

Announcements (January 13)

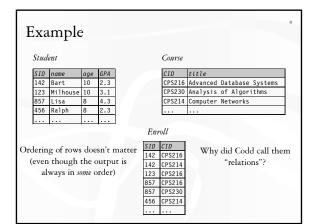
- \bigstar Homework #1 will be assigned on Thursday
- * Reading assignment for this week
 - Posted on course Web page
 - Remember to register on H2O and join Duke CPS216
 - Review due on Thursday night

Relational data model

- * A database is a collection of relations (or tables)
- Each relation has a list of attributes (or columns)
 Set-valued attributes not allowed
- Each attribute has a domain (or type)
- $\boldsymbol{\diamond}$ Each relation contains a set of tuples (or rows)

Duplicates not allowed

Simplicity is a virtue!



Schema versus instance

- Schema (metadata)
 - Specification of how data is to be structured logically
 - Defined at set-up
 - Rarely changes
- ✤ Instance
 - Content
 - Changes rapidly, but always conforms to the schema
- Compare to type and object of type in a programming language

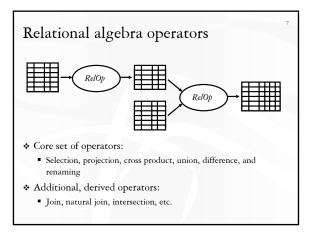
Example

✤ Schema

- Student (SID integer, name string, age integer, GPA float)
- Course (CID string, title string)
- Enroll (SID integer, CID integer)

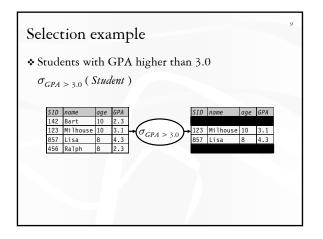
✤ Instance

- { (142, Bart, 10, 2.3), (123, Milhouse, 10, 3.1), ...}
- { (CPS216, Advanced Database Systems), ... }
- { (142, CPS216), (142, CPS214), ...}



Selection

- * Input: a table R
- * Notation: $\sigma_p(R)$
- p is called a selection condition/predicate
- $\boldsymbol{\diamond}$ Purpose: filter rows according to some criteria
- * Output: same columns as R, but only rows of R that satisfy p



More on selection

♦ Selection predicate in general can include any column of *R*, constants, comparisons such as $=, \leq$, etc., and Boolean connectives \land , \lor , and \neg

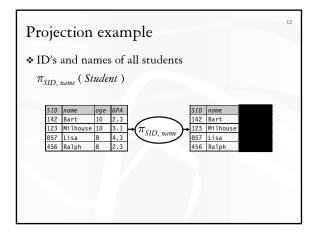
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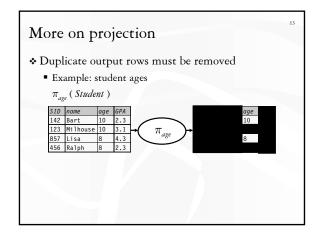
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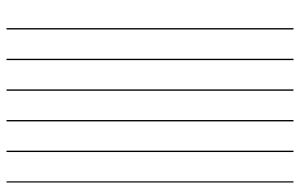
- Example: straight A students under 18 or over 21 $\sigma_{GPA \ge 4.0 \land (age < 18 \lor age > 21)}(Student)$
- But you must be able to evaluate the predicate over a single row
 - Example: student with the highest GPA

Projection

- * Input: a table R
- * Notation: $\pi_L(R)$
- *L* is a list of columns in *R*
- ✤ Purpose: select columns to output
- \clubsuit Output: same rows, but only the columns in L



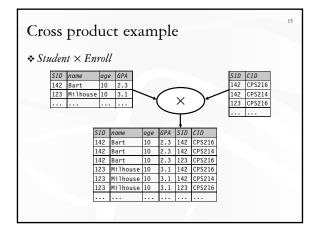




Cross product

- * Input: two tables R and S
- * Notation: $R \times S$
- * Purpose: pairs rows from two tables
- Output: for each row r in R and each row s in S, output a row rs (concatenation of r and s)

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A note on column ordering

- The ordering of columns in a table is considered unimportant (as is the ordering of rows)
- SID
 name
 age
 GPA
 SID
 CID

 142
 Bart
 10
 2.3
 142
 CPS216

 142
 Bart
 10
 2.3
 142
 CPS216

 142
 Bart
 10
 2.3
 142
 CPS216

 142
 Bart
 10
 2.3
 123
 CPS216

 123
 Milhouse
 10
 3.1
 142
 CPS216

 123
 Milhouse
 10
 3.1
 142
 CPS214

 123
 Milhouse
 10
 3.1
 142
 CPS214

 123
 Milhouse
 10
 3.1
 123
 CPS214

	SID	CID	SID	name	age	GPA
	142	CPS216	142	Bart	10	2.3
=	142	CPS214	142	Bart	10	2.3
	123	CPS216	142	Bart	10	2.3
	142	CPS216	123	Milhouse	10	3.1
	142	CPS214	123	Milhouse	10	3.1
	123	CPS216	123	Milhouse	10	3.1

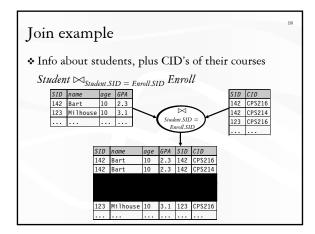
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• That means cross product is commutative, i.e., $R \times S = S \times R$ for any R and S

