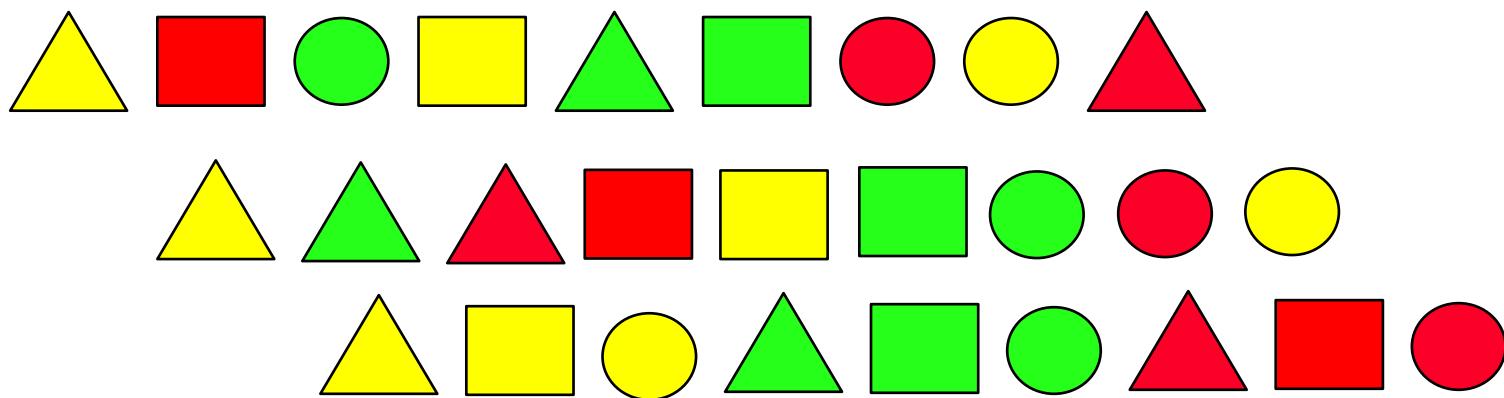
[**owl**, **ant**, **mice**, **kelp**, **sloth**, **house**]

- Why does "owl" come before "ant"?
 - Stable sort respects order of equal keys

```
copy = Arrays.copyOf(a, a.length);
Arrays.sort(copy, Comparator.comparing(String::length));
System.out.println(Arrays.toString(copy));
```

Stable, Stability

- Respect order of equal keys when sorting
 - First sort by shape, then by color: Stable!
 - Triangle < Square < Circle; Yellow < Green < Red



Sorting by length and then naturally

```
[sloth, house, owl, ant, mice, kelp]  
[ant, owl, kelp, mice, house, sloth]
```

- Could put this on one line, easier to read?
 - First sort by length, if same? naturally

```
Arrays.sort(copy, Comparator.
```

```
    comparing(String::length).
```

```
    thenComparing(Comparator.naturalOrder()));
```

Comparator with “lambdas”

- What if you want to sort by something that doesn’t have a getter method?
- Or you just want to do something different than sort by a getter method?
- Can also define a comparator with a “lambda” expression.
- Example: Sort an Array of Arrays

```
int[] ar1 = {2, 0, 1};      int[] ar2 = {1, 0, 2, 3};  
                           int[][] bothAr = {ar1, ar2};
```

Comparator with lambda to sort Array of Arrays by first elements

```
int[] ar1 = {2, 0, 1};      int[] ar2 = {1, 0, 2, 3};  
  
int[][] bothAr = {ar1, ar2};  
  
{ int[3] { 2, 0, 1 }, int[4] { 1, 0, 2, 3 } }
```

```
Comparator<int[]> comp =  
    (a, b) -> (a[0] - b[0]);
```

Type we want
to compare

Given an a
and a b of
that type...

comp.compare(a,b)
should return this
expression

Comparator with lambda to sort Array of Arrays by first elements

```
int[] ar1 = {2, 0, 1};      int[] ar2 = {1, 0, 2, 3};  
  
int[][] bothAr = {ar1, ar2};  
  
{ int[3] { 2, 0, 1 }, int[4] { 1, 0, 2, 3 } }
```

```
Comparator<int[]> comp =  
    (a, b) -> (a[0] - b[0]);
```

comp.compare(ar1, ar2) returns (2-1) = 1.
comp.compare(ar1, ar1) returns (2-2)=0
comp.compare(ar2, ar1) returns (1-2)=-1

