

### Announcements (January 13)

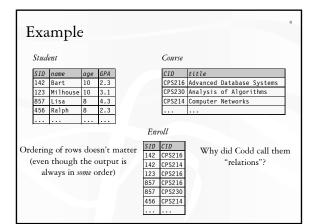
- $\bigstar$  Homework #1 will be assigned on Thursday
- \* Reading assignment for this week
  - Posted on course Web page
  - Remember to register on H2O and join Duke CPS216
  - Review due on Thursday night

# Relational data model

- \* A database is a collection of relations (or tables)
- Each relation has a list of attributes (or columns)
  Set-valued attributes not allowed
- Each attribute has a domain (or type)
- $\boldsymbol{\diamond}$  Each relation contains a set of tuples (or rows)

Duplicates not allowed

Simplicity is a virtue!



#### Schema versus instance

- Schema (metadata)
  - Specification of how data is to be structured logically
  - Defined at set-up
  - Rarely changes
- ✤ Instance
  - Content
  - Changes rapidly, but always conforms to the schema
- Compare to type and object of type in a programming language

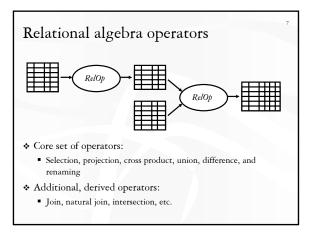
### Example

#### ✤ Schema

- Student (SID integer, name string, age integer, GPA float)
- Course (CID string, title string)
- Enroll (SID integer, CID integer)

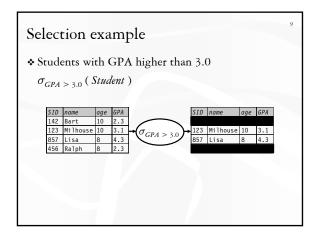
#### ✤ Instance

- { (142, Bart, 10, 2.3), (123, Milhouse, 10, 3.1), ...}
- { (CPS216, Advanced Database Systems), ... }
- { (142, CPS216), (142, CPS214), ...}



#### Selection

- \* Input: a table R
- \* Notation:  $\sigma_p(R)$
- p is called a selection condition/predicate
- $\boldsymbol{\diamond}$  Purpose: filter rows according to some criteria
- \* Output: same columns as R, but only rows of R that satisfy p



### More on selection

♦ Selection predicate in general can include any column of *R*, constants, comparisons such as  $=, \leq$ , etc., and Boolean connectives  $\land$ ,  $\lor$ , and  $\neg$ 

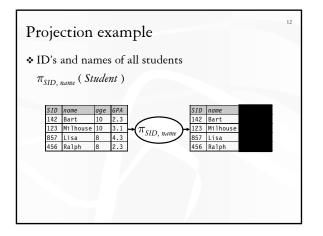
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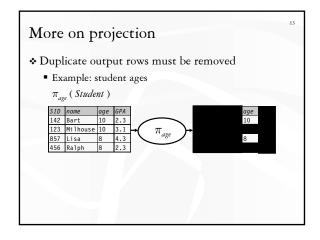
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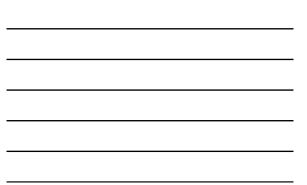
- Example: straight A students under 18 or over 21  $\sigma_{GPA \ge 4.0 \land (age < 18 \lor age > 21)}(Student)$
- But you must be able to evaluate the predicate over a single row
  - Example: student with the highest GPA

#### Projection

- \* Input: a table R
- \* Notation:  $\pi_L(R)$
- *L* is a list of columns in *R*
- ✤ Purpose: select columns to output
- $\clubsuit$  Output: same rows, but only the columns in L