Derived operator: join

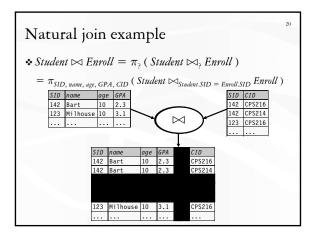
- * Input: two tables R and S
- \mathbf{A} Notation: $R \bowtie_p S$
- p is called a join condition/predicate
- Purpose: relate rows from two tables according to some criteria
- Output: for each row r in R and each row s in S, output a row rs if r and s satisfy p
- Shorthand for





Derived operator: natural join

- \bullet Input: two tables *R* and *S*
- \diamond Notation: $R \bowtie S$
- * Purpose: relate rows from two tables, and
 - Enforce equality on all common attributes
 - Eliminate one copy of common attributes
- ♦ Shorthand for π_L ($R \bowtie_p S$)
 - *L* is the union of all attributes from *R* and *S*, with duplicates removed
 - p equates all attributes common to R and S





Union

- * Input: two tables R and S
- ♦ Notation: $R \cup S$
 - R and S must have identical schema
- ♦ Output:
 - Has the same schema as R and S
 - Contains all rows in *R* and all rows in *S*, with duplicates eliminated

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Difference

- * Input: two tables R and S
- ♦ Notation: R S
 - R and S must have identical schema
- ♦ Output:
 - Has the same schema as R and S
 - Contains all rows in R that are not found in S

Derived operator: intersection

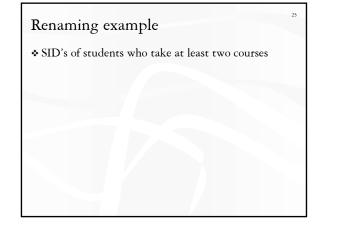
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- * Input: two tables R and S
- ♦ Notation: $R \cap S$
- R and S must have identical schema
- ♦ Output:
 - Has the same schema as R and S
 - Contains all rows that are in both R and S

Renaming

- * Input: a table R
- \bigstar Notation: $\rho_{\scriptscriptstyle S}(R),$ or $\rho_{\scriptscriptstyle S(A_1,A_2,\,\ldots)}(R)$
- Purpose: rename a table and/or its columns
- \diamond Output: a renamed table with the same rows as R
- ♦ Used to
 - Avoid confusion caused by identical column names
 - Create identical columns names for natural joins



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Summary of core operators

- $\mathbf{Selection}: \sigma_p(R)$
- Projection: π_L (R)
- * Cross product: $R \times S$
- \diamond Union: $R \cup S$
- * Difference: R S
- - Does not really add to processing power

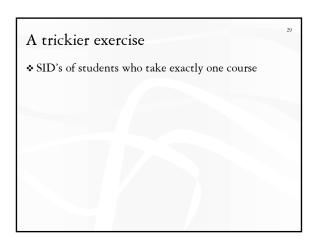
Summary of derived operators

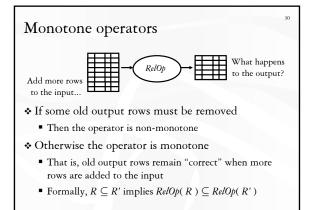
- \diamond Join: $R \bowtie_p S$
- * Natural join: $R \bowtie S$
- ♦ Intersection: $R \cap S$
- ✤ Many more
 - Semijoin, anti-semijoin, quotient, ...

An exercise

 \clubsuit CID's of the courses that Lisa is NOT taking

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Classification of relational operators

*	Selection:	$\sigma_p(R)$	Monotone

- Projection: $\pi_L(R)$ Monotone
- * Cross product: $R \times S$ Monotone Monotone
- \diamond Join: $R \bowtie_{h} S$
- ♦ Natural join: R ⋈ S Monotone
- \diamond Union: $R \cup S$
- Monotone ♦ Difference: R - SNon-monotone (not w.r.t. S)
- ♦ Intersection: $R \cap S$
- Monotone

Why is "-" needed for "exactly one"?

- * Composition of monotone operators produces a monotone query
 - Old output rows remain "correct" when more rows are added to the input
- Exactly-one query is non-monotone
 - Say Nelson is currently taking only CPS216
 - Add another record to Enroll: Nelson takes CPS214 too
 - Nelson is no longer in the answer
- * So it must use difference!

Why do we need core operator X?

Difference

- The only non-monotone operator
- Cross product
- ✤ Union

Selection? Projection?

Homework problem ⁽²⁾

Why is r.a. a good query language?

- * Declarative?
 - Yes, compared with older languages like CODASYL
 - But operators are inherently procedural
- * Simple
 - A small set of core operators who semantics are easy to grasp
- Complete?
 - With respect to what?

Relational calculus

- ♦ { $e.SID \mid e \in Enroll \land$ $\neg(\exists e' \in Enroll: e'.SID = e.SID \land e'.CID \neq e.CID$ } or { $e.SID \mid e \in Enroll \land$
 - $(\forall e' \in Enroll: e'.SID \neq e.SID \lor e'.CID \neq e.CID \}$

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- Relational algebra = "safe" relational calculus
 - Every query expressible as a safe relational calculus query is also expressible as a relational algebra query
 - And vice versa
- $\boldsymbol{\diamond}$ Example of an unsafe relational calculus query
 - { s.name $| \neg(s \in Student)$ }
 - Cannot evaluate this query just by looking at the database

Turing machine?

* Relational algebra has no recursion

- Example of something not expressible in relational algebra: Given relation *Parent(parent, child)*, who are Bart's ancestors?
- * Why not recursion?
 - Optimization becomes undecidable
 - You can always implement it at the application level
 - Recursion is added to SQL nevertheless