

CPS 590.4: Computational Microeconomics: Game Theory, Social Choice, and Mechanism Design

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Course web page:

<http://www.cs.duke.edu/courses/spring14/compsci590.4/>

Journal, conference, ...

ACM Transactions on Economics and Computation (TEAC)



History



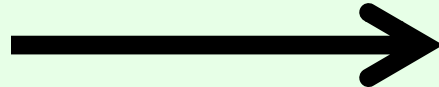
John von Neumann

computer architecture
(von Neumann
architecture)



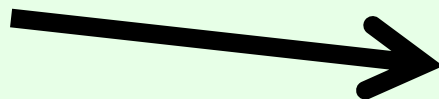
***Computer Science
& Engineering***

game theory
(minimax theorem)

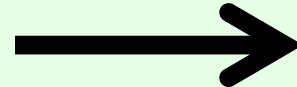
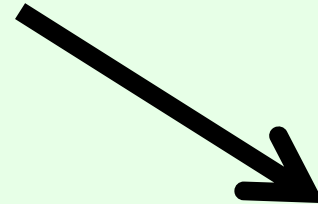


Economic Theory

linear programming
(duality)



***Mathematical
Optimization &
Operations
Research***



?

1900

1950

2000



CS-ECON@DUKE

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We are a group of people interested in the intersection of computer science and economics (and the social sciences more broadly) and the impact of this interplay on decisions in information technology and digital business. This includes applying techniques from computer science and optimization to economics -- for example, using computation to design market clearing mechanisms and to implement efficient allocation and pricing in them -- as well as applying techniques from economics to computer science -- for example, designing incentives for users of networked computer systems and social networks.

Contacts

For organizational questions about the seminar series, please contact [Dima Korzhyk](#). For other matters, please approach the relevant faculty contact(s): [Atila Abdulkadiroglu](#) (Econ), [Vincent Conitzer](#) (CS), [Rachel Kranton](#) (Econ), [Ben Lee](#) (ECE), [Kamesh Munagala](#) (CS), [Sasa Pekec](#) (Fuqua). [Pam Spencer](#) helps with catering and arranging the speakers' travel.

Mailing List

Please subscribe to the [cs-econ mailing list](#) if you are at Duke (or in the vicinity) and interested in the seminar series. The list will be used for talk announcements.



<http://econ.cs.duke.edu>

- [Atila Abdulkadiroglu](#)
Department of Economics.
- [Owen Astrachan](#)
Department of Computer Science.
- [Charles Becker](#)
Department of Economics.
- [Alexandre Belloni](#)
The Fuqua School of Business.
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- [Vincent Conitzer](#)
Department of Computer Science, and
- [Landon Cox](#)
Department of Computer Science.
- [Brendan Daley](#)
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- [Daniel A. Graham](#)
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- [Rachel E. Kranton](#)
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- [R. Vijay Krishna](#)
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- [Kenneth C Wilbur](#)
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Master's of Science in Economics and Computation (MSEC)

The MSEC degree is a joint master's program of the Departments of Economics and **Computer Science**. The joint field of economics and computation has recently emerged from two converging intellectual needs, which has created the opportunity for a truly interdisciplinary program.

The MSEC program is the outcome of exciting developments across the two fields:

- Computer science is becoming increasingly important for economists addressing complex questions on large repositories of data;
- The explosion of computer uses in all areas of life has made it necessary for computer scientists to understand the economics of computing systems; and,
- Computer scientists may now also analyze informational and financial transactions between people, businesses, governments, and electronic agents in economic terms.



"Macroeconomic problems are almost always analytically intractable and therefore require a computer to solve ... Having a background in computer science made it much easier to learn (computational) methods, as well as apply cutting-edge advances in technology to economic problems."

David Klemish
MSEM

"Tech giants such as Google, Microsoft, Yahoo, and Facebook are in many ways ahead of academia in getting computer scientists and economists to work together, and interest in these topics extends well beyond this group of companies. With this Master's program, Duke is at the forefront of catching up with industry in breaking down boundaries."

Vince Conitzer
Department of Computer Science

Application Deadline

For Fall 2014: February 15, 2014

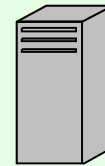
Charles Becker, MSEC Program Director

What is Economics?

- “Economics is the social science that analyzes the production, distribution, and consumption of goods and services.” [\[Wikipedia, Jan. 2014\]](#)
- Some key concepts:
 - Economic **agents** or **players** (individuals, households, firms, ...)
 - Agents’ current **endowments** of goods, money, skills, ...
 - Possible **outcomes** ((re)allocations of resources, tasks, ...)
 - Agents’ **preferences** or **utility functions** over outcomes
 - Agents’ **beliefs** (over other agents’ utility functions, endowments, production possibilities, ...)
 - Agents’ possible **decisions/actions**
 - **Mechanism** that maps decisions/actions to outcomes

An economic picture

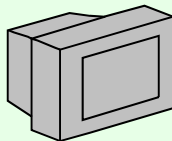
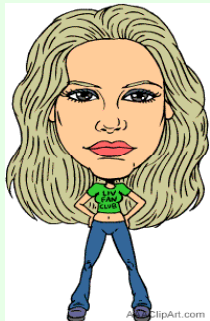
$$v(\text{server}) = 200$$



