

### Announcements (February 22)

- Reading assignment for this week
- Variant indexes (due next Monday)
- Homework #2 due in 1½ weeks (March 3)
- Course project proposal due in 2 weeks
- ♦ Midterm in 2½ weeks

## Overview

- \* Many different ways of processing the same query
  - Scan? Sort? Hash? Use an index?
  - All with different performance characteristics
- \* Best choice depends on the situation
  - Implement all alternatives
  - Let the query optimizer choose at run-time

## Notation

- \* Relations: R, S
- ✤ Tuples: r, s
- Number of tuples: |R|, |S|
- \* Number of disk blocks: B(R), B(S)
- Number of memory blocks available: M
- Cost metric
  - Number of I/O's
  - Memory requirement

#### Table scan

- $\diamond$  Scan table *R* and process the query
  - Selection over R
  - Projection of R without duplicate elimination
- **♦** I/O's: *B*(*R*)
  - Trick for selection: stop early if it is a lookup by key
- Memory requirement: 2 (double buffering)
- \* Not counting the cost of writing the result out
  - Same for any algorithm!
  - Maybe not needed—results may be pipelined directly into another operator

# Nested-loop join

#### $R \bowtie_p S$

- For each block of *R*, and for each *r* in the block: For each block of *S*, and for each *s* in the block: Output *rs* if *p* evaluates to true over *r* and *s* 
  - R is called the outer table; S is called the inner table
- $\mathbf{I}$ O's:  $B(R) + |R| \cdot B(S)$
- Memory requirement: 4 (double buffering)
- Improvement: block-based nested-loop join
  - For each block of *R*, and for each block of *S*:
     For each *r* in the *R* block, and for each *s* in the *S* block: ...
  - I/O's:  $B(R) + B(R) \cdot B(S)$
  - Memory requirement: same as before

## More improvements of nested-loop join

\* Stop early

- If the key of the inner table is being matched
- May reduce half of the I/O's (less for block-based)
- Make use of available memory

## External merge sort

Problem: sort R, but R does not fit in memory

- Pass 0: read M blocks of R at a time, sort them, and write out a level-0 run
  - There are  $\left\lceil B(R) / M \right\rceil$  level-0 sorted runs
- ♦ Pass *i*: merge (M 1) level-(i-1) runs at a time, and write out a level-*i* run
  - (M-1) memory blocks for input, 1 to buffer output
  - # of level-*i* runs =  $\left[ \# \text{ of level-}(i-1) \operatorname{runs} / (M-1) \right]$
- \* Final pass produces 1 sorted run

## Example of external merge sort

Input: 1, 7, 4, 5, 2, 8, 9, 6, 3, 0

- Each block holds one number, and memory has 3 blocks
  Pass 0
  - 1, 7,  $4 \rightarrow 1, 4, 7$
  - 5, 2,  $8 \rightarrow 2, 5, 8$
  - 9, 6,  $3 \rightarrow 3, 6, 9$
  - 0  $\rightarrow 0$
- ✤ Pass 1

```
    1, 4, 7 + 2, 5, 8 → 1, 2, 4, 5, 7, 8
```

- 3, 6, 9 + 0  $\rightarrow$  0, 3, 6, 9
- Pass 2 (final)

```
• 1, 2, 4, 5, 7, 8 + 0, 3, 6, 9 \rightarrow 0, 1, 2, 3, 4, 5, 6, 7, 8, 9
```

# Performance of external merge sort

- ♦ Number of passes:  $\lceil \log_{M-1} \lceil B(R) / M \rceil \rceil + 1$
- **◊** I/O's
  - Multiply by  $2 \cdot B(R)$ : each pass reads the entire relation once and writes it once
  - Subtract B(R) for the final pass
  - Roughly, this is  $O(B(R) \cdot \log_M B(R))$
- Memory requirement: M (as much as possible)

### Some tricks for sorting

- Double buffering
  - Allocate an additional block for each run
- ✤ Blocked I/O
  - Instead of reading/writing one disk block at time, read/write a bunch ("cluster")

 Dealing with input whose size is not an exact power of fan-in



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## Internal sort algorithm

\* Quicksort

☞Fast

- \* Replacement selection
  - One block for input, one for output, rest for a heap
  - Fill the heap with input records
  - Find the smallest record in the heap that is no less than the largest record in the current run
    - If that exists, move it to the output buffer, and move a new record from input buffer into the heap
    - If that does not exist, flush output and start a new run
  - Slower than quicksort, but produces longer runs (twice the size of memory if records are in random order)

#### Sort-merge join

#### $\bigstar R \bowtie_{R.A = S.B} S$

♦ Sort *R* and *S* by their join attributes, and then merge r, s = the first tuples in sorted *R* and *S* Repeat until one of *R* and *S* is exhausted: If r.A > s.B then s = next tuple in *S* else if r.A < s.B then r = next tuple in *R* else output all matching tuples, and r, s = next in *R* and *S* 

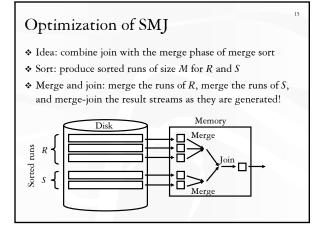
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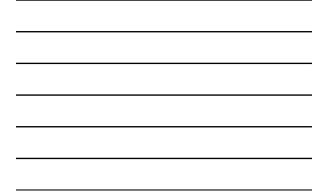
#### $\mathbf{I}$ /O's: sorting + 2 B(R) + 2 B(S)

