

Unsupervised pattern discovery in human chromatin structure through genomic segmentation

Michael M Hoffman¹, Orion J Buske^{1,5}, Jie Wang², Zhiping Weng², Jeff A Billes³ & William Stafford Noble^{1,4}

We trained Segway, a dynamic Bayesian network method, simultaneously on chromatin data from multiple experiments, including positions of histone modifications, transcription-factor binding and open chromatin, all derived from a human chronic myeloid leukemia cell line. In an unsupervised fashion, we identified patterns associated with transcription start sites, gene ends, enhancers, transcriptional regulator CTCF-binding regions and repressed regions. Software and genome browser tracks are at <http://noble.gs.washington.edu/proj/segway/>.

Recently, the genomics community has seen an explosion in the availability of large-scale functional genomics data. Researchers have produced genome-wide data sets on the locations of transcription-factor binding, histone modifications, open chromatin and RNA transcription with sequence census assays that measure properties genome-wide by analyzing the location and count of sequenced tags. Consequently, our representation of the whole human genome has expanded from a sequence of nucleotides, occasionally annotated with discrete features, to a collection of numerical data tracks with values at almost every part of every chromosome. We will soon have access to data from dozens of cell types¹. How can we make sense out of this multitude of data?

A segmentation procedure provides a conceptually simple approach to finding patterns in genomic data^{2–7}. The segmentation task involves finding segment boundaries while simultaneously assigning labels to the segments. One partitions the genome into nonoverlapping contiguous segments, assigning one of a finite set of labels (such as ‘promoter’ or ‘enhancer’) to each, such that regions sharing the same segment label have in common certain properties in observed data. Occam’s razor implies the desirability

of making the set of segment labels as small as possible, while still retaining their capacity to accurately model the observations.

Because the label at one position is unknown but is influenced by the label at the previous position, a hidden Markov model (HMM) provides a natural solution for the segmentation task. Use of an HMM, however, has some limitations. For example, HMMs handle missing data poorly, requiring interpolation and smoothing to process regions where data are not reported. Similarly, hard or soft constraints on segment lengths prove complex and difficult to implement with a simple HMM.

Dynamic Bayesian networks (DBNs), in contrast, provide a powerful framework for modeling the complex hidden relationships that explain observed data sampled at regular intervals along some axis, such as physical positions on a genome. Automatic speech recognition researchers have long used DBNs⁸, and now scientists have started using them to solve biological problems⁹.

A DBN is a graphical structure that depicts the conditional independence properties of multiple random variables. We can represent a standard HMM by a DBN with a hidden random variable for the HMM’s hidden state and an observed random variable for the observations. With a DBN, however, we can easily incorporate complex relationships among variables at the current or nearby positions in the genome. The DBN therefore allows us to include multiple hidden variables and model their interrelationships without flattening them into a single state variable and thereby ignoring the properties implied by these interrelationships. For example, the DBN can incorporate a structured state space in which superlabels and sublabels augment a simple label set: the superlabel might represent a region of active euchromatin, and the sublabel might represent the 3’ end of an active gene in active euchromatin. In general, incorporating various types of prior knowledge and interpreting a trained model proves much easier with a DBN than with an HMM. For example, our model includes a principled mechanism for handling heterogeneous missing data. This mechanism is necessary because functional genomics assays may target only a subset of the genome or because repetitive sequences may lead to different patterns of missing data in different experiments (**Supplementary Discussion, Supplementary Fig. 1 and Supplementary Table 1**).

Here we describe a segmentation method, Segway, that uses DBN techniques to simultaneously segment and cluster genomic data. We describe the application of Segway to human chromatin immunoprecipitation sequencing (ChIP-seq), DNase I hypersensitive site sequencing (DNase-seq) and formaldehyde-assisted isolation of regulatory elements sequencing (FAIRE-seq) data from the Encyclopedia of DNA elements (ENCODE) Project¹.