\$ 800

$$v(\text{monitor}) = 100$$

$$v(\text{laptop}) = 400$$



\$ 600

$$v(\text{laptop}) = 200$$

$$v(\text{server}, \text{monitor}) = 400$$



\$ 200



After trade (a more efficient outcome)

$$v(\text{server}) = 200$$

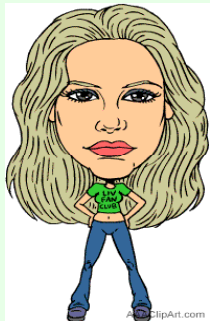


\$ 1100

... but how do we
get here?
Auctions?
Exchanges?
Unstructured trade?

$$v(\text{monitor}) = 100$$

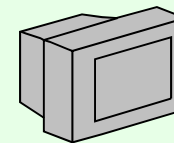
$$v(\text{laptop}) = 400$$



\$ 400

$$v(\text{laptop}) = 200$$

$$v(\text{server}, \text{monitor}) = 400$$



\$ 100



Some distinctions in economics

- **Descriptive** vs. **normative** economics
 - Descriptive:
 - seeks only to describe real-world economic phenomena
 - does not care if this is in any sense the “right” outcome
 - Normative:
 - studies how people “should” behave, what the “right” or “best” outcome is
- **Microeconomics** vs. **macroeconomics**
 - Microeconomics: analyzes decisions at the level of individual agents
 - deciding which goods to produce/consume, setting prices, ...
 - “bottom-up” approach
 - Macroeconomics: analyzes “the sum” of economic activity
 - interest rates, inflation, growth, unemployment, government spending, taxation, ...
 - “big picture”

What is Computer Science?

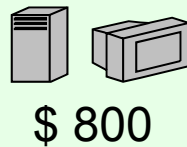
- “Computer science (abbreviated CS or CompSci) is the scientific and practical approach to computation and its applications. [...] A computer scientist specializes in the theory of computation and the design of computational systems.” [Wikipedia, Jan. 2014]
- A **computational problem** is given by a function f mapping inputs to outputs
 - For integer x , let $f(x) = 0$ if x is prime, 1 otherwise
 - For an initial allocation of resources x , let $f(x)$ be the (re)allocation that maximizes the sum of utilities
- An **algorithm** is a fully specified procedure for computing f
 - E.g., sieve of Eratosthenes
 - A **correct algorithm** always returns the **right** answer
 - An **efficient algorithm** returns the answer **fast**
- Computer science is also concerned with building **larger artifacts** out of these building blocks (e.g., personal computers, spreadsheets, the Internet, the Web, search engines, artificial intelligence, ...)

Resource allocation as a computational problem

input

$$v(\text{server, monitor}) = \$400$$

$$v(\text{laptop}) = \$600$$

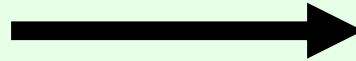


$$v(\text{server, monitor}) = \$500$$

$$v(\text{laptop}) = \$400$$



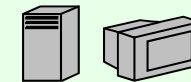
\$ 400



output



\$ 750



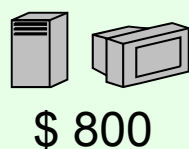
\$ 450

Here, gains from trade (\$300)
are divided evenly
(not essential)

Economic mechanisms

“true” input

$$v(\text{server, monitor}) = \$400$$
$$v(\text{laptop}) = \$600$$



\$ 800

$$v(\text{server, monitor}) = \$500$$
$$v(\text{laptop}) = \$400$$

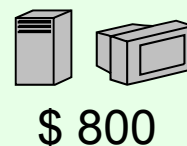


\$ 400

agent 1's
bidding
algorithm

agents' bids

$$v(\text{server, monitor}) = \$500$$
$$v(\text{laptop}) = \$501$$



\$ 800

$$v(\text{server, monitor}) = \$451$$
$$v(\text{laptop}) = \$450$$



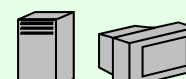
\$ 400

agent 2's
bidding
algorithm

exchange
mechanism
(algorithm)



\$ 800



\$ 400

*Exchange mechanism designer
does not have direct access to
agents' private information*