Comparator with lambda to sort Array of Arrays by first elements

```
int[] ar1 = {2, 0, 1};      int[] ar2 = {1, 0, 2, 3};  
  
int[][] bothAr = {ar1, ar2};  
{ int[3] { 2, 0, 1 }, int[4] { 1, 0, 2, 3 } }  
  
Comparator<int[]> comp =  
    (a, b) -> (a[0] - b[0]);  
  
Arrays.sort(bothAr, comp);  
{ int[4] { 1, 0, 2, 3 }, int[3] { 2, 0, 1 } }
```

WOTO

Go to duke.is/pr6v

Not graded for correctness,
just participation.

Try to answer *without* looking
back at slides and notes.

But do talk to your neighbors!



Summary: Sorting Blobs

```
1  public class Blob implements Comparable{  
2      public String name;  
3      public String shape;  
4      public String color;  
5  
6      public Blob(String n, String c, String s) {  
7          name = n;  
8          shape = s;  
9          color = c;  
10     }  
11  
12     public String getShape() {  
13         return shape;  
14     }  
15  
16     @Override  
17     public int compareTo(Object o) {  
18         Blob other = (Blob) o;  
19         return name.compareTo(other.name);  
20     }  
}
```

Getter method for shape,
can use with Comparator

compareTo / natural order
based on name

Sorting Blobs many ways

```
List<Blob> myBlobs = ...
```

```
16 // Sorting by natural order (names)  
17 Collections.sort(myBlobs);  
18 System.out.println(myBlobs);  
--
```

```
[(al, round, red), (bo, square, blue), (cj, triangle, green), (di, square, red)]
```

```
20 // Sorting by shape with Comparator using getShape method  
21 Comparator<Blob> comp = Comparator.comparing(Blob::getShape);  
22 Collections.sort(myBlobs, comp);  
23 System.out.println(myBlobs);
```

```
[(al, round, red), (bo, square, blue), (di, square, red), (cj, triangle, green)]
```

Sorting Blobs even more ways

```
25 // Sorting by color with Comparator using lambda
26 Comparator<Blob> comp2 = (b1, b2) -> (b1.color.compareTo(b2.color));
27 Collections.sort(myBlobs, comp2);
28 System.out.println(myBlobs);
```

`[(bo, square, blue), (cj, triangle, green),
(al, round, red), (di, square, red)]`

```
30 // Sorting by with multiple comparators
31 Collections.sort(myBlobs, comp.thenComparing(comp2));
32 System.out.println(myBlobs);
```

`[(al, round, red), (bo, square, blue),
(di, square, red), (cj, triangle, green)]`

Algorithms using sortedness

Binary Search

- Given a **sorted** list of N elements and a target, in just $O(\log(N))$ time, return:
 - Index i such that $\text{list.get}(i)$ equals target, or
 - 1 if target not in list
- Example:
 - If we search for 'h', should return 4
 - If we search for 'c', should return -1

value	'a'	'b'	'd'	'g'	'h'	'j'	'k'	'm'	'p'
index	0	1	2	3	4	5	6	7	8

Java API Binary Search

`Arrays.binarySearch` (for arrays) and
`Collections.binarySearch` (for Lists).

```
String[] ar = {"ape", "bird", "cat", "dog", "elephant",  
"ferret", "gecko", "hippo"};
```

```
int index = Arrays.binarySearch(ar, "cat");
```

Returns 2

Careful, does not check for you if list is sorted!

```
String[] ar = {"cat", "ape", "bird", ...
```

```
int index = Arrays.binarySearch(ar, "cat");
```

Returns -4

Java API Binary Search with Comparator

Can pass a comparator `comp`, in which case:

1. Array/List should be sorted by that `comp`, and
2. Want an index i such i 'th element e_i has
`comp.compare(e_i , target)==0.`

Sorted by length

[ape, cat, dog, bird, gecko, hippo, ferret, elephant]

```
Comparator<String> comp =  
    Comparator.comparing(String::length);
```

```
index = Arrays.binarySearch(ar, "dog", comp);
```

Returns 1.
`comp.compare ("cat", "dog")==0`

How is Binary Search $O(\log(N))$?