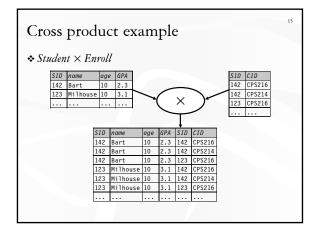




## Cross product

- \* Input: two tables R and S
- \* Notation:  $R \times S$
- \* Purpose: pairs rows from two tables
- Output: for each row r in R and each row s in S, output a row rs (concatenation of r and s)

14





## A note on column ordering

- The ordering of columns in a table is considered unimportant (as is the ordering of rows)
- SID
   name
   age
   GPA
   SID
   CID

   142
   Bart
   10
   2.3
   142
   CPS216

   142
   Bart
   10
   2.3
   142
   CPS216

   142
   Bart
   10
   2.3
   142
   CPS216

   142
   Bart
   10
   2.3
   123
   CPS216

   123
   Milhouse
   10
   3.1
   142
   CPS216

   123
   Milhouse
   10
   3.1
   142
   CPS214

   123
   Milhouse
   10
   3.1
   142
   CPS214

   123
   Milhouse
   10
   3.1
   123
   CPS214

	SID	CID	SID	name	age	GPA
	142	CPS216	142	Bart	10	2.3
=	142	CPS214	142	Bart	10	2.3
	123	CPS216	142	Bart	10	2.3
	142	CPS216	123	Milhouse	10	3.1
	142	CPS214	123	Milhouse	10	3.1
	123	CPS216	123	Milhouse	10	3.1

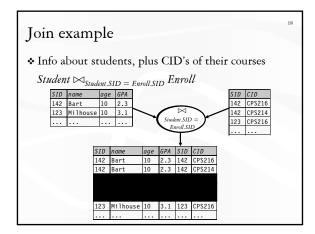
16

17

• That means cross product is commutative, i.e.,  $R \times S = S \times R$  for any R and S

#### Derived operator: join

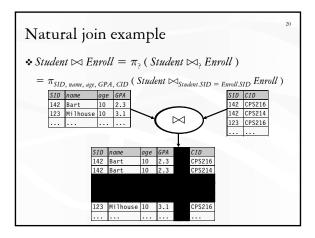
- \* Input: two tables R and S
- $\mathbf{A}$  Notation:  $R \bowtie_p S$
- p is called a join condition/predicate
- Purpose: relate rows from two tables according to some criteria
- Output: for each row r in R and each row s in S, output a row rs if r and s satisfy p
- Shorthand for





# Derived operator: natural join

- $\bullet$  Input: two tables *R* and *S*
- $\diamond$  Notation:  $R \bowtie S$
- \* Purpose: relate rows from two tables, and
  - Enforce equality on all common attributes
  - Eliminate one copy of common attributes
- ♦ Shorthand for  $\pi_L$  (  $R \bowtie_p S$  )
  - *L* is the union of all attributes from *R* and *S*, with duplicates removed
  - p equates all attributes common to R and S





#### Union

- \* Input: two tables R and S
- ♦ Notation:  $R \cup S$ 
  - R and S must have identical schema
- ♦ Output:
  - Has the same schema as R and S
  - Contains all rows in *R* and all rows in *S*, with duplicates eliminated

21

# Difference

- \* Input: two tables R and S
- ♦ Notation: R S
  - R and S must have identical schema
- ♦ Output:
  - Has the same schema as R and S
  - Contains all rows in R that are not found in S

## Derived operator: intersection

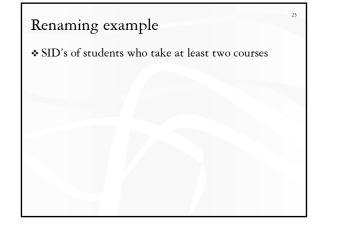
23

24

- \* Input: two tables R and S
- ♦ Notation:  $R \cap S$
- R and S must have identical schema
- ♦ Output:
  - Has the same schema as R and S
  - Contains all rows that are in both R and S

