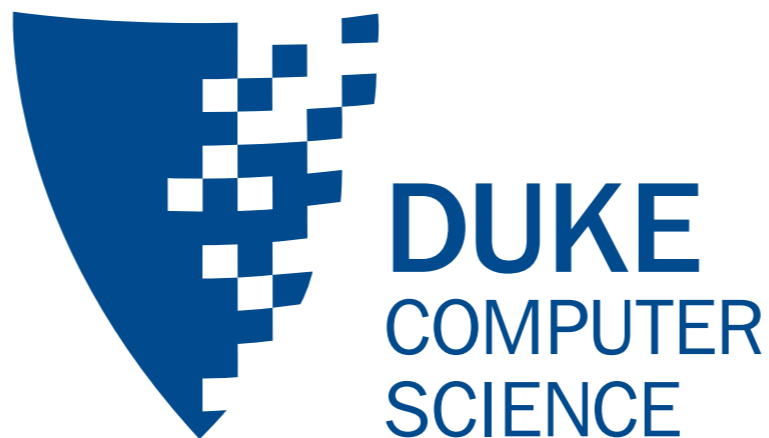


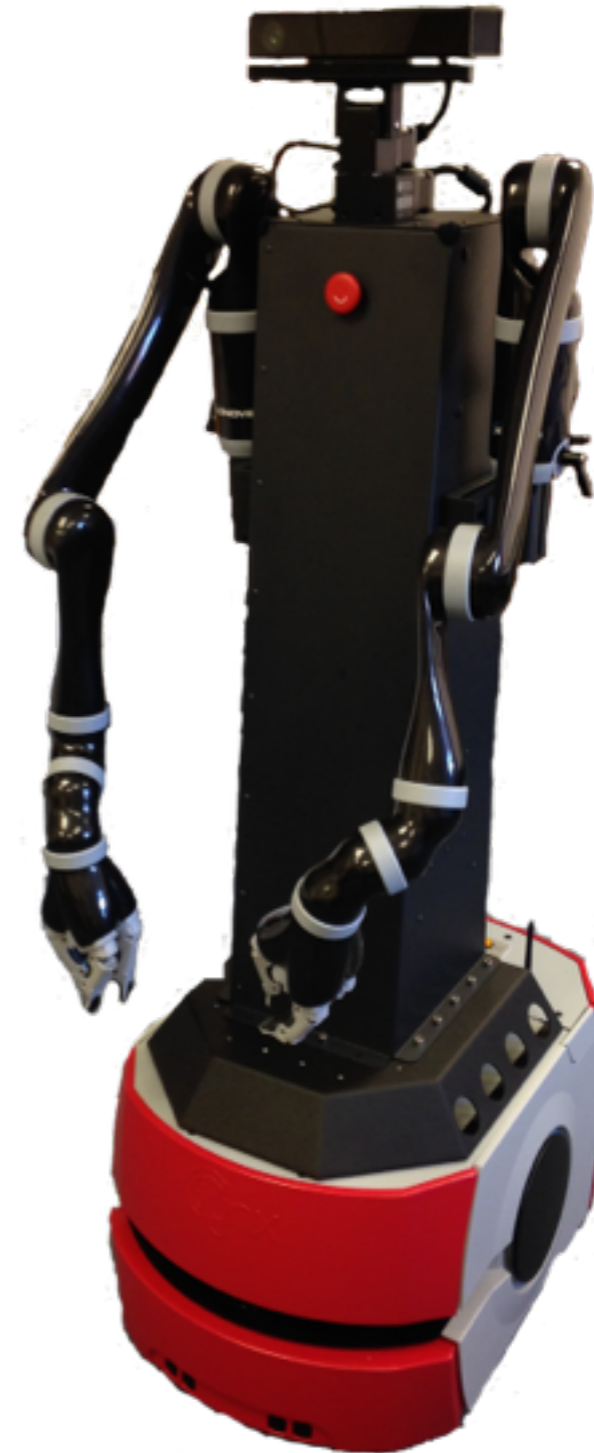
# Robot Motion