CompSci 334 Fall 2024 10/10/24 10/17/24

Section: LR Parsing

LR PARSING

LR(k) Parser

- bottom-up parser
- shift-reduce parser
- L means: reads input left to right
- R means: produces a rightmost derivation
- k number of lookahead symbols
- LR parsing process
 - convert CFG to PDA
 - Use the PDA and lookahead symbols

Convert CFG to PDA

The constructed NPDA:

- three states: s, q, f start in state s, assume z on stack
- all rewrite rules in state s, backwards
 rules pop rhs, then push lhs
 (s,lhs) ∈ δ(s,λ,rhs)
 This is called a reduce operation.
- additional rules in s to recognize terminals

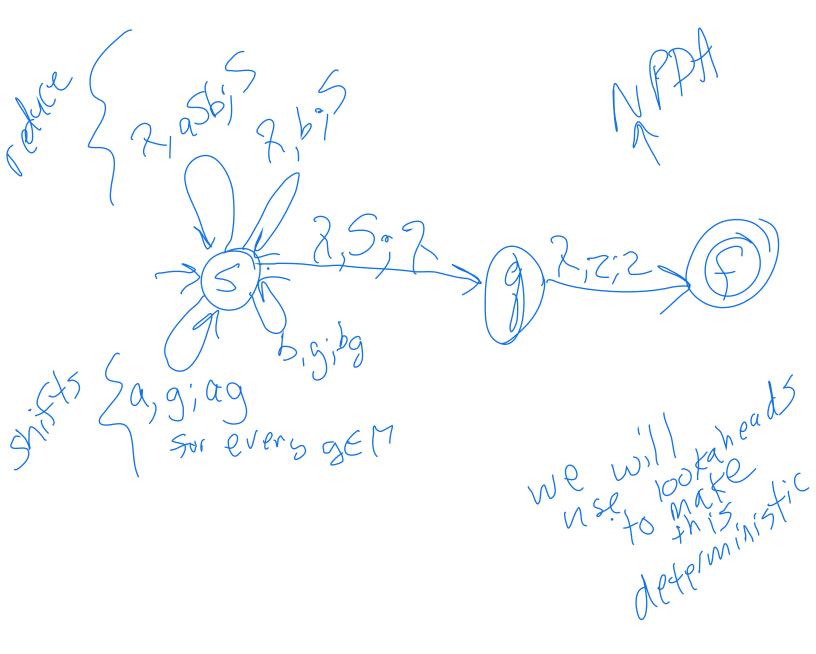
For each $\mathbf{x} \in \Sigma$, $\mathbf{g} \in \Gamma$, $(\mathbf{s}, \mathbf{xg}) \in \delta(\mathbf{s}, \mathbf{x}, \mathbf{g})$

This is called a shift operation.

- pop S from stack and move into state q
- pop z from stack, move into f, accept.

Example: Construct a PDA.

 $egin{array}{ccc} \mathbf{S}
ightarrow \mathbf{aSb} \ \mathbf{S}
ightarrow \mathbf{b} \end{array}$



LR Parsing Actions

1. shift

transfer the lookahead to the stack

2. reduce

For $\mathbf{X} \to \mathbf{w},$ replace \mathbf{w} by \mathbf{X} on the stack

3. accept

input string is in language

4. error

input string is not in language

LR(1) Parse Table

• Columns:

terminals, \$ and variables

• Rows:

state numbers: represent patterns in a derivation

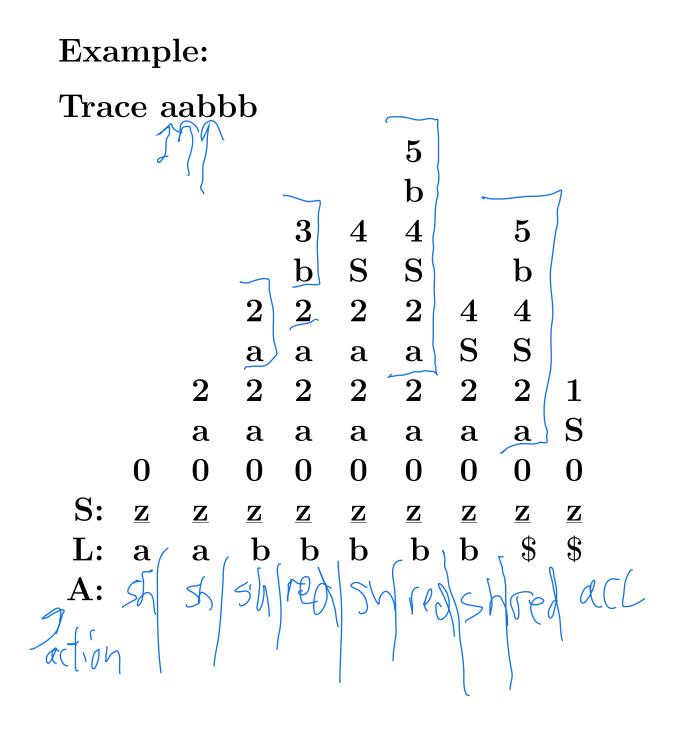


	a	b	\$	S
0	$\mathbf{s2}$	$\mathbf{s3}$		1
1			acc	
2	s2	$\mathbf{s3}$		4
3		$\mathbf{r2}$	$\mathbf{r2}$	
4		$\mathbf{s5}$		
5		$\mathbf{r1}$	$\mathbf{r1}$	

Definition of entries:

- sN shift terminal and move to state N
- N move to state N
- rN reduce by rule number N
- acc accept
- blank error

state = 0push(state) read(symbol) entry = T[state, symbol]while entry. action \neq accept do if entry.action == shift then push(symbol) state = entry.statepush(state) read(symbol) else if entry.action == reduce then do $2*size_rhs times {pop()}$ state := top-of-stack() push(entry.rule.lhs) state = T[state, entry.rule.lhs]push(state) else if entry.action == blank then error entry = T[state, symbol]end while if symbol \neq \$ then error



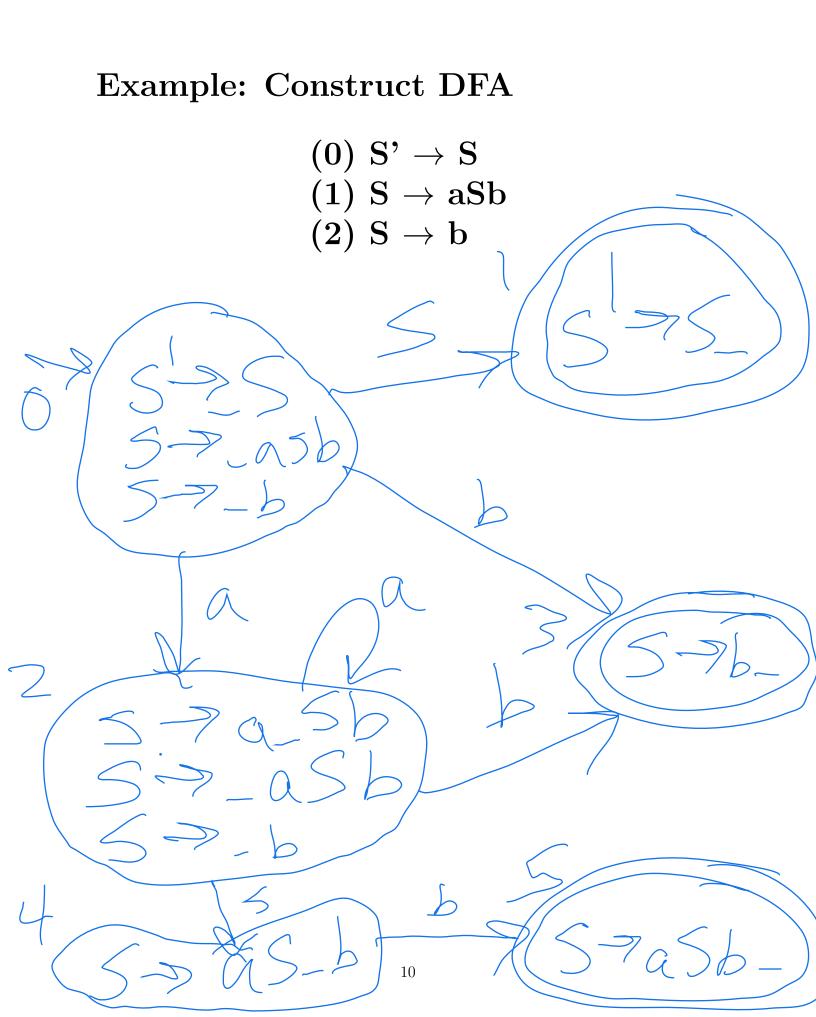
To construct the LR(1) parse table:

- Construct a dfa to model the top of the stack
- Using the dfa, construct an LR(1) parse table

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- To Construct the DFA
 - Add S' \rightarrow S
 - place a marker "_" on the rhs $S' \rightarrow _S$
 - Compute closure($S' \rightarrow _S$). Def. of closure:
 - 1. closure(A \rightarrow v_xy) = {A \rightarrow v_xy} if x is a terminal.
 - 2. closure(A \rightarrow v_xy) = {A \rightarrow v_xy} \cup (closure(x $\rightarrow _w$) for all w if x is a variable.

- The closure (S' $\rightarrow _$ S) is state 0 and "unprocessed".
- Repeat until all states have been processed
 - unproc = any unprocessed state
 - $\begin{array}{l} -\operatorname{For} \ each \ x \ that \ appears \ in \\ A {\rightarrow} u_xv \ do \end{array}$
 - * Add a transition labeled "x" from state "unproc" to a new state with production $A \rightarrow ux_v$
 - * The set of productions for the new state are: $closure(A \rightarrow ux_v)$
 - * If the new state is identical to another state, combine the states Otherwise, mark the new state as "unprocessed"
- Identify final states. Marker is M



Backtracking through the DFA

Consider aabbb

- Start in state 0.
- Shift "a" and move to state 2.
- Shift "a" and move to state 2.
- Shift "b" and move to state 3.
 Reduce by "S → b"
 Pop "b" and Backtrack to state 2.
 Shift "S" and move to state 4.
- Shift "b" and move to state 5.
 Reduce by "S → aSb"
 Pop "aSb" and Backtrack to state 2.

Shift "S" and move to state 4.

• Shift "b" and move to state 5. Reduce by "S \rightarrow aSb" Pop "aSb" and Backtrack to state 0.

Shift "S" and move to state 1.Accept. aabbb is in the language.

To construct LR(1) table from diagram:

- 1. If there is an arc from state1 to state2
 - (a) arc labeled x is terminal or T[state1, x] =sh state2

state'

- (b) arc labeled X is nonterminal T[state1, X] = state2
- 2. If state1 is a final state with $\mathbf{X}
 ightarrow \mathbf{w}_{-}$

For all a in FOLLOW(X), T[state1,a] = reduce by $X \rightarrow w$

3. If state1 is a final state with $S' \rightarrow S_{-}$ T[state1,\$] = accept

4. All other entries are error

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Example: LR(1) Parse Table

Here is the LR(1) Parse Table with \mathcal{A} by \mathcal{A} contents of each state.

Stack	State	Terminals			Variables
contents	number	a	b	\$	S
(empty)	0	22	53		
S	1			QCC	(
Ca RX.	2	52	33		4
QQX5×D	3		52	K2	1
CIQXS	4		55		
ant S b	5		r í	6	

Actions for entries in LR(1) Parse table T[state,symbol]

Let entry = T[state,symbol].

- If symbol is a terminal or \$
 - If entry is "shift state*i*"
 push lookahead and state*i* on the stack
 - If entry is "reduce by rule $\mathbf{X} \rightarrow \mathbf{w}$ "

pop w and k states (k is the size of w) from the stack.

- If entry is "accept"
 Halt. The string is in the language.
- If entry is "error"
 Halt. The string is not in the language.