*Agents will selfishly respond to
incentives*

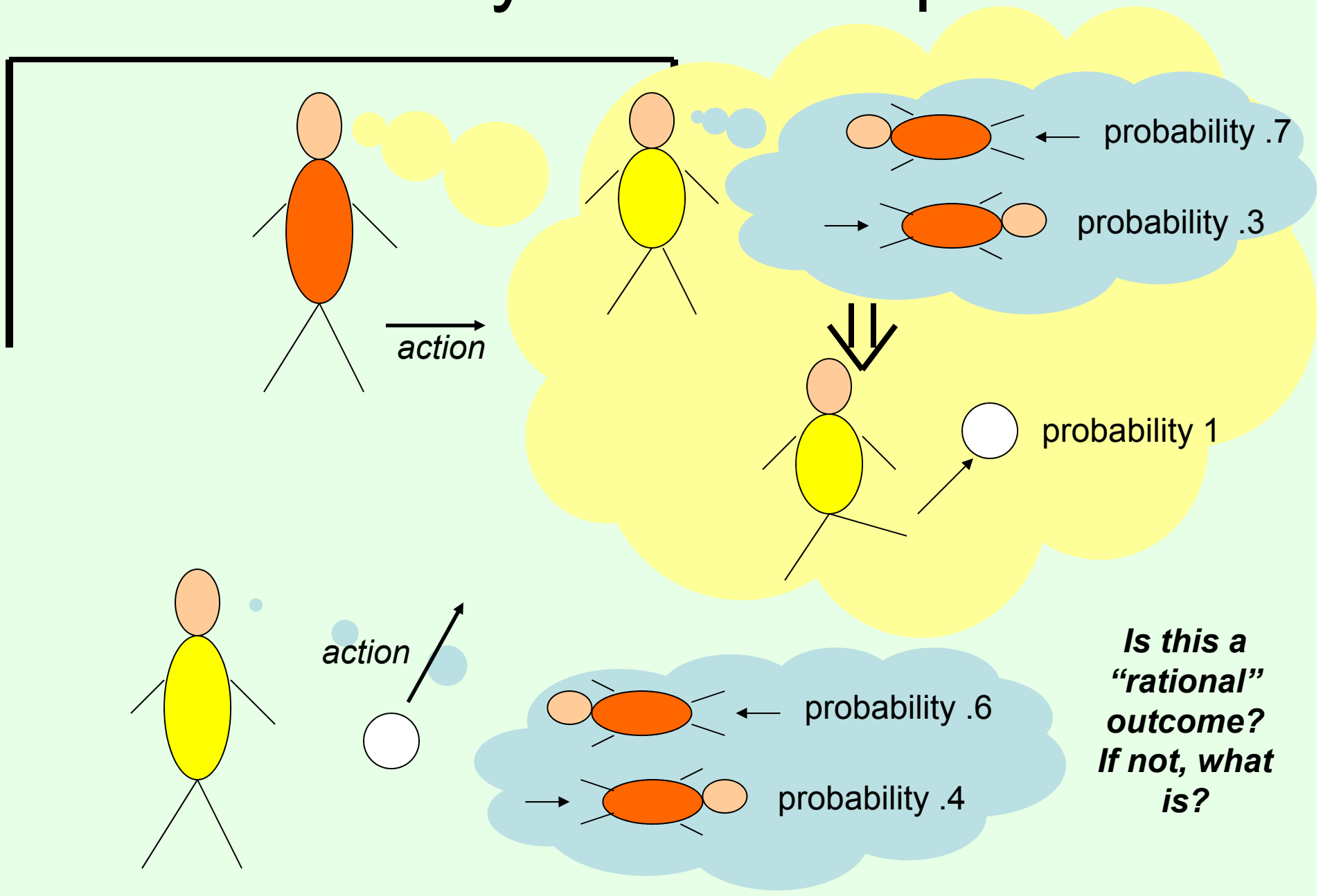
What is game theory?

- “Game theory is a study of strategic decision making. More formally, it is ‘the study of mathematical models of conflict and cooperation between intelligent rational decision-makers’ [...] Game theory is mainly used in economics, political science, and psychology, as well as logic and biology.” [[Wikipedia, Jan. 2014](#)]

What is game theory...

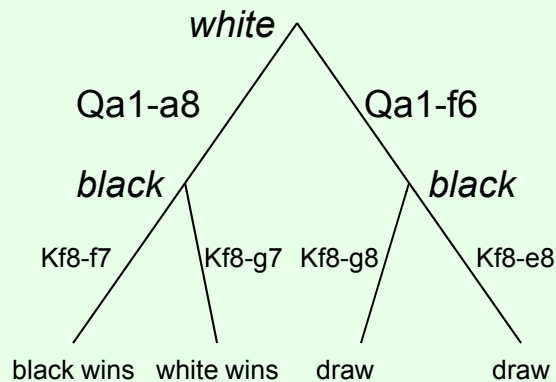
- Game theory studies settings where multiple parties (**agents**) each have
 - different preferences (utility functions),
 - different actions that they can take
- Each agent's utility (potentially) depends on all agents' actions
 - What is optimal for one agent depends on what other agents do
 - Very circular!
- Game theory studies how agents can rationally form **beliefs** over what other agents will do, and (hence) how agents should **act**
 - Useful for acting as well as predicting behavior of others

