



# Today

- Big-Oh

# O

- Snarf today's code



# Announcements

- Hangman - Due tomorrow!
- APT set 2 - Due Jan 29
- NO recitation prep for Friday
  - Bring your book (if you have one)
  
- UTAs are in the LINK!!!!!!!!!!!!



- Data Structures
  - Array
  - ArrayList
  - HashSet
  - HashMap
- When to use?
  - function and time



- Big-Oh
  - **Estimate** time required for a program
  - No units of time!!!!!!
  - Count operations





# Big-Oh

- How to calculate Big-Oh
  - Assign costs to operations



# Big-Oh

- Declarations cost 0 units
  - `double d;`
- Operations cost 1 unit
  - `d = 4.56` //assignment
  - `d * 5` //mathematical operation
  - `return d;` //returns



# Big-Oh

```
1 public double getArea(double r){  
2     double pi;  
3     pi = 3.14;  
4     double area;  
5     area = pi * r * r;  
6     return area;  
7 }
```



# Big-Oh

```
1 public double getArea(double r){
2     double pi;           0
3     pi = 3.14;          1
4     double area;        0
5     area = pi * r * r;  3
6     return area;        1
7 }
```

Total: 5





# Big-Oh

- How to calculate Big-Oh
  - Assign costs to operations
  - Write in Big-Oh notation



# Big-Oh

```
1 public double getArea(double r){
2     double pi;           0
3     pi = 3.14;          1
4     double area;        0
5     area = pi * r * r;   3
6     return area;        1
7 }
```

Total: 5

**$O(5)$**



# Big-Oh

- How to calculate Big-Oh
  - Assign costs to operations
  - Write in Big-Oh notation
  - Simplify



# Big-Oh

- Simplify
  - Remove constants!
    - $O(4N) = O(N)$
    - $O(3N^2 + 5) = O(N^2)$
  - Remove lower order terms
    - $O(N^2 + N) = O(N^2)$



# Big-Oh

```
1 public double getArea(double r){
2     double pi;           0
3     pi = 3.14;          1
4     double area;        0
5     area = pi * r * r;  3
6     return area;        1
7 }
```

Total: 5

$$O(5) = O(1)$$



# Big-Oh

- How to calculate Big-Oh
  - Assign costs to operations
  - Write in Big-Oh notation
  - Simplify



# Code

```
1 public static int sum( int n)
2 {
3     int partialSum;
4     partialSum = 0;
5     for(int i = 1; i <= n; i++)
6         partialSum += i * i * i;
7     return partialSum;
8 }
```



# Code

```
1 public static int sum( int n)
2 {
3     int partialSum;           0
4     partialSum = 0;          1
5     for(int i = 1; i <= n; i++)  n
6         partialSum += i * i * i;  4
7     return partialSum;        1
8 }
```





# Code

```
1 public static int sum( int n)
2 {
3     int partialSum;           0
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6         partialSum += i * i * i;  4
7     return partialSum;       1
8 }
```

$O(1+N*4 + 1) = O(4N+2) = O(N)$



# Big-Oh

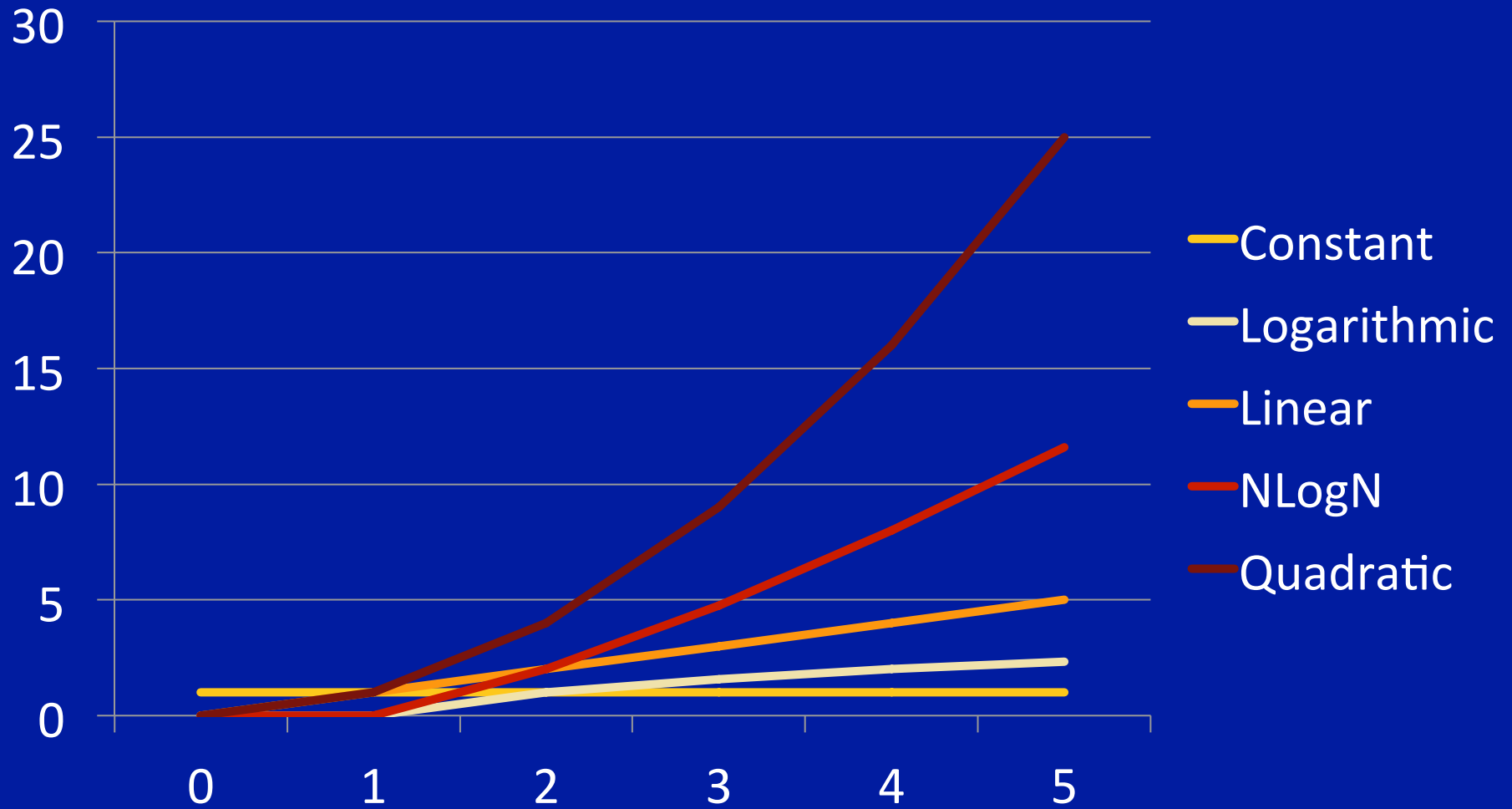
- Rules
  - for-loops
    - (statements in for-loop) \* iterations
  - Nested for-loops (inside-out)
    - (statements in innermost for-loop) \* iterations \* iterations
  - Consecutive statements
    - Add them
  - If/else
    - Test + max(if, else)