¹Department of Genome Sciences, University of Washington, Seattle, Washington, USA. ²Program in Bioinformatics and Integrative Biology, University of Massachusetts Medical School, Worcester, Massachusetts, USA. ³Department of Electrical Engineering, University of Washington, Seattle, Washington, USA. ⁴Department of Computer Science and Engineering, University of Washington, Seattle, Washington, USA. ⁵Present address: Department of Computer Science, University of Toronto, Toronto, Ontario, Canada. Correspondence should be addressed to W.S.N. (william-noble@uw.edu).

suggestions, and members of the ENCODE Project Consortium, the ENCODE Data Coordination Center and the US National Human Genome Research Institute for providing early public access to the unpublished data used in this work. This work used data produced in the laboratories of B.E. Bernstein (Broad Institute of the Massachusetts Institute of Technology and Harvard University), M.P. Snyder (Stanford University), R.M. Myers (HudsonAlpha Institute for Biotechnology), P.J. Farnham (University of Southern California), V.R. Iyer (University of Texas at Austin), G.E. Crawford (Duke University), J.D. Lieb and T.S. Furey (University of North Carolina at Chapel Hill), J.A. Stamatoyannopoulos (University of Washington), P. Carninci (RIKEN), T.R. Gingeras (Cold Spring Harbor Laboratory), and A. Sidow (Stanford University). This publication was made possible by grants 004695, 004561 and 006259 from National Human Genome Research Institute.

AUTHOR CONTRIBUTIONS

M.M.H., W.S.N. and J.A.B. conceived of the project; M.M.H., W.S.N. and Z.W. designed computational and biological experiments. M.M.H., J.A.B., O.J.B. and J.W. developed software used in this work; M.M.H., O.J.B. and J.W. conducted computational experiments and analyzed data; and M.M.H., W.S.N., Z.W., J.A.B., O.J.B. and J.W. wrote the manuscript.

COMPETING FINANCIAL INTERESTS

The authors declare no competing financial interests.

Published online at <http://www.nature.com/naturemethods/>.

Reprints and permissions information is available online at <http://www.nature.com/reprints/index.html>.

1. ENCODE Project Consortium. *PLoS Biol.* **9**, e1001046 (2011).
2. Day, N., Hemmaplardh, A., Thurman, R.E., Stamatoyannopoulos, J.A. & Noble, W.S. *Bioinformatics* **23**, 1424–1426 (2007).
3. Erdman, C. & Emerson, J.W. *Bioinformatics* **24**, 2143–2148 (2008).
4. Jaschek, R. & Tanay, A. in *Research in Computational Molecular Biology, Lecture Notes in Computer Science* Vol. 5541 (ed. Batzoglou, S.) 170–183 (Springer, Berlin, 2009).
5. Ernst, J. & Kellis, M. *Nat. Biotechnol.* **28**, 817–825 (2010).
6. Filion, G.J. *et al. Cell* **143**, 212–224 (2010).
7. Kharchenko, P.V. *et al. Nature* **471**, 480–485 (2011).
8. Bilmes, J. & Bartels, C. *IEEE Signal Process. Mag.* **22**, 89–100 (2005).
9. Reynolds, S.M., Käll, L., Riffle, M.E., Bilmes, J.A. & Noble, W.S. *PLoS Comput. Biol.* **4**, e1000213 (2008).
10. Wang, Z., Schones, D.E. & Zhao, K. *Curr. Opin. Genet. Dev.* **19**, 127–134 (2009).
11. Hon, G., Ren, B. & Wang, W. *PLoS Comput. Biol.* **4**, e1000201 (2008).

ONLINE METHODS

Signal generation. We selected data from 31 ChIP-seq, DNase-seq and FAIRE-seq assays carried out in the chronic myeloid leukemia cell line K562 by the ENCODE Project¹. We downloaded tagAlign files from the ENCODE Data Coordination Center¹² (**Supplementary Table 4**). We used Wiggler (<http://code.google.com/p/align2rawsignal/>) to convert tag alignment positions into an extended reads per base signal for each position of the genome, pooling multiple replicates when available. We then loaded the signal data into a Genomdata¹³ archive. We include the URL for each of the tagAlign and signal files used in **Supplementary Table 3**.