Penalty kick example



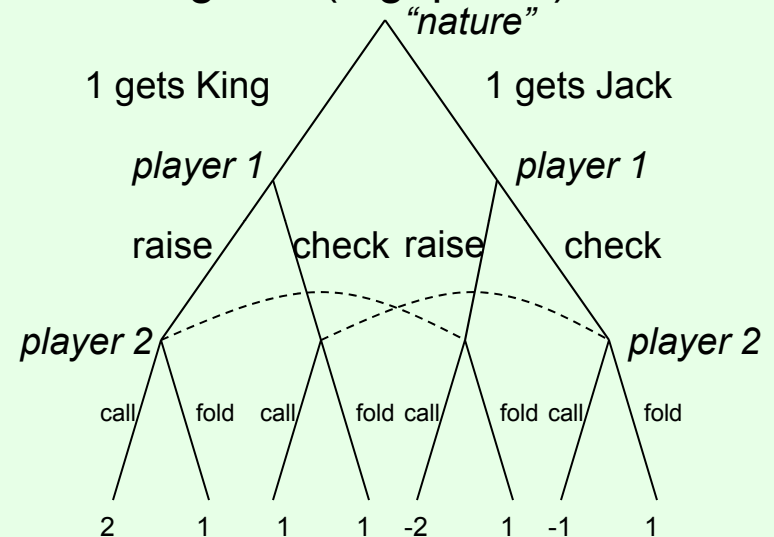
Game playing & AI

perfect information games:
no uncertainty about the
state of the game (e.g. tic-
tac-toe, chess, Go)



- Optimal play: value of each node = value of optimal child for current player (**backward induction**, minimax)
- For chess and Go, tree is too large
 - Use other techniques (heuristics, limited-depth search, alpha-beta, ...)
- Top computer programs (arguably) better than humans in chess, not yet in Go

imperfect information
games: uncertainty
about the state of the
game (e.g. poker)



- Player 2 **cannot distinguish** nodes connected by dotted lines
 - Backward induction fails; need more sophisticated game-theoretic techniques for optimal play
- Small poker variants can be solved optimally
- Humans still better than top computer programs at full-scale poker (at least most versions)
- Top computer (heads-up) poker players are based on techniques for game theory

Real-world security applications



Milind Tambe's TEAMCORE group (USC)

Airport security



- Where should checkpoints, canine units, etc. be deployed?
- Deployed at LAX and another US airport, being evaluated for deployment at all US airports

Federal Air Marshals

- Which flights get a FAM?



US Coast Guard

- Which patrol routes should be followed?
- Deployed in Boston Harbor



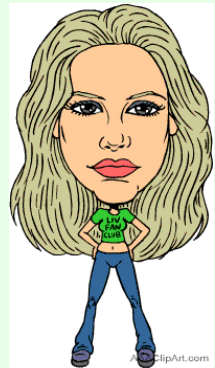
Questions and problems in (computational) game theory

- How should we **represent** games (=strategic settings)?
 - Standard game-theoretic representations not always concise enough
- What does it mean to **solve** a game?
 - **Solution concepts** from game theory, e.g., Nash equilibrium
- How **computationally hard** is it to solve games?
 - Can we solve them approximately?
- Is there a role for **(machine) learning** in games?
- What types of **modeling problems** do we face when addressing real-world games?
 - E.g., applications in security
- ...

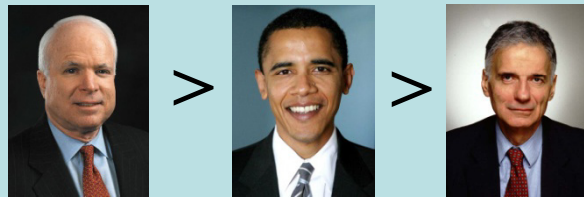
What is **social choice**?

- “Social choice theory or social choice is a theoretical framework for analysis of combining individual opinions, preferences, interests, or welfares to reach a collective decision or social welfare in some sense.” [\[Wikipedia, Jan. 2014\]](#)
- I.e., making decisions based on the preferences of multiple agents
- Largely, but not exclusively, focused on **voting**

Voting over outcomes

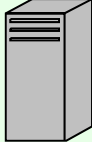
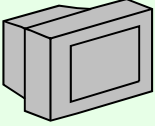


voting rule
(mechanism)
determines winner
based on votes



- Can vote over other things too
 - Where to go for dinner tonight, other joint plans, ...
- Many different rules exist for selecting the winner