- In most cases (e.g., join of key and foreign key)
- Worst case is  $B(R) \cdot B(S)$ : everything joins

Example		14
<i>R</i> :	S:	$R \bowtie_{R.A = S.B} S:$
$\Rightarrow r_1 A = 1$	$\Rightarrow s_1 \cdot B = 1$	$r_1 s_1$
$\Rightarrow r_2 A = 3$	$\Rightarrow s_2 \cdot B = 2$	$r_2 s_3$
$r_3 A = 3$	$\Rightarrow s_3.B = 3$	$r_2s_4$
$\Rightarrow r_4 A = 5$	$s_4 B = 3$	$r_3 s_3$
$\Rightarrow r_5 A = 7$	$\Rightarrow s_5.B = 8$	$r_3 s_4$
$\Rightarrow r_6 A = 7$		$r_7 s_5$
$\Rightarrow r_7 A = 8$		







## Performance of two-pass SMJ

- $\mathbf{I}/\mathbf{O}$ 's:  $3 \cdot (B(R) + B(S))$
- Memory requirement
  - To be able to merge in one pass, we should have enough memory to accommodate one block from each run: M > B(R) / M + B(S) / M
  - $M > \operatorname{sqrt}(B(R) + B(S))$

#### Other sort-based algorithms

- Union (set), difference, intersection
  More or less like SMJ
- Duplication elimination
  - External merge sort

• Eliminate duplicates in sort and merge

- ✤ GROUP BY and aggregation
  - External merge sort
    - Produce partial aggregate values in each run
    - Combine partial aggregate values during merge
    - Partial aggregate values don't always work though

## Hash join

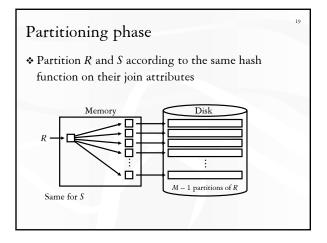
#### $\bigstar R \bowtie_{R.A = S.B} S$

- ✤ Main idea
  - Partition R and S by hashing their join attributes, and then consider corresponding partitions of R and S
  - If *r*.*A* and *s*.*B* get hashed to different partitions, they don't join

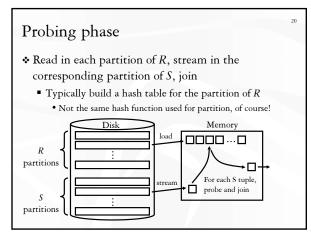


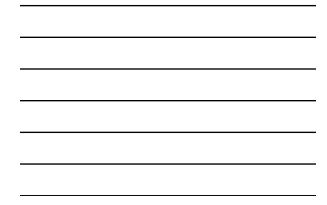
Nested-loop join considers all slots Hash join considers only those along the diagonal

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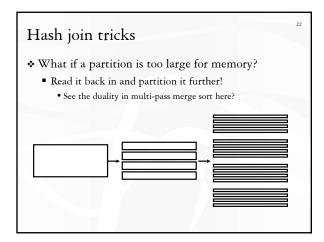




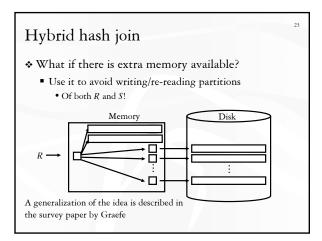
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## Performance of hash join

- $I/O's: 3 \cdot (B(R) + B(S))$
- Memory requirement:
  - In the probing phase, we should have enough memory to fit one partition of  $R: M 1 \ge B(R) / (M 1)$
  - $M > \operatorname{sqrt}(B(R))$
  - We can always pick R to be the smaller relation, so:
     M > sqrt(min(B(R), B(S)))





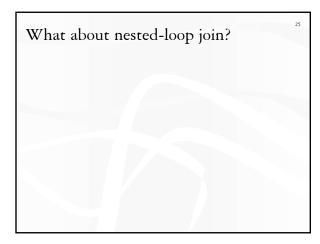


# Hash join versus SMJ

(Assuming two-pass)

- ♦ I/O's: same
- Memory requirement: hash join is lower
  - $\operatorname{sqrt}(\min(B(R), B(S)) < \operatorname{sqrt}(B(R) + B(S))$
- Other factors
  - Hash join performance depends on the quality of the hash
     Might not get evenly sized buckets

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## Other hash-based algorithms

- Union (set), difference, intersection
  More or less like hash join
- Duplicate elimination
  - Check for duplicates within each partition/bucket
- ✤ GROUP BY and aggregation
  - Apply the hash functions to GROUP BY attributes
  - Tuples in the same group must end up in the same partition/bucket
  - Keep a running aggregate value for each group

## Duality of sort and hash

- Divide-and-conquer paradigm
  - Sorting: physical division, logical combination
  - Hashing: logical division, physical combination
- Handling very large inputs
  - Sorting: multi-level merge
  - Hashing: recursive partitioning
- ♦ I/O patterns
  - Sorting: sequential write, random read (merge)
  - Hashing: random write, sequential read (partition)