Signal transformation. To reduce the distorting effects of high data values in sequence census assay data, Segway first transforms all data values with the inverse hyperbolic sine function $\text{asinh } x = \ln(x + \sqrt{x^2 + 1})$. This function has the compressing effect of a function like $\ln x$ for large values of x but has much less of a compressing effect for small values. Additionally, it is defined on the entire real number line, preserving the input data values as positive or negative. One therefore avoids the discontinuities inherent in the use of a simple logarithmic transformation and the necessity of first adding some offset to deal with zero values¹⁴.

The core model. Segway carries out training and inference on a DBN model designed for genomic segmentation (**Supplementary Fig. 11**). The core of the default Segway DBN has some similarity to an HMM, with multiple observation tracks and a number of discrete hidden variables. The default Segway DBN has a segment label backbone defined for each base pair of a genomic region. This hidden variable emits an observation variable for each observation track present at that position. An observation track is a sequence of numerical observations, such as the number of sequence tags overlapping successive genomic positions, or the intensity of a microarray probe associated with a position. In the default model, the i th observation track is represented by the sequence of random variables $X_{1:T}^{(i)} = (X_1^{(i)}, \dots, X_T^{(i)})$. Some positions t may not correspond to a defined value of $X_t^{(i)}$. Examples include unmappable sequence in sequence census assays, or sequence not represented by a probe in a microarray assay. To explicitly model these missing data, we use an indicator variable to mark whether $X_t^{(i)}$ is defined ($\hat{X}_t^{(i)} = 1$) or undefined ($\hat{X}_t^{(i)} = 0$). The observation variables at every position have dependency only on the hidden segment label variable at that position Q_t (**Supplementary Fig. 11**). When the indicator variable ($\hat{X}_t^{(i)} = 0$), then $X_t^{(i)}$ does not have a dependence on Q_t . In that case, the conditional parent arc from Q_t to $X_t^{(i)}$ is, for all intents and purposes, nonexistent in the DBN¹⁵. Segway models the asinh-transformed data with an $m \times n$ matrix of scalar Gaussians, with one Gaussian for each combination of n observation tracks and m segment labels. Each Gaussian has a mean parameter μ , and variance parameter σ^2 , which control the signal distribution that the Gaussian emits. Segway ties variance parameters such that they are all equal for a given observation track.

Weighting. Segway weights the contribution of each observation variable such that tracks with different numbers of data points still have roughly the same contribution to the overall likelihood of the model. It does this by exponentiating during inference calculations

every occurrence of an original probability $P(X_t^{(i)} | Q_t)$ for some track i by the number of data points for that track $N^{(i)} = \sum_t \hat{X}_t^{(i)}$ divided by the maximum number of data points for any particular track $N^* = \max_j N^{(j)}$. In other words, it replaces the original probability with a new probability:

$$P'(X_t^{(i)} | Q_t) = (P(X_t^{(i)} | Q_t))^{\frac{N^{(i)}}{N^*}}$$

Because probabilities are always in the range [0, 1], an increase in weight will result in a decreased probability of the model overall, but when the weight is held constant, changes in the probabilities exponentiated to higher weights will affect the overall probability more than those exponentiated to lower weights.