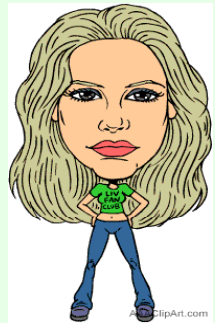
Combinatorial auctions

Simultaneously for sale:  ,  , 



bid 1

$$v(\text{server}, \text{cabinet}) = \$500$$



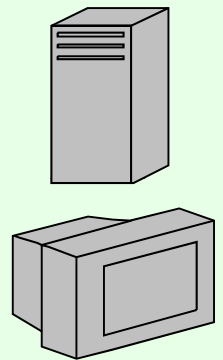
bid 2

$$v(\text{laptop}, \text{cabinet}) = \$700$$



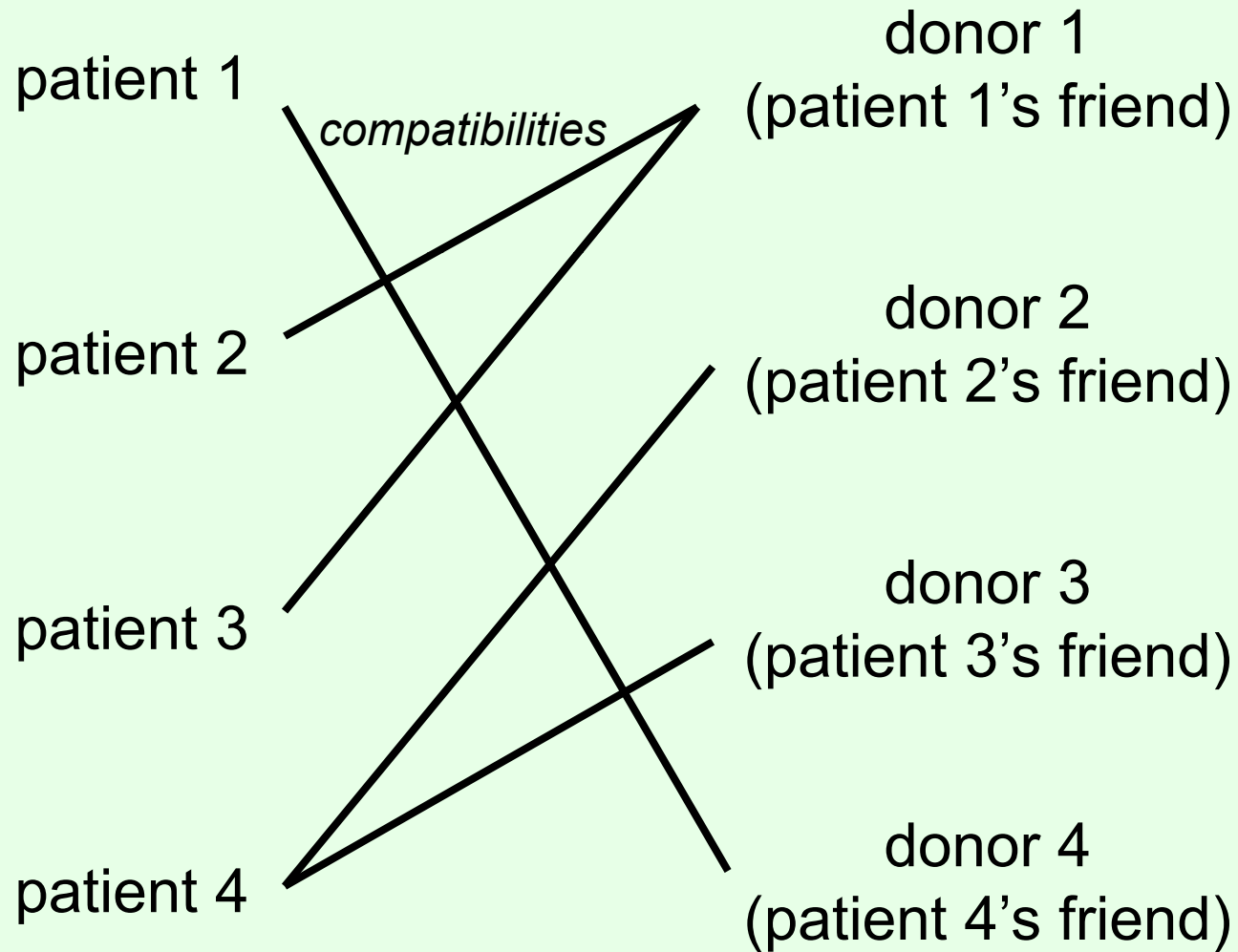
bid 3

$$v(\text{laptop}) = \$300$$



used in truckload transportation, industrial procurement, radio spectrum allocation, ...

Kidney exchange



Problems in computational social choice

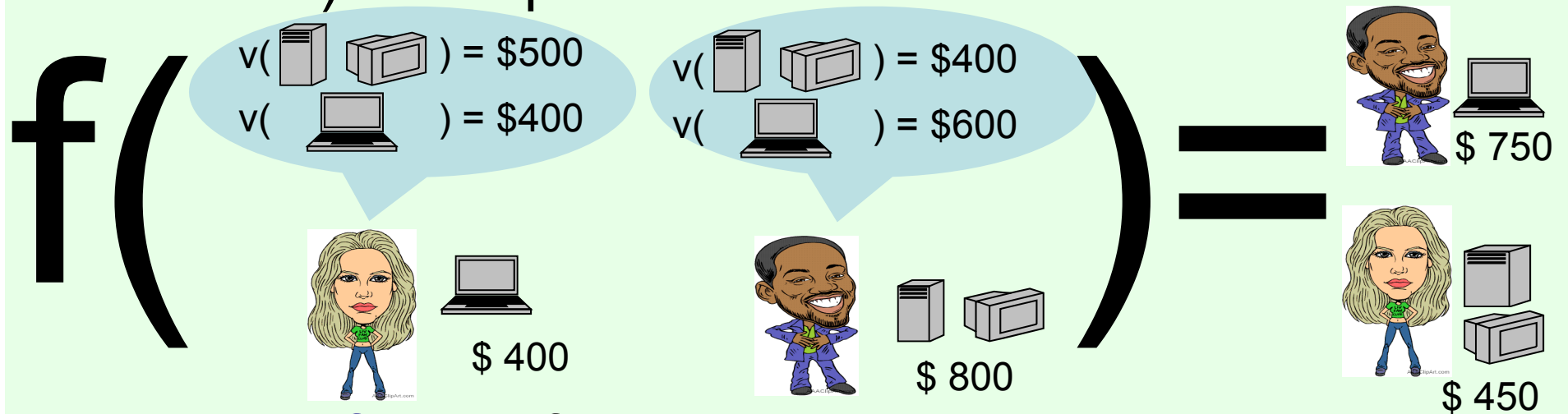
- **Winner determination** problem
 - For some voting rules, determining the winner is NP-hard
 - In a combinatorial auction, deciding which bids win is (in general) an NP-hard problem
- **Preference elicitation** (communication) problem
 - Can be impractical to communicate all of one's preferences (e.g., valuation for every bundle)
- **Mechanism design** problem
 - How do we get the bidders to behave so that we get good outcomes?
- These problems **interact** in nontrivial ways
 - E.g. limited computational or communication capacity can limit mechanism design options
 - ... but can perhaps also be used in a positive way

