Relational Model & Algebra

CPS 216
Advanced Database Systems

Announcements (January 13)

- ❖ Homework #1 will be assigned on Thursday
- * Reading assignment for this week
 - Posted on course Web page
 - Remember to register on H2O and join Duke CPS216
 - Review due on Thursday night

Relational data model

- * A database is a collection of relations (or tables)
- ❖ Each relation has a list of attributes (or columns)
 - Set-valued attributes not allowed
- ❖ Each attribute has a domain (or type)
- ❖ Each relation contains a set of tuples (or rows)
 - Duplicates not allowed
- ☞ Simplicity is a virtue!

Example

Student

ı	SID	name	age	GPA
ı	142	Bart	10	2.3
ı	123	Milhouse	10	3.1
ı	857	Lisa	8	4.3
ı	456	Ralph	8	2.3
ı				

Course

	CID title	
		Advanced Database Systems
		Analysis of Algorithms
	CPS214	Computer Networks
ľ		

Enroll

456 CPS214

Ordering of rows doesn't matter (even though the output is always in *some* order)

SID CID 142 CPS216 142 CPS214 123 CPS216 857 CPS216 From

Why did Codd call them "relations"?

Each *n*-tuple relates *n* elements from *n* domains, precisely in the mathematical sense of a "relation"

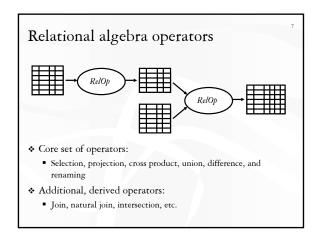
Schema versus instance

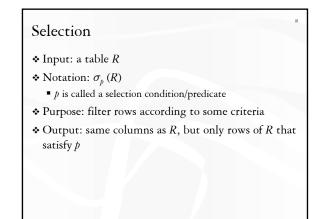
- Schema (metadata)
 - Specification of how data is to be structured logically
 - Defined at set-up
 - Rarely changes
- Instance
 - Content
 - Changes rapidly, but always conforms to the schema
- Compare to type and object of type in a programming language

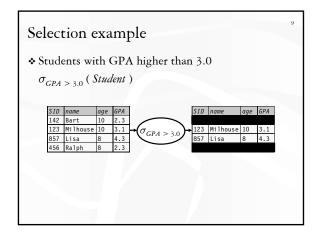
Example

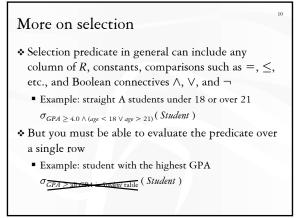
- ❖ Schema
 - Student (SID integer, name string, age integer, GPA float)
 - Course (CID string, title string)
 - Enroll (SID integer, CID integer)
- ❖ Instance
 - { (142, Bart, 10, 2.3), (123, Milhouse, 10, 3.1), ...}
 - { ⟨CPS216, Advanced Database Systems⟩, ...}
 - $\bullet \ \{ \ \langle 142, \text{CPS216} \rangle, \ \langle 142, \text{CPS214} \rangle, \ldots \}$

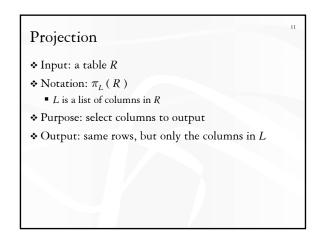
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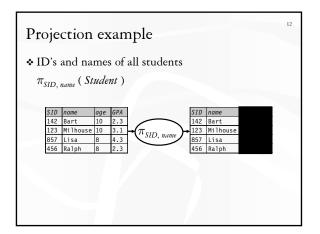


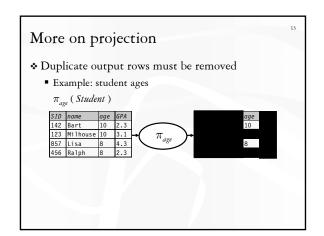


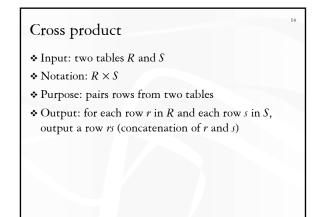


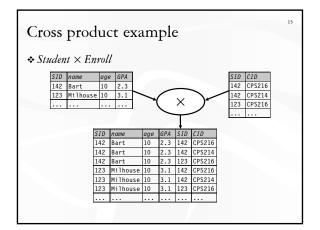


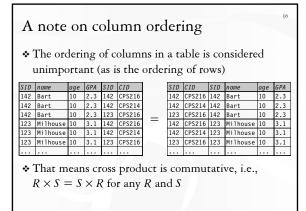


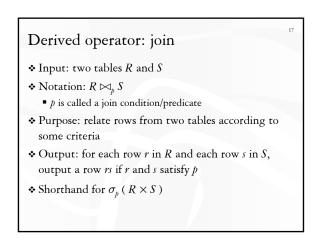


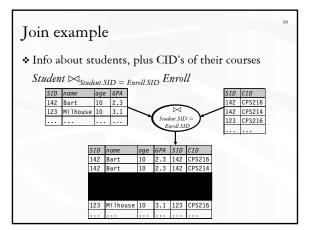












Derived operator: natural join

- \diamond Input: two tables R and S
- ❖ Notation: $R \bowtie S$
- * Purpose: relate rows from two tables, and
 - Enforce equality on all common attributes
 - Eliminate one copy of common attributes
- ❖ Shorthand for π_L ($R \bowtie_p S$)
 - L is the union of all attributes from R and S, with duplicates removed
 - \blacksquare p equates all attributes common to R and S