Planning

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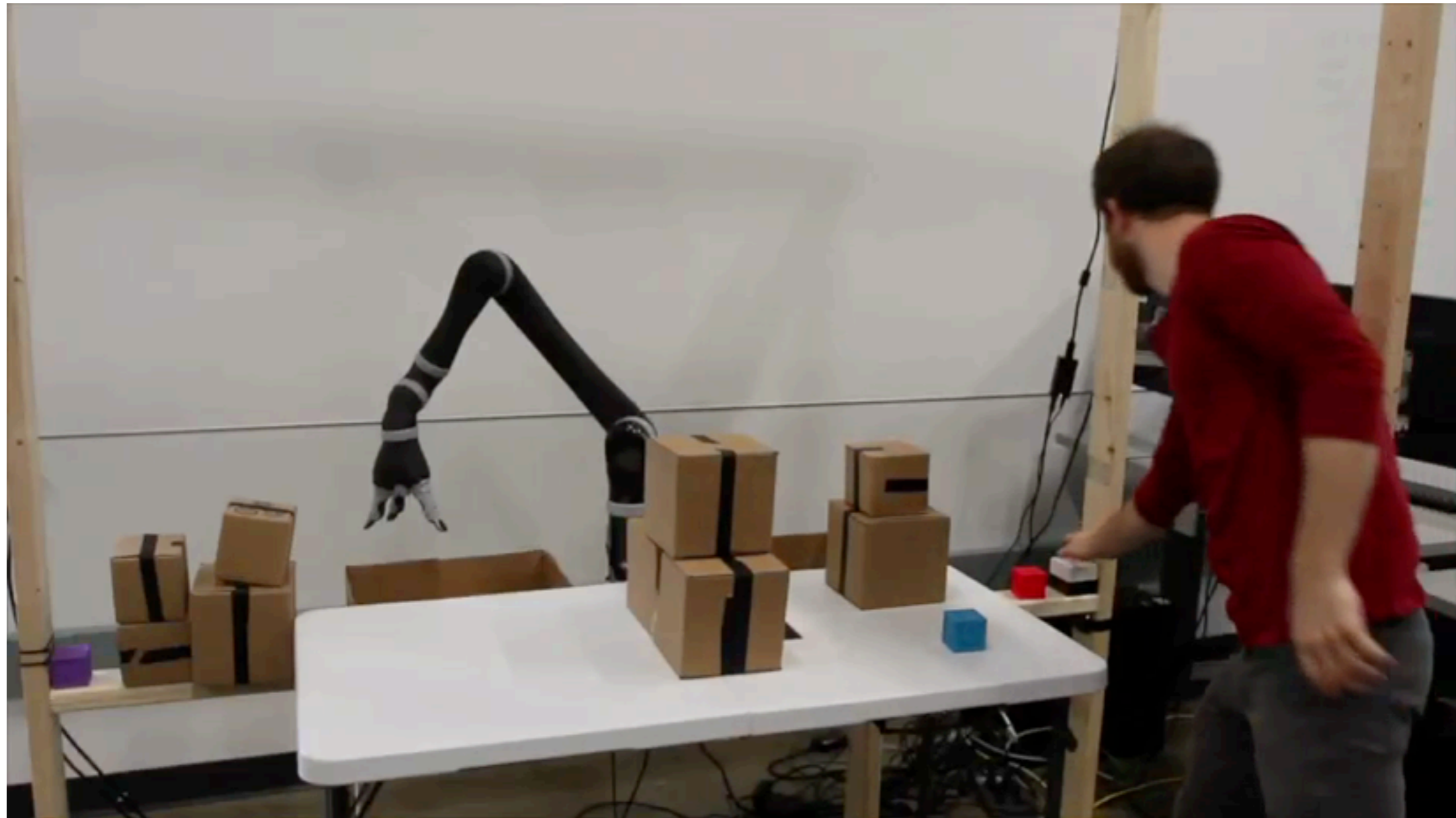