Function	Name
$c$	Constant
$\log N$	Logarithmic
$\log^2 N$	Log-squared
$N$	Linear
$N \log N$	
$N^2$	Quadratic
$N^3$	Cubic
$2^N$	Exponential



# Big-Oh





# Rules

- $T_1(N) = O(f(N))$  and  $T_2(N) = O(g(N))$ 
  - $T_1(N) + T_2(N) = O(f(N) + g(N))$
  - $T_1(N) * T_2(N) = O(f(N) * g(N))$
- $\log^k N = O(N)$



# Rules

- Remove constants!
  - $O(4N) = O(N)$
  - $O(3N^2 + 5) = O(N^2)$
- Remove lower order terms
  - $O(N^2 + N) = O(N^2)$



# Practice

- Snarf today's code
- Complete the form
  - <http://goo.gl/kuuHM>
- For the timings
  - Choose an N that is DIFFERENT from neighbors



- Big-Oh
  - **Estimate** time required for a program
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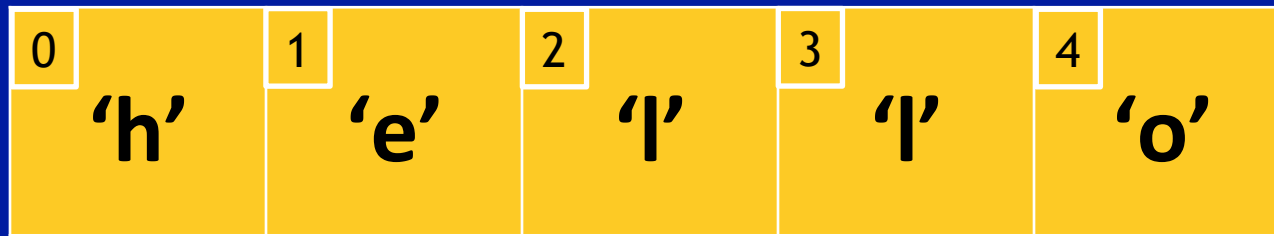


<b>Data Structure</b>	<b>Add</b>	<b>Contains</b>
Array	$O(1)$	$O(N)$
ArrayList	$O(1)$	$O(N)$
HashSet	$O(1)$	$O(1)$



# Contains

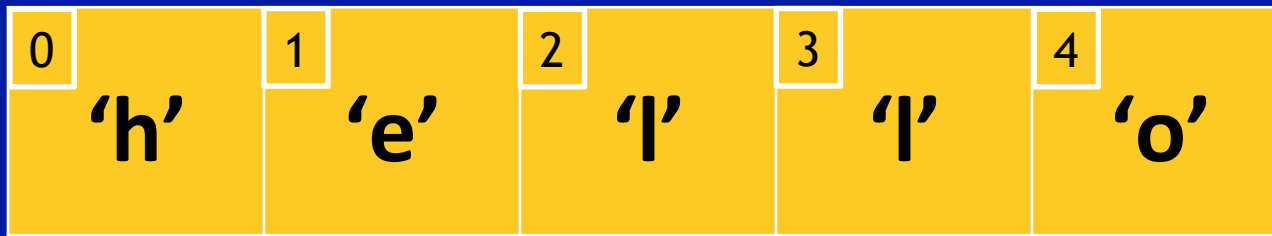
- Array and ArrayList
  - Best case?
  - Average case?
  - Worst case?





# Contains

- Array and ArrayList
  - Best case? 1
  - Average case?  $N/2$
  - Worst case?  $N$





# Contains