Natural join example			
♦ Student \bowtie Enroll = π , (Student \bowtie , Enroll)			
$=\pi_{SID,\;name,\;age,\;GPA,\;CID}\;(\;Student \bowtie_{Student.SID} = \underbrace{Enroll.SID}\;Enroll\;)$ $\frac{SID\;\;name}{142\;\;Bart}\;\;10\;\;2.3$ $123\;\;Milhouse\;10\;\;3.1$ $\dots\;\dots\;\dots\;\dots$			
SID name age GPA CID 142 Bart 10 2.3 CPS216 142 Bart 10 2.3 CPS214			
123 Milhouse 10 3.1 CPS216			

Union

❖ Input: two tables R and S

❖ Notation: $R \cup S$

R and S must have identical schema

- Output:
 - Has the same schema as *R* and *S*
 - Contains all rows in R and all rows in S, with duplicates eliminated

Difference

❖ Input: two tables R and S

❖ Notation: R - S

R and S must have identical schema

- Output:
 - Has the same schema as R and S

Contains all rows in R that are not found in S

Derived operator: intersection

❖ Input: two tables R and S

❖ Notation: $R \cap S$

R and S must have identical schema

- Output:
 - Has the same schema as R and S
 - Contains all rows that are in both R and S
- ❖ Shorthand for R (R S)
- ❖ Also equivalent to S (S R)
- \diamond And to $R \bowtie S$

Renaming

❖ Input: a table R

* Notation: ρ_{S} (R), or $\rho_{S(A_{1},A_{2},...)}$ (R)

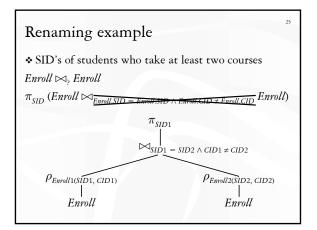
* Purpose: rename a table and/or its columns

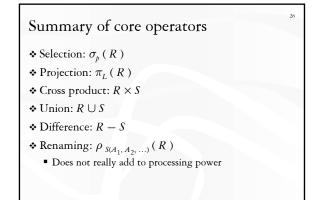
 \diamond Output: a renamed table with the same rows as R

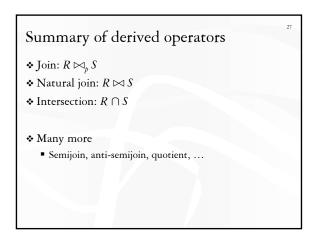
❖ Used to

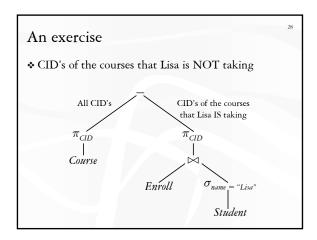
- Avoid confusion caused by identical column names
- Create identical columns names for natural joins

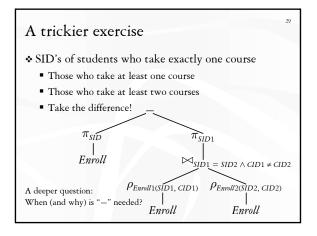
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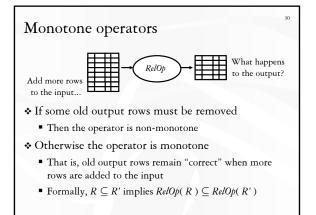












Classification of relational operators

 ❖ Selection: $\sigma_p(R)$ Monotone

 ❖ Projection: $\pi_L(R)$ Monotone

 ❖ Cross product: $R \times S$ Monotone

 ❖ Join: $R \bowtie_p S$ Monotone

 ❖ Natural join: $R \bowtie S$ Monotone

 ❖ Union: $R \cup S$ Monotone

❖ Difference: R - S Non-monotone (not w.r.t. S)

❖ Intersection: $R \cap S$ Monotone

Why is "-" needed for "exactly one"?

- Composition of monotone operators produces a monotone query
 - Old output rows remain "correct" when more rows are added to the input
- * Exactly-one query is non-monotone
 - Say Nelson is currently taking only CPS216
 - Add another record to *Enroll*: Nelson takes CPS214 too
 - Nelson is no longer in the answer
- So it must use difference!

Why do we need core operator X?

- Difference
 - The only non-monotone operator
- Cross product
 - The only operator that adds columns
- ❖ Union
 - The only operator that allows you to add rows?
 - A more rigorous proof?
- Selection? Projection?
 - Homework problem ^③

Why is r.a. a good query language?

- ❖ Declarative?
 - Yes, compared with older languages like CODASYL
 - But operators are inherently procedural
- Simple
 - A small set of core operators who semantics are easy to grasp
- ❖ Complete?
 - With respect to what?

Relational calculus

❖ { $e.SID \mid e \in Enroll \land$

 $\neg(\exists e' \in Enroll: e'.SID = e.SID \land e'.CID \neq e.CID \} \text{ or } \{ e.SID \mid e \in Enroll \land$

 $(\forall e' \in \textit{Enroll: } e'.SID \neq e.SID \lor e'.CID = e.CID \}$

- ❖ Relational algebra = "safe" relational calculus
 - Every query expressible as a safe relational calculus query is also expressible as a relational algebra query
 - And vice versa
- * Example of an unsafe relational calculus query
 - $\{ s.name \mid \neg(s \in Student) \}$
 - · Cannot evaluate this query just by looking at the database

Turing machine?

- * Relational algebra has no recursion
 - Example of something not expressible in relational algebra: Given relation *Parent(parent, child)*, who are Bart's ancestors?
- Why not recursion?
 - Optimization becomes undecidable
 - You can always implement it at the application level
 - Recursion is added to SQL nevertheless

36

6