The duration model. The Segway model includes additional random variables that allow tuning beyond the simple HMM-like core model. A discrete countdown variable C_t allows the specification of minimum or maximum segment length. This variable begins with an initial value dependent on Q_p , and decreases by 1 at every position where the ruler marker variable M_t is 1 ('ruler marks'). Decreasing the countdown variable only upon the occurrence of an occasional ruler mark decreases the countdown variable state space while still allowing longer minimum or maximum segment lengths. This heuristic greatly decreases computational complexity. A binary segment transition variable J_t can either force the segment label to change at the current position ($J_t = 1$), or prevent it from changing ($J_t = 0$). Segway generates a conditional probability table $P(J_t = 1 | Q_{t-1}, C_{t-1})$ that maps each (Q_{t-1}, C_{t-1}) tuple to one of three rules that determine the value of J_t : (i) force, $P(J_t = 1) = 1$; (ii) prevent, $P(J_t = 0) = 1$; or (iii) allow, $P(J_t = 1) = 1/(1 + L)$. The duration in which the segment label is unchanged following the point where the 'allow' rule becomes active follows a geometric distribution with an expected length of the L value^{9,16}. In this study, we set $C_t = 10$ and the 'force' rule at the beginning of each segment. We also set the ruler marker every ten positions. This setting allows the enforcement of large minimum segment lengths with only a small increase in state space and computational complexity. When C_t decreases to 0, we set the 'allow' rule with $L = 100,000$ to model broader behavior when the observation variables do not control the segment label as they usually do. Despite the enforcement of a minimum duration before allowing a change in segment label, it is still possible to have very short segments at the end of input sequences, such as at the 3' ends of genome assembly scaffolds.

DBN inference. Segway uses the graphical models toolkit (GMTK)¹⁷ to do expectation-maximization training¹⁸ and Viterbi decoding¹⁹ on the Segway models. Segway uses model structure files in the GMTKL specification language, and users may modify them or replace them with a DBN of arbitrary complexity. For decoding, Segway divides large sequences into nonoverlapping windows of no more than 2 Mb in size each so that the necessary computation can fit into available memory.

Training and parameters. We carried out ten separate instances of expectation-maximization training, each with different initial parameters, and each instance had no more than 100 iterations. Segway picks an initial mean parameter μ for each track

uniformly from the values in $\tilde{\mu} \pm 0.2 \tilde{\sigma}$ for the empirical mean $\tilde{\mu}$ and s.d. $\tilde{\sigma}$ of the training data. It sets variance parameters σ^2 to the difference between the maximum and minimum data values within a particular observation track. We did training on the ENCODE pilot regions (<http://hgdownload.cse.ucsc.edu/goldenPath/hg18/database/encodeRegions.txt.gz>), which represent 1% of the human genome (30 Mb). Segway sets the probabilities $P(Q_1 = q)$ of starting a sequence with each segment label $q \in [1, n]$ to $1/n$, and does not adjust these probabilities during training. The conditional probability table $P(Q_t | Q_{t-1})$, which Segway only uses when the segment transition variable $J_t = 1$, has only zeroes in its diagonal. This prevents a ‘transition’ that does not change the segment label. Segway initially sets the other values equally, but expectation-maximization training will adjust them. A training instance continues until the difference between the difference between the current likelihood L_n and the likelihood from the previous round L_{n-1} diminishes such that:

$$\left| \frac{\log L_n - \log L_{n-1}}{\log L_{n-1}} \right| < 10^{-5}$$

We designated the training instance with the highest final likelihood as the winning training instance and used its parameters to create the primary segmentation discussed here.

Segment identification and visualization. We carried out Viterbi decoding on 92% of the genome (2,828 Mb), excepting excluded blacklist regions downloaded from the ENCODE Data Coordination Center¹² (<http://hgdownload.cse.ucsc.edu/goldenPath/hg18/encodeDCC/wgEncodeMapability/wgEncodeDukeRegionsExcluded.bed6.gz>). These regions contain repetitive elements that cause artifactually high signal in sequence census assays. We created the primary segmentation discussed here with the winning training instance parameters but did Viterbi decoding with parameters from the other nine training instances for comparison purposes. Segway produces segmentations in BED format, designed for easy uploading and display on the UCSC Genome Browser²⁰.

Distributed computing. Segway uses the Grid Engine or Platform LSF distributed computing systems through the Distributed Resource Management Application API (<http://www.drmaa.org/>) interface. Using these systems, Segway trains or decodes on multiple sequences and multiple initial parameter values at once, leading to a considerable savings in wall clock time. Segway automatically tunes memory usage by first queuing jobs with a small amount of memory (such as 2 gigabytes) and then repeating with ever larger amounts of memory if GMTK cannot complete inference with the smaller amount. This approach allows efficient resource management even when one cannot easily predict the memory usage in advance.