**Spring 2016**

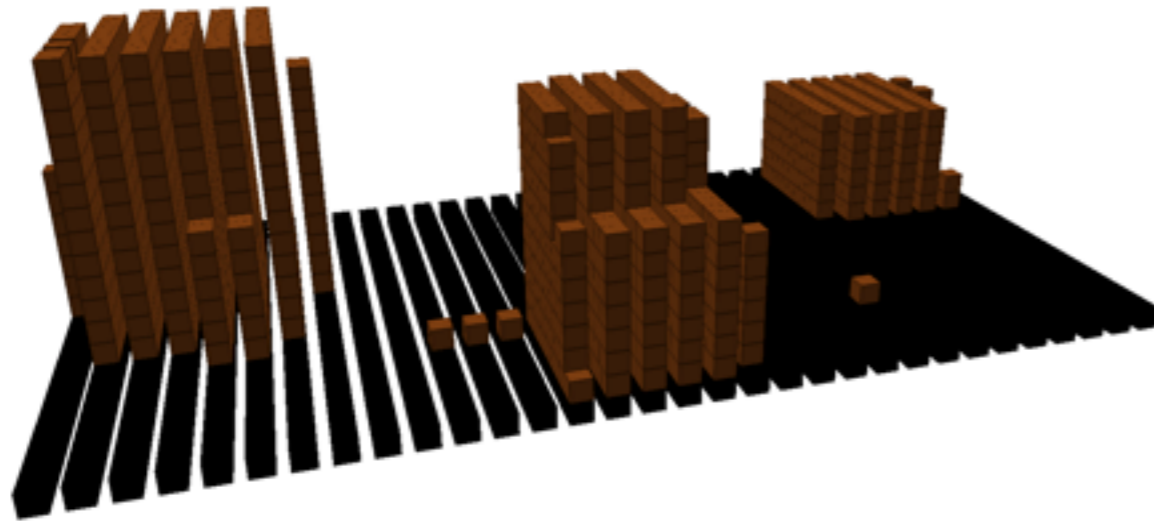
# Robot Motion Planning



# Motion Planning



# Motion Planning



# Problem Definition

Robot has a **configuration space (C-space)**

- Values for each joint
- Overall pose of reference frame

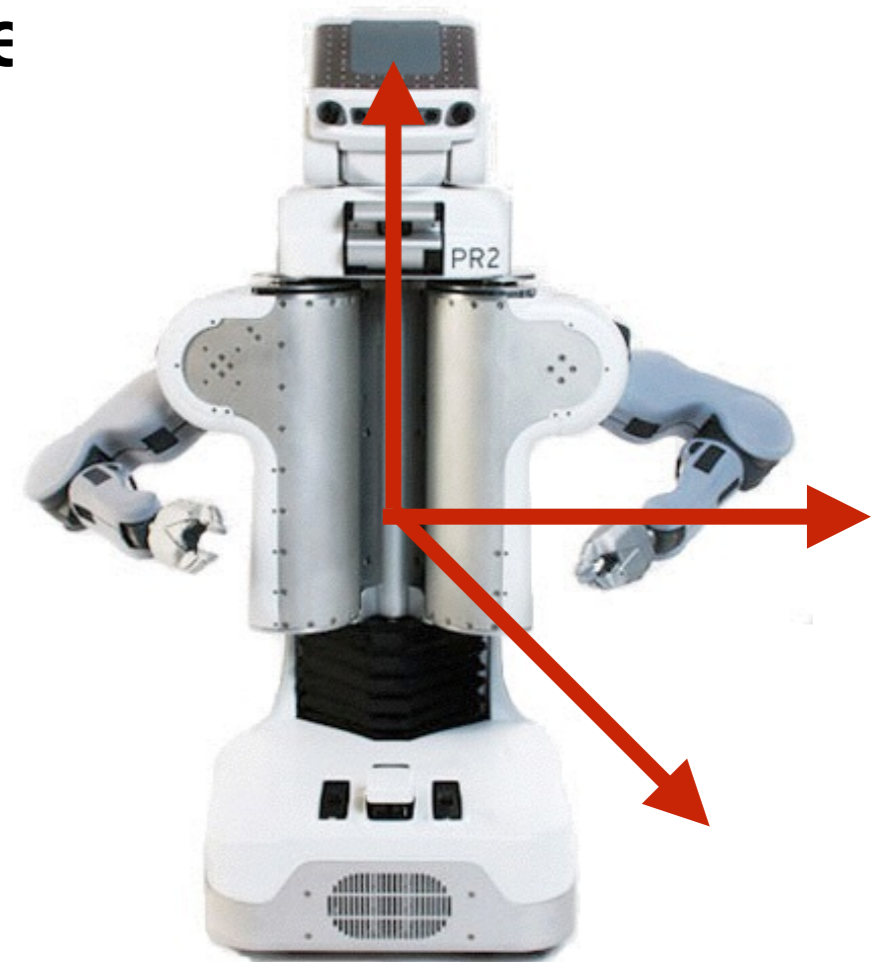
Start and end points

- Start point
- Goal region

Set of obstacles

- Dense regions of 3D-space (*Also regions of C-space*)

**Objective:** obstacle-free path through configuration space from start to goal.



# Configuration Spaces

Each joint is a *dimension* of the configuration space.

Let's say we have a robot with an arm with two revolute joints.