# Renaming

- \* Input: a table R
- $\bigstar$  Notation:  $\rho_{\scriptscriptstyle S}(R),$  or  $\rho_{\scriptscriptstyle S(A_1,A_2,\,\ldots)}(R)$
- Purpose: rename a table and/or its columns
- $\diamond$  Output: a renamed table with the same rows as R
- ♦ Used to
  - Avoid confusion caused by identical column names
  - Create identical columns names for natural joins



26

# Summary of core operators

- $\mathbf{Selection}: \sigma_p(R)$
- Projection:  $\pi_L$  ( R )
- \* Cross product:  $R \times S$
- $\diamond$  Union:  $R \cup S$
- \* Difference: R S
- - Does not really add to processing power

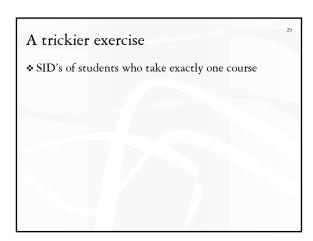
# Summary of derived operators

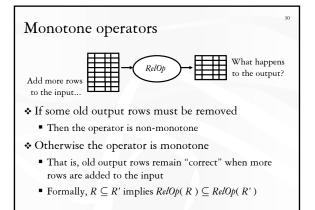
- $\diamond$  Join:  $R \bowtie_p S$
- \* Natural join:  $R \bowtie S$
- ♦ Intersection:  $R \cap S$
- ✤ Many more
  - Semijoin, anti-semijoin, quotient, ...

# An exercise

 $\clubsuit$  CID's of the courses that Lisa is NOT taking

28





# Classification of relational operators

*	Selection:	$\sigma_p(R)$	Monotone

- Projection:  $\pi_L(R)$ Monotone
- \* Cross product:  $R \times S$ Monotone Monotone
- $\diamond$  Join:  $R \bowtie_{h} S$
- ♦ Natural join: R ⋈ S Monotone
- $\diamond$  Union:  $R \cup S$
- Monotone ♦ Difference: R - SNon-monotone (not w.r.t. S)
- ♦ Intersection:  $R \cap S$
- Monotone

# Why is "-" needed for "exactly one"?

- \* Composition of monotone operators produces a monotone query
  - Old output rows remain "correct" when more rows are added to the input
- Exactly-one query is non-monotone
  - Say Nelson is currently taking only CPS216
  - Add another record to Enroll: Nelson takes CPS214 too
  - Nelson is no longer in the answer
- \* So it must use difference!

## Why do we need core operator X?

Difference

- The only non-monotone operator
- Cross product
- ✤ Union

#### Selection? Projection?

Homework problem <sup>(2)</sup>

# Why is r.a. a good query language?

- \* Declarative?
  - Yes, compared with older languages like CODASYL
  - But operators are inherently procedural
- \* Simple
  - A small set of core operators who semantics are easy to grasp
- Complete?
  - With respect to what?

### Relational calculus

- ♦ {  $e.SID \mid e \in Enroll \land$   $\neg(\exists e' \in Enroll: e'.SID = e.SID \land e'.CID \neq e.CID$  } or {  $e.SID \mid e \in Enroll \land$ 
  - $(\forall e' \in Enroll: e'.SID \neq e.SID \lor e'.CID \neq e.CID \}$

35

- Relational algebra = "safe" relational calculus
  - Every query expressible as a safe relational calculus query is also expressible as a relational algebra query
  - And vice versa
- $\boldsymbol{\diamond}$  Example of an unsafe relational calculus query
  - { s.name  $| \neg(s \in Student)$  }
  - Cannot evaluate this query just by looking at the database

## Turing machine?

#### \* Relational algebra has no recursion

- Example of something not expressible in relational algebra: Given relation *Parent(parent, child)*, who are Bart's ancestors?
- \* Why not recursion?
  - Optimization becomes undecidable
  - You can always implement it at the application level
  - Recursion is added to SQL nevertheless