

# CompSci 6

## Programming Design and Analysis

|  |     |                    |
|--|-----|--------------------|
| $t_0$                                    | $=$ | 2.0                |
| $t_1 = \frac{1}{2}(t_0 + \frac{2}{t_0})$ | $=$ | 1.5                |
| $t_2 = \frac{1}{2}(t_1 + \frac{2}{t_1})$ | $=$ | 1.4166666666666665 |
| $t_3 = \frac{1}{2}(t_2 + \frac{2}{t_2})$ | $=$ | 1.4142156862745097 |
| $t_4 = \frac{1}{2}(t_3 + \frac{2}{t_3})$ | $=$ | 1.4142135623746899 |
| $t_5 = \frac{1}{2}(t_4 + \frac{2}{t_4})$ | $=$ | 1.414213562373095  |

February 4, 2010

Prof. Rodger and Prof. Forbes

## Announcements

- Reading for next time
  - Chap. 4.6, Chap 7.5, Chap 11.1
  - Reading Quiz due before next class
- Assignment 3 due tonight!
- Assignment 4 out.

## Estimation

- Square Root:
  - Given a real number  $c$  and some error tolerance *epsilon*
  - Estimate  $t$ , the square root of  $c$
- Pi:
  - Estimate  $\pi$  with a given number of *Monte Carlo* trials

## While Loops: Square Root

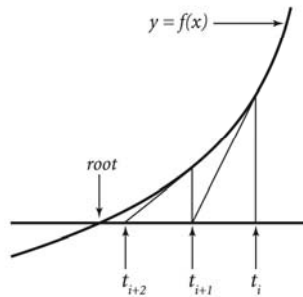
- Q. How might we implement `Math.sqrt()`?
- A. To compute the square root of  $c$ :
  - Initialize  $t_0 = c$ .
  - Repeat until  $t_i = c / t_i$ , up to desired precision:  
set  $t_{i+1}$  to be the average of  $t_i$  and  $c / t_i$ .

|  |     |                    |
|--|-----|--------------------|
| $t_0$                                    | $=$ | 2.0                |
| $t_1 = \frac{1}{2}(t_0 + \frac{2}{t_0})$ | $=$ | 1.5                |
| $t_2 = \frac{1}{2}(t_1 + \frac{2}{t_1})$ | $=$ | 1.4166666666666665 |
| $t_3 = \frac{1}{2}(t_2 + \frac{2}{t_2})$ | $=$ | 1.4142156862745097 |
| $t_4 = \frac{1}{2}(t_3 + \frac{2}{t_3})$ | $=$ | 1.4142135623746899 |
| $t_5 = \frac{1}{2}(t_4 + \frac{2}{t_4})$ | $=$ | 1.414213562373095  |

computing the square root of 2

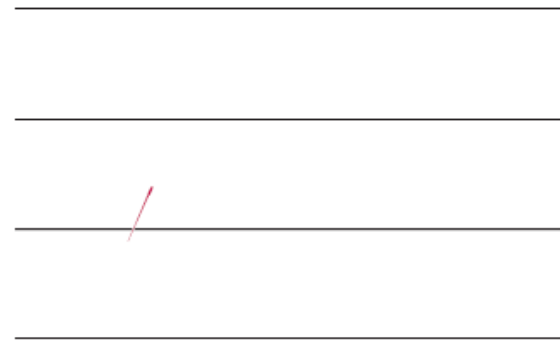
# Newton-Raphson Method

- Square root method explained.  $f(x) = x^2 - c$  to compute  $\sqrt{c}$ 
  - Goal: find root of function  $f(x)$ .
  - Start with estimate  $t_0 = c$ .
  - Draw line tangent to curve at  $x = t_i$ .
  - Set  $t_{i+1}$  to be x-coordinate where line hits x-axis.
  - Repeat until desired precision.



5

# Buffon Needle Experiment

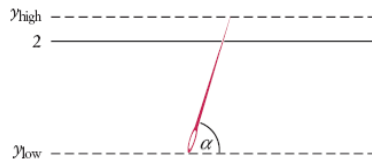


**Figure 3** The Buffon Needle Experiment

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# Needle Position

- Needle length = 1, distance between lines = 2
- Generate random  $y_{low}$  between 0 and 2
- Generate random angle  $\alpha$  between 0 and 180 degrees
- $y_{high} = y_{low} + \sin(\alpha)$
- Hit if  $y_{high} \geq 2$



**Figure 4**

When Does the Needle Fall on a Line?

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# Constructing objects/Applying methods

- Class Rectangle in Chapter 2
- Creating a Rectangle object with x, y, width, and height
 

```
Rectangle box = new Rectangle(5, 10, 20, 30);
```
- Applying Methods
 

```
box.translate(15, 25); // move the rectangle
System.out.println("x: ", box.getX()); // print x
System.out.println("y: ", box.getY()); // print y
```

## Parts of a Class

- State
  - Data
- Constructors
  - Initialize state when object is created
- Accessor methods
  - Accessing data
- Mutator methods
  - Modify data – change the state

## Class Example

- Needle class – `Needle.java`
  - Defines state and behavior of Needle
  - Keeps track of the number of times needle hits the line
  - Use `drop()` method to simulate dropping needle
- `java.util.Random` class in Java library
  - `nextDouble()` generates pseudo-random numbers in  $[0,1]$

### ch06/random2/Needle.java

```
01: import java.util.Random;
02:
03: /**
04:  * This class simulates a needle in the Buffon needle experiment.
05:  */
06: public class Needle
07: {
08:     /**
09:      * Constructs a needle.
10:      */
11:     public Needle()
12:     {
13:         hits = 0;
14:         tries = 0;
15:         generator = new Random();
16:     }
17:
18:     /**
19:      * Drops the needle on the grid of lines and
20:      * remembers whether the needle hit a line.
21:      */
```

*Continued*

### ch06/random2/Needle.java (cont.)

```
22:     public void drop()
23:     {
24:         double ylow = 2 * generator.nextDouble();
25:         double angle = 180 * generator.nextDouble();
26:
27:         // Computes high point of needle
28:
29:         double yhigh = ylow + Math.sin(Math.toRadians(angle));
30:         if (yhigh >= 2) myHits++;
31:         tries++;
32:     }
33:
34:     /**
35:      * Gets the number of times the needle hit a line.
36:      * @return the hit count
37:      */
38:     public int getHits()
39:     {
40:         return myHits;
41:     }
42:
```

*Continued*

## ch06/random2/Needle.java (cont.)

```
43:  /**
44:      Gets the total number of times the needle was dropped.
45:      @return the try count
46:  */
47:  public int getTries()
48:  {
49:      return myTries;
50:  }
51:
52:  private Random myGenerator;
53:  private int myHits;
54:  private int myTries;
55: }
```

### Intended Output:

```
Tries = 10000, Tries / Hits = 3.08928
Tries = 1000000, Tries / Hits = 3.14204
```

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## Classwork Today – Loops/Classes

- Snarf the *classwork* project
- Complete Sqrt
  - Finish *estimate* method
  - Print results
- Complete Needle
  - Finish *main* method
  - Print results
- Classwork handout has all the details
- Submit under assignment name *Class07-Feb04*