What is mechanism design?

- “[...] a field in game theory [...] The distinguishing features of [mechanism design] are:
 - that a game “designer” chooses the game structure rather than inheriting one
 - that the designer is interested in the game’s outcome
- “[...] usually solved by motivating agents to disclose their private information.” [\[Wikipedia, Jan. 2014\]](#)

Mechanism design...

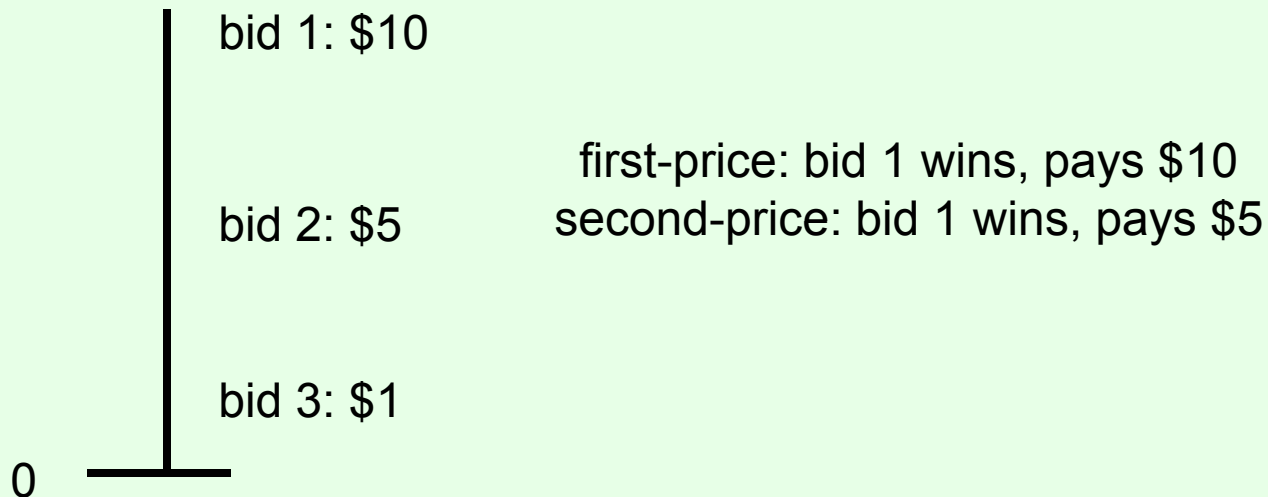
- **Mechanism** = rules of auction, exchange, ...
- A **function** that takes **reported preferences** (bids) as input, and produces **outcome** (allocation, payments to be made) as output



- The **entire function** f is **one** mechanism
- E.g., the mechanism from before: find allocation that maximizes (reported) utilities, distribute (reported) gains evenly
- Other mechanisms choose different allocations, payments