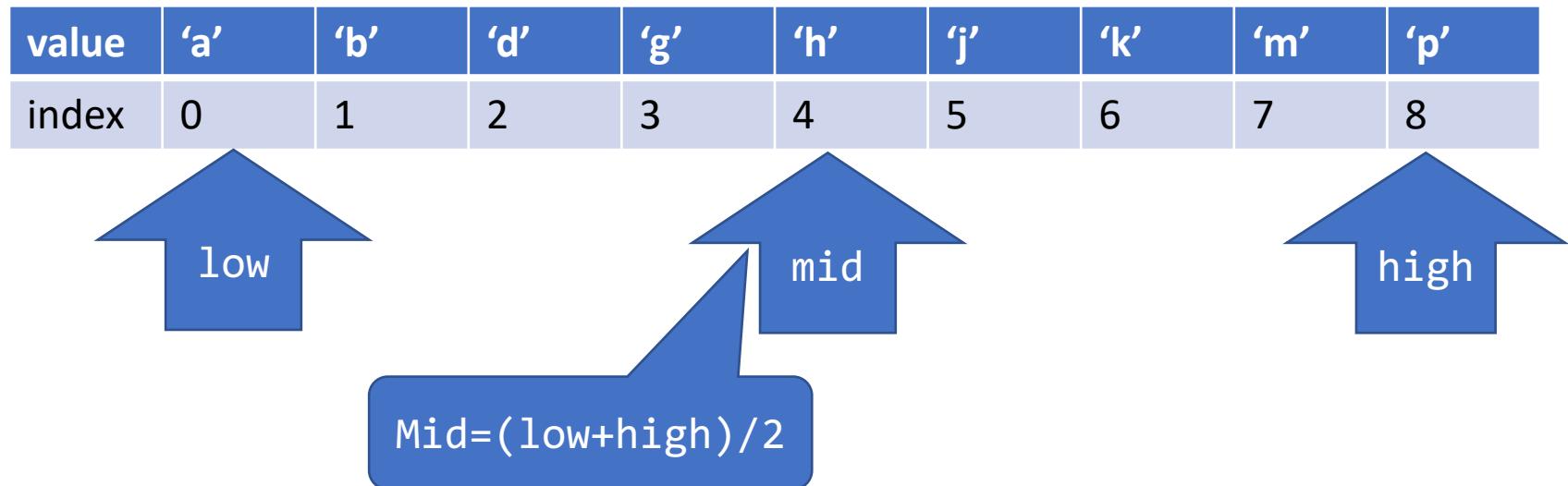
- How to find something in a list of N elements without looping over the list?
- Let `low` (initially 0) and `high` (initially $N-1$) mark the limits of the active search space.
- Want to cut down the search space by half at each step:



value	'a'	'b'	'd'	'g'	'h'	'j'	'k'	'm'	'p'
index	0	1	2	3	4	5	6	7	8

Binary Search in Pictures

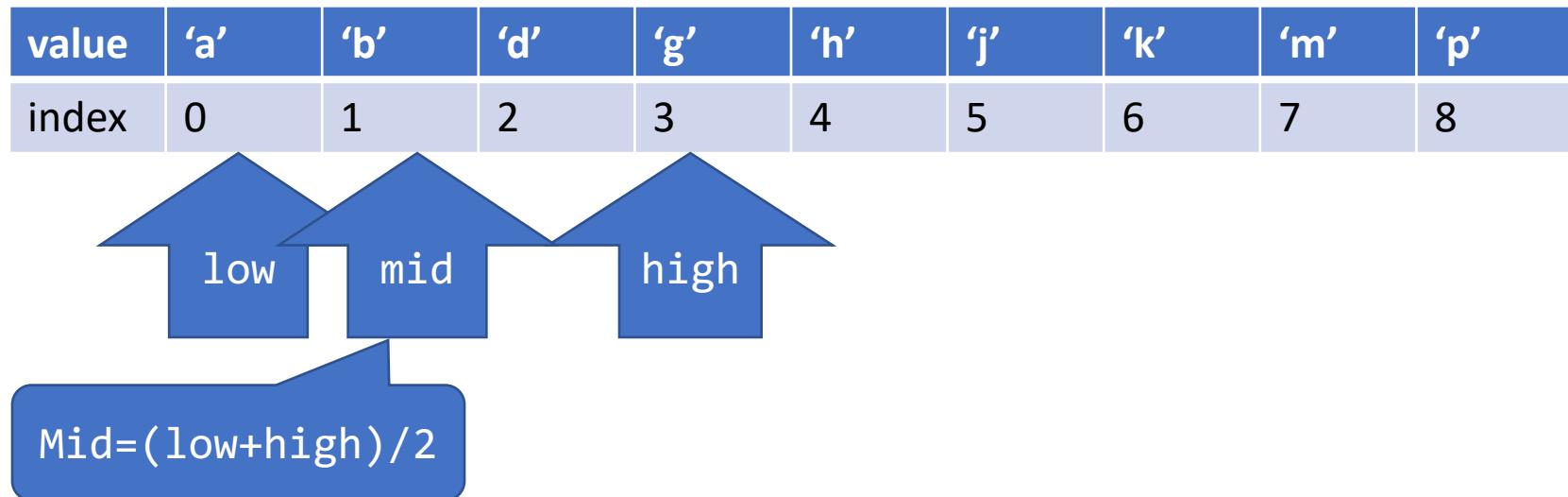
- Searching for 'd' in



- 'h' > 'd', so need to keep searching in the *lower* half.
- Set `high = mid-1;`

Binary Search in Pictures

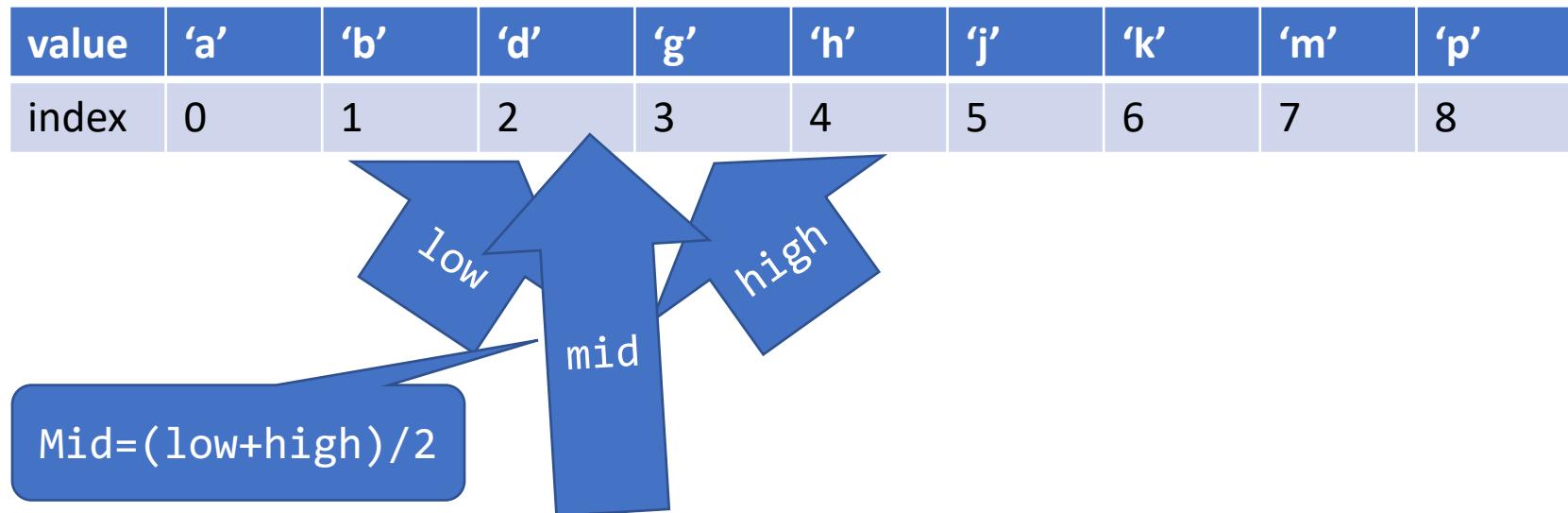
- Searching for 'd' in



- 'b' < 'd', so need to keep searching in the *upper* half.
- Set **low = mid+1;**

Binary Search in Pictures

- Searching for 'd' in



- 'd' equals 'd', return `mid` (2)