Configuration space:

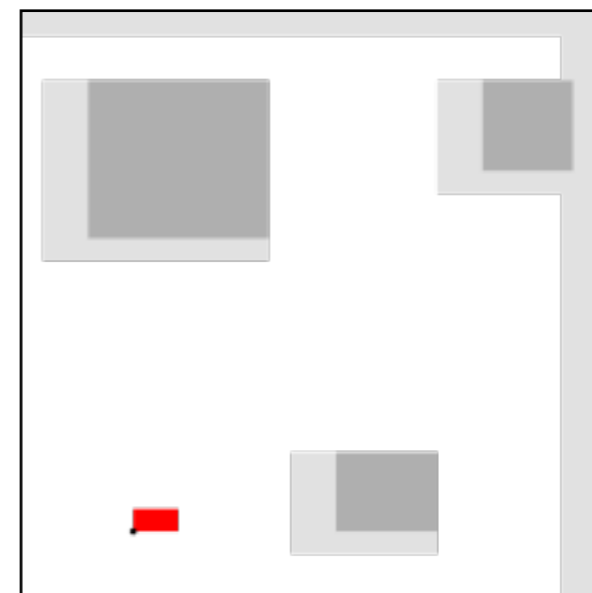
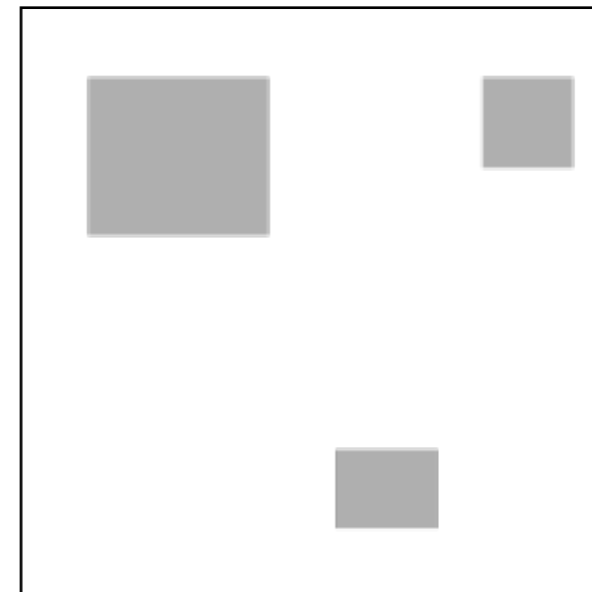
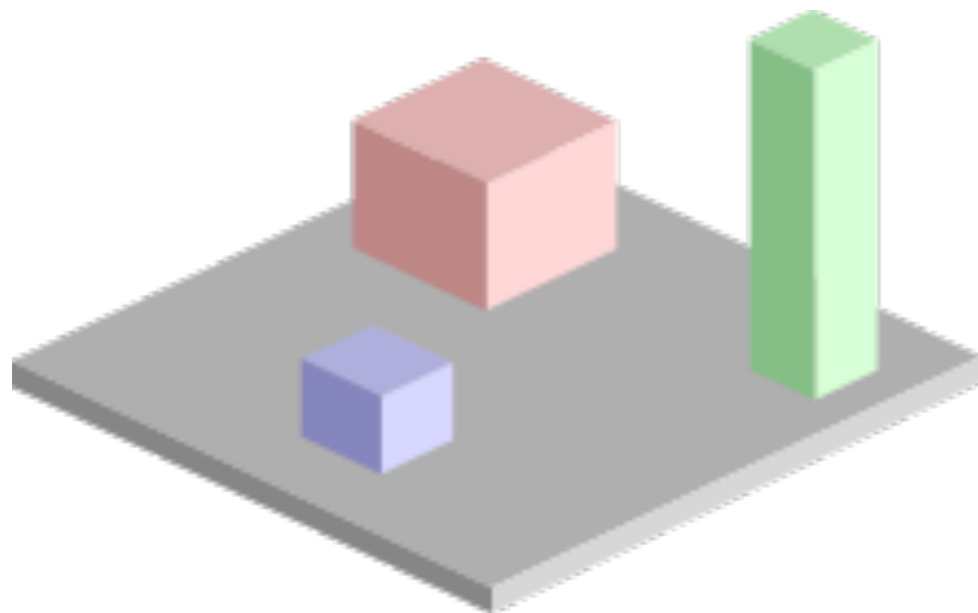
- $x, y, z$  of *base frame*
- pitch, roll, yaw, of *base frame*
- angle of first joint
- angle of second joint



A configuration is a *setting of values* to these 8 variables.  
Configuration space is the *space of all such settings*.

# Configuration Space

Obstacles are no-go regions of configuration space.