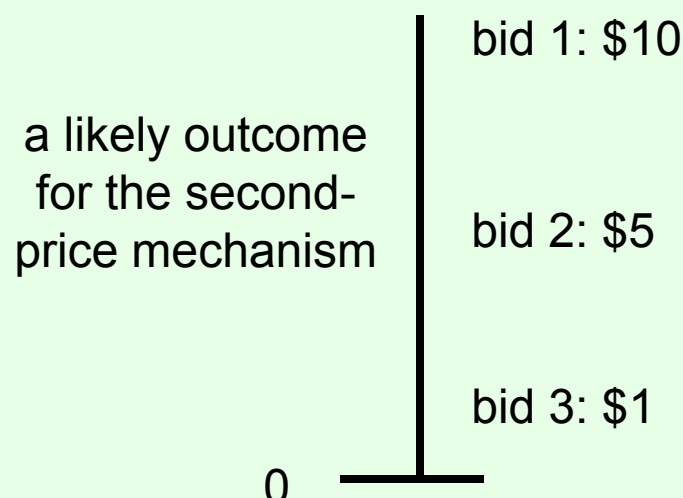
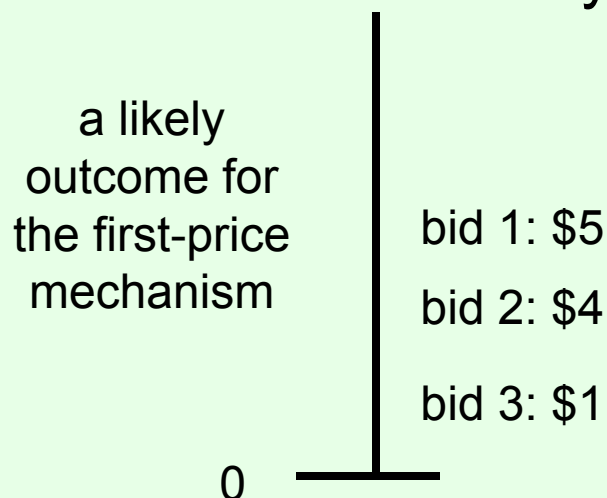
Example: (single-item) auctions

- **Sealed-bid** auction: every bidder submits bid in a sealed envelope
- **First-price** sealed-bid auction: highest bid wins, pays amount of own bid
- **Second-price** sealed-bid auction: highest bid wins, pays amount of second-highest bid



Which auction generates more revenue?

- Each bid depends on
 - bidder's **true valuation** for the item (utility = valuation - payment),
 - bidder's **beliefs** over what others will bid ($\rightarrow$ game theory),
 - and... the **auction mechanism** used
- In a first-price auction, it does not make sense to bid your true valuation
 - Even if you win, your utility will be 0...
- In a second-price auction, (we will see later that) it always makes sense to bid your true valuation



Are there other auctions that perform better? How do we know when we have found the best one?

Mechanism design...

- Mechanism = game
- → we can use game theory to predict what will happen under a mechanism
 - if agents act strategically
- When is a mechanism “good”?
 - Should it result in outcomes that are good for the **reported** preferences, or for the **true** preferences?
 - Should agents ever end up **lying** about their preferences (in the game-theoretic solution)?
 - Should it always **generate the best allocation**?
 - Should agents ever **burn money**?(!?)
- Can we solve for the optimal mechanism?

Many uses of linear programming, mixed integer (linear) programming in this course

	Linear programming	Mixed integer linear programming
Game theory	Dominated strategies Minimax strategies Correlated equilibrium Optimal mixed strategies to commit to	Nash equilibrium Optimal mixed strategies to commit to in more complex settings
Social choice, expressive marketplaces	Winner determination in auctions, exchanges, ... with partially acceptable bids	Winner determination in: auctions, exchanges, ... without partially acceptable bids; Kemeny, Slater, other voting rules; kidney exchange
Mechanism design	Automatically designing optimal mechanisms that use randomization	Automatically designing optimal mechanisms that do not use randomization

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[Algorithm for optimal winner determination in ...](#) - [Sandholm](#) - Cited by 755

[Combinatorial auctions](#) - [Cramton](#) - Cited by 364

[Taming the computational complexity of combinatorial ...](#) - [Fujishima](#) - Cited by 424

[Combinatorial auction](#) - Wikipedia, the free encyclopedia

Jun 26, 2009 ... A combinatorial auction is an auction in which bidders can place bids on combinations of items, or "packages," rather than just individual ...

en.wikipedia.org/wiki/Combinatorial_auction - [Cached](#) - [Similar](#)

[Introduction to Combinatorial Auctions](#)

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combinatorial auctions can be studied in a wide range of auction In Chapter 18, Leyton-Brown and Shoham present the Combinatorial Auction Test Suite ...

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A comprehensive book on combinatorial auctions—auctions in which bidders can bid on packages of items. The book consists of original material intended for ...

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of combinatorial auctions. Second, it uses this subject as a vehicle to the auction. This feature of combinatorial auctions is called the threshold ...

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[Combinatorial auctions enhance our ability to allocate mul-](#)

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Jun 17, 2003 ... combinatorial auction that, during laboratory testing, eliminated ... currently used by the FCC in the field, a combinatorial auction ...

[http://www.fcc.gov/.../combinatorial-auctions-enhance-our-ability-to-allocate-mul-...](#)

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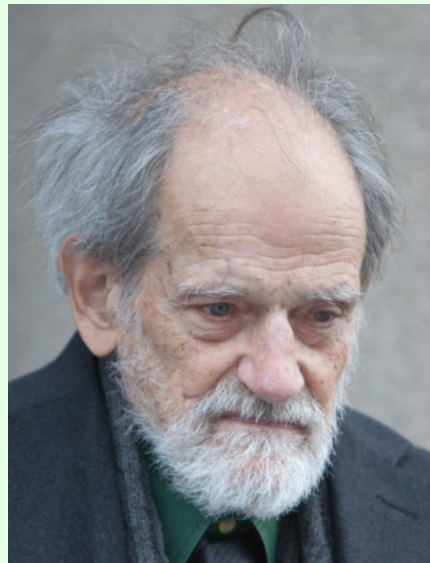
www.Amazon.com/Books