• If symbol is nonterminal

We have just reduced the rhs of a production $X \rightarrow w$ to a symbol. The entry is a state number, call it state *i*. Push T[state *i*, X] on the stack. Constructing Parse Tables for CFG's with λ -rules

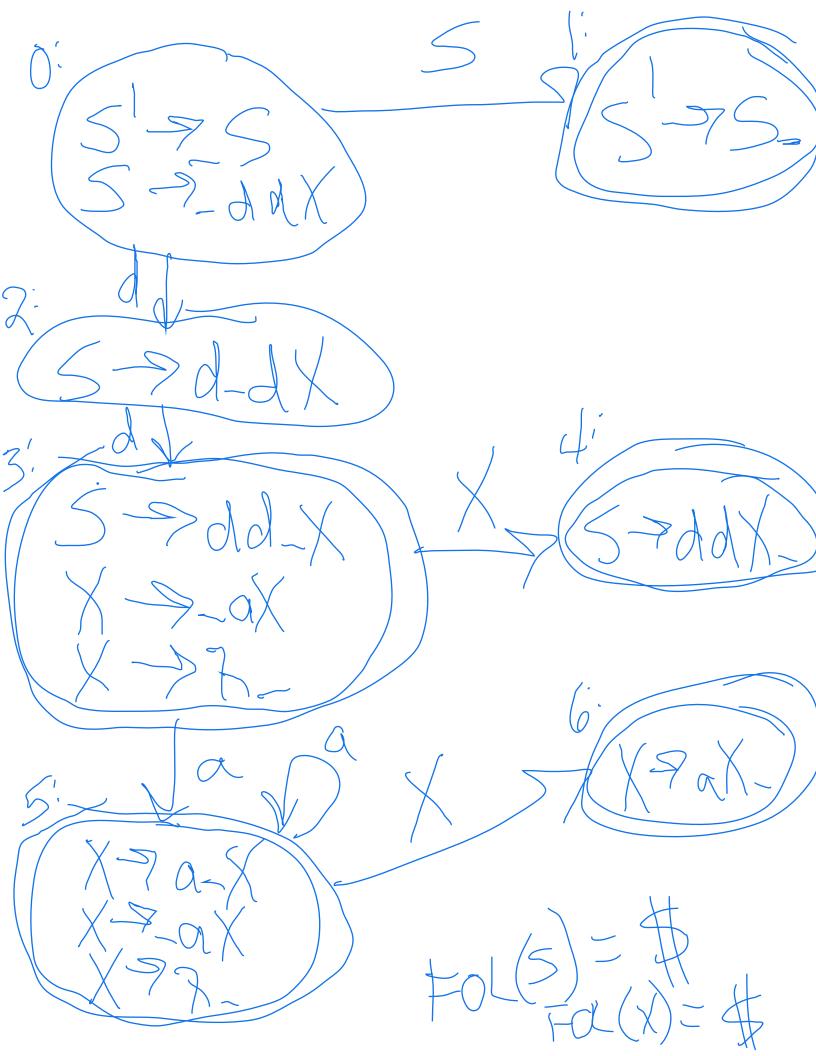
 $\mathbf{A} \rightarrow \lambda$ written as $\mathbf{A} \rightarrow \lambda_{-}$

Example

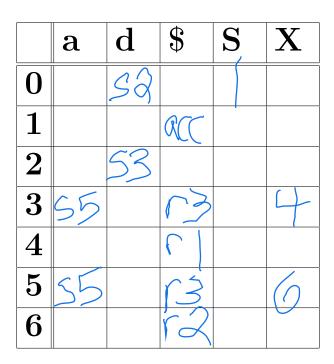
Add a new start symbol and number the rules:

$$egin{aligned} \mathbf{(0)} & \mathbf{S'}
ightarrow \mathbf{S} \ \mathbf{(1)} & \mathbf{S}
ightarrow \mathbf{ddX} \ \mathbf{(2)} & \mathbf{X}
ightarrow \mathbf{aX} \ \mathbf{(3)} & \mathbf{X}
ightarrow \lambda \end{aligned}$$

Construct the DFA:

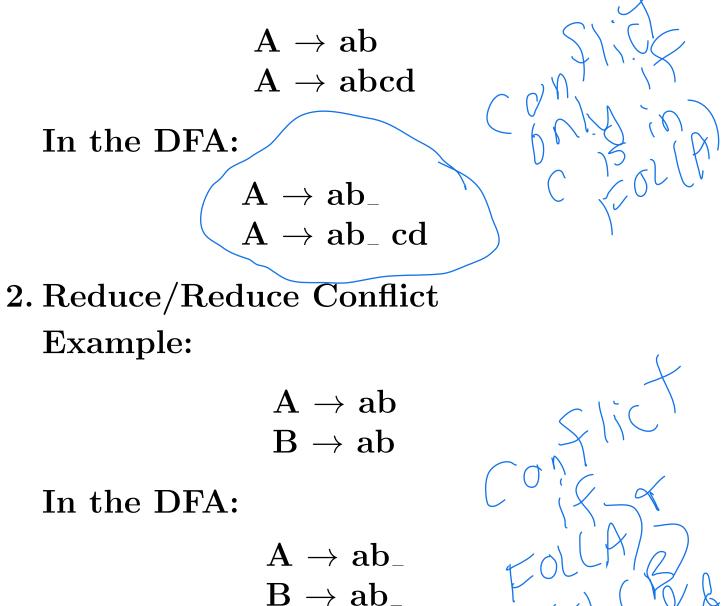


Construct the LR(1) Parse Table



Possible Conflicts:

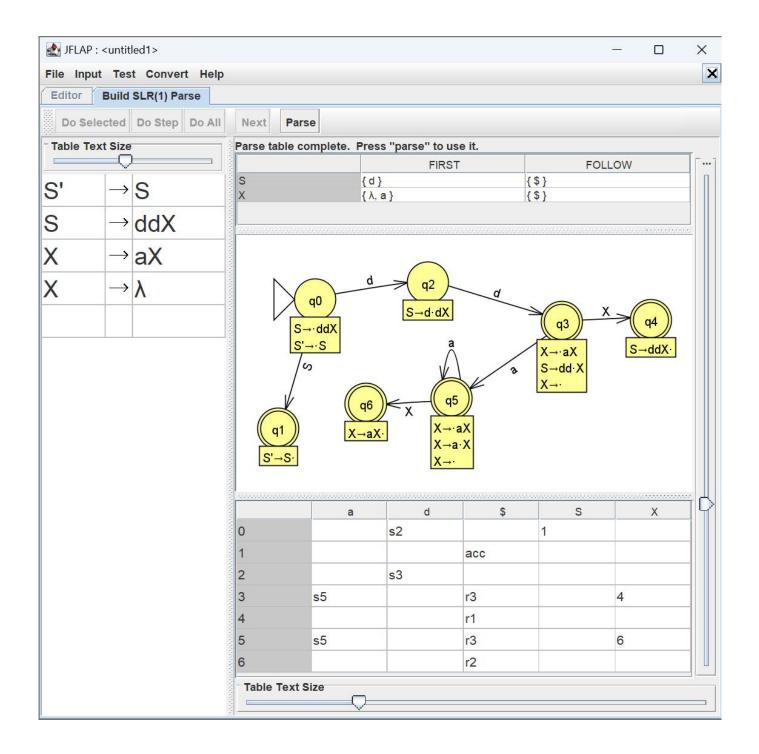
1. Shift/Reduce Conflict Example:



3. Shift/Shift Conflict

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Same example in JFLAP



Now parsing the string ddaa with the LR Parse table

	IFLAP : <	untitleo	d1>			- D X				
File	File Input Test Convert Help									
Edi	Editor Build SLR(1) Parse SLR(1) Parsing									
Table Text Size										
	a	d	\$	S	X	Start Step Noninverted Tree				
0		s2		1		Start Step Noninverted Tree				
1			acc							
2		s3				Input ddaa				
3	s5		r3		4	Input Remaining \$				
4			r1			Stack S0				
5	s5		r3		6					
6			r2			Stack SO				
	anananana		ananan		Antoninan					
	ole Text	Size			—					
L	.HS		RHS	1000						
S'	-	→ S				S				
S	-	→ dc	lX	an a						
X		→ a≯	X							
X	-	×λ		100000000						
String accepted										

From the classwork on 10/17