Genome assembly and annotations. We did all training, segmentation, and analysis on the NCBI36 assembly of the human genome (hg18). We used GENCODE²¹ version 3c gene annotations (<http://www.encodegenes.org/releases/3c.html>) for aggregation and overlap analyses, as well as track display. We used ENCODE Project CAGE²² data (ftp://genome.crg.es/pub/Encode/data_analysis/TSS/Mar-July2010/Genocodev3c_TSS.gff) for overlap analyses. We downloaded PhastCons scores for multiple alignments of 45 vertebrates

to the human genome²³ from the UCSC Genome Browser. We downloaded nucleosome positioning signal data collected in K562 by micrococcal nuclease digestion and high-depth sequencing from the UCSC Genome Browser (<http://genome.ucsc.edu/cgi-bin/hgFileUi?db=hg19&g=wgEncodeSydhNsosome>). We produced genome-wide visualizations and summary statistics using Segtools²⁴. We based precision and recall statistics on the overlap of the bases within a segment against some annotation, where true positives (TP) are positions where the segment label overlaps the annotation, false positives (FP) are positions where the segment label does not overlap the annotation, and false negatives (FN) are positions where the annotation does not overlap the segment label. We expanded point annotations (such as TSSs) by 500 bp on each side before calculating these statistics. Precision (also known as positive predictive value) is defined as $TP/(TP + FP)$. Recall (also known as sensitivity) is defined as $TP/(TP + FN)$. We used precision and recall for evaluation instead of receiver operating characteristic curves, because precision and recall can provide a more informative measurement of performance²⁵. We defined TSSs with reproducible CAGE support as those with at least two cytoplasmic CAGE tags.

Transient transfection luciferase assays. We predicted the promoter activity of sequences in the segmentation selected by the following procedure. We started with the segments that overlapped both GENCODE manually annotated protein-coding TSSs and a catalog of existing constructs from SwitchGear Genomics. We then excluded the segments that overlapped RepeatMasker 3.27 regions downloaded from the UCSC Genome Browser (<http://hgdownload.cse.ucsc.edu/goldenPath/hg18/database/>). We defined positive predictions as those segments with a TSS label that overlapped a GENCODE TSS with at least two K562 cytosolic poly(A)⁺ CAGE tags and a GENCODE TSS for a gene with at least K562 RNA-seq reads per kilobase per million reads (RPKM) above the 90th percentile. We defined negative predictions as those segments with R labels that overlapped a GENCODE TSS with no CAGE tags in any K562 cellular compartment, and a GENCODE TSS for a gene with 0.0 RPKM K562 RNA-seq reads. We further divided negative predictions by whether they had GM12878 RNA-seq read RPKM over the 10th percentile or not. This process resulted in a candidate set of 26 positive predictions and 74 negative predictions. SwitchGear Genomics did transient transfection luciferase assays in triplicate on 24 positive predictions, 67 negative predictions, and 5 control constructs, narrowing from the candidate set on the basis of constructs in stock. They mixed 100 ng luciferase reporter DNA, 0.4 μ m Lipofectamine LTX (Invitrogen), and 0.1 μ l PLUS Reagent (Invitrogen), and incubated it for 30 min. SwitchGear then thoroughly mixed this suspension with 25,000 freshly counted K562 cells resuspended in warm, complete media. They dispensed 100 μ l of the combined suspension into replicate white 96-well assay plates and incubated them at 37 °C for 24 h. They then removed the plates from the incubator, added SteadyGlo reagent (Promega) to each well, and kept the plates in the dark for >30 min. They then read the plates on an LmaxII-384 luminometer (Molecular Devices). We considered the resulting data points substantial when their activity exceeded a threshold of the mean control activity plus six times the s.d. of control activity.