Deferred Acceptance algorithm

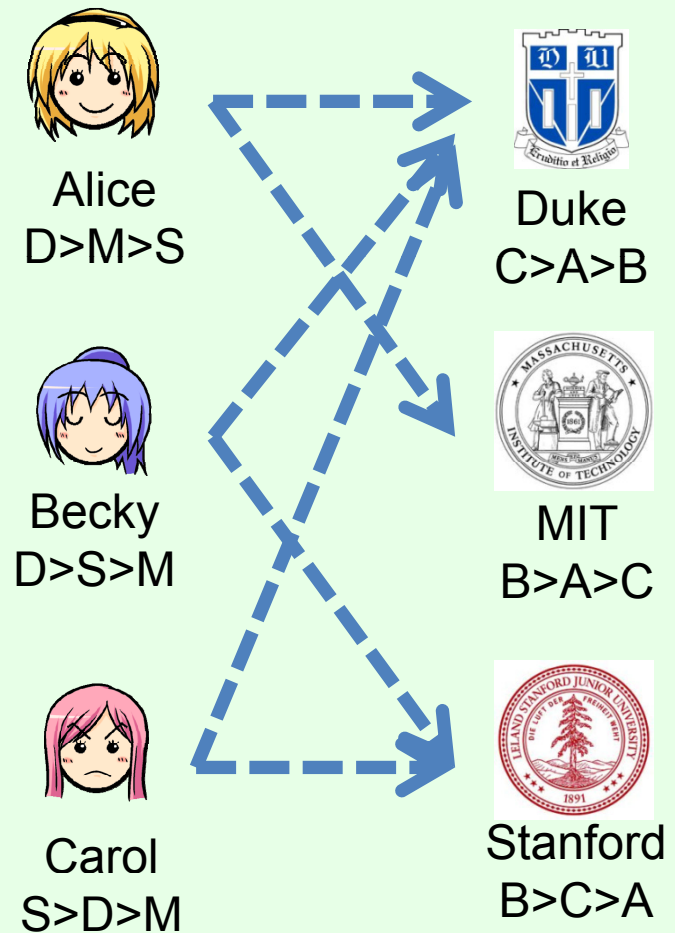
[Gale & Shapley 1962]



David Gale



Lloyd Shapley



Prediction markets

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Mitt Romney to win the 2012 South Carolina Primary

Last prediction was: **\$7.94** / share

Today's Change: ▲ **+\$0.22** (+2.8%)

79.4%
CHANCE

Event: [South Carolina Primary \(Republican\)](#)



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Step: **1. Buy or Sell** > 2. Select Price > 3. Review & Confirm

1. Choose to buy or sell shares in this market

Tip: Buy if you think it's going to happen, sell if you don't!

Think this event **will** occur?

Current best (lowest) price to buy shares is **\$7.94** / share. There are **4** shares available at this price.

Think this event **won't** occur?

Current best (highest) price to sell shares is **\$7.66** / share. There are **3** shares available at this price.

Tip: Yes, you can sell shares you don't own!

[Disclaimer](#)

Your Money

Available to spend: Not Logged In

Money currently invested: -

Financial securities

- Tomorrow there must be one of   
- Agent 1 offers \$5 for a security that pays off \$10 if  or 
- Agent 2 offers \$8 for a security that pays off \$10 if  or 
- Agent 3 offers \$6 for a security that pays off \$10 if 
- Can we accept some of these at offers **at no risk?**

How to incentivize a weather forecaster

$$P(\text{☀}) = .5$$

$$P(\text{☁}) = .3$$

$$P(\text{⚡}) = .2$$

$$P(\text{☀}) = .8$$

$$P(\text{☁}) = .1$$

$$P(\text{⚡}) = .1$$



- Forecaster's bonus can depend on
 - Prediction
 - Actual weather on predicted day
- Reporting true beliefs should maximize expected bonus

Why should economists care about computer science?

- Finding efficient allocations of resources is a (typically hard) **computational problem**
 - Sometimes beyond current computational techniques
 - If so, unlikely that **any** market mechanism will produce the efficient allocation (even without incentives issues)
 - Market mechanisms must be designed **with computational limitations in mind**
 - New algorithms allow new market mechanisms

Why should economists care about computer science...

- **Agents** also face difficult computational problems in participating in the market
 - Especially acting in a game-theoretically optimal way is often **computationally hard**
 - Game-theoretic predictions **will not come true** if they cannot be computed
 - Sometimes bad (e.g., want agents to find right bundle to trade)
 - Sometimes good (e.g., do not want agents to manipulate system)

Why should computer scientists care about economics?

- Economics provides high-value computational problems
- Interesting technical twist: **no direct access to true input**, must incentivize agents to reveal true input
- Conversely: Computer systems are increasingly used by **multiple parties** with different preferences (e.g., Internet)
- Economic techniques must be used to
 - **predict** what will happen in such systems,
 - **design** the systems so that they will work well
- Game theory is relevant for **artificial intelligence**
 - E.g., computer poker