Gene Ontology enrichment analysis. We analyzed the sets of GENCODE TSSs that overlapped with each segment label for

the enrichment of GO terms. We used the Ensembl²⁶ Perl API to convert GENCODE transcript identifiers to UniProt²⁷ identifiers. We then used FuncAssociate²⁸ to find enrichment in 25 resulting gene sets, using 10,000 resamplings for each to determine hypothesis-wise *P* values. We then multiplied these *P* values by 25 as a Bonferroni correction for testing multiple hypotheses.

Transcription factor motif analysis. We obtained position specific scoring matrices (PSSMs) from the TRANSFAC 10.2 (ref. 29) and JASPAR CORE 2009 (ref. 30) databases. Using FIMO³¹, we scanned the human genome for significant matches to the PSSM ($q < 0.1$). From these candidate motifs, we selected known vertebrate *cis*-regulatory motifs with at least 1,000 significant matches in the genome. We used the genome structure correction marginal region overlap test in block_bootstrap³², as implemented in Statmap (<http://www.statmap-bio.org/>), to test each segment label for enrichment in matches to each of the selected motifs. We then applied the Bonferroni correction to the resulting *P* values.

Statistical analysis. We carried out statistical analysis with R 2.11 (<http://www.rproject.org/>).

12. Raney, B.J. *et al. Nucleic Acids Res.* **39**, D871–D875 (2011).
13. Hoffman, M.M., Buske, O.J. & Noble, W.S. *Bioinformatics* **26**, 1458–1459 (2010).

14. Johnson, N.L. *Biometrika* **36**, 149–176 (1949).
15. Bilmes, J. in *UAI '00: Proceedings of the 16th Conference on Uncertainty in Artificial Intelligence* (eds. Boutilier, C. & Goldszmidt, M.) 38–45 (Morgan Kaufmann, San Francisco, 2000).
16. Grundy, W.N., Bailey, T.L., Elkan, C.P. & Baker, M.E. *Comput. Appl. Biosci.* **13**, 397–406 (1997).
17. Bilmes, J. & Bartels, C. in *UAI '03, Proceedings of the 19th Conference in Uncertainty in Artificial Intelligence* (eds. Meek, C. & Kjærulff, U.) 47–56 (Morgan Kaufmann Publishers, San Francisco, 2003).
18. Dempster, A.P., Laird, N.M. & Rubin, D.B. *J. Royal Stat. Soc. B* **39**, 1–22 (1977).
19. Viterbi, A.J. *IEEE Trans. Inf. Theory* **13**, 260–269 (1967).
20. Fujita, P.A. *et al. Nucleic Acids Res.* **39**, D876–D882 (2011).
21. Harrow, J. *et al. Genome Biol.* **7**, S4.1–S4.9 (2006).
22. Takahashi, H., Kato, S., Murata, M. & Carninci, P. *Methods Mol. Biol.* **786**, 181–200 (2012).
23. Siepel, A. *et al. Genome Res.* **15**, 1034–1050 (2005).
24. Buske, O.J., Hoffman, M.M., Ponts, N., Roch, K.G.L. & Noble, W.S. *BMC Bioinformatics* **12**, 415 (2011).
25. Davis, J. & Goadrich, M. in *Proceedings of the 23rd International Conference on Machine Learning* 233–240 (ACM, New York, 2006).
26. Flicek, P. *et al. Nucleic Acids Res.* **39**, D800–D806 (2011).
27. UniProt Consortium. *Nucleic Acids Res.* **39**, D214–D219 (2011).
28. Berriz, G.F., Beaver, J.E., Cenik, C., Tasan, M. & Roth, F.P. *Bioinformatics* **25**, 3043–3044 (2009).
29. Wingender, E. *et al. Nucleic Acids Res.* **28**, 316–319 (2000).
30. Sandelin, A., Alkema, W., Engstrom, P., Wasserman, W. & Lenhard, B. *Nucleic Acids Res.* **32**, D91–D94 (2004).
31. Grant, C.E., Bailey, T.L. & Noble, W.S. *Bioinformatics* **27**, 1017–1018 (2011).
32. Bickel, P.J., Boley, N., Brown, J.B., Huang, H. & Zhang, N.R. *Ann. Appl. Stat.* **4**, 1660–1697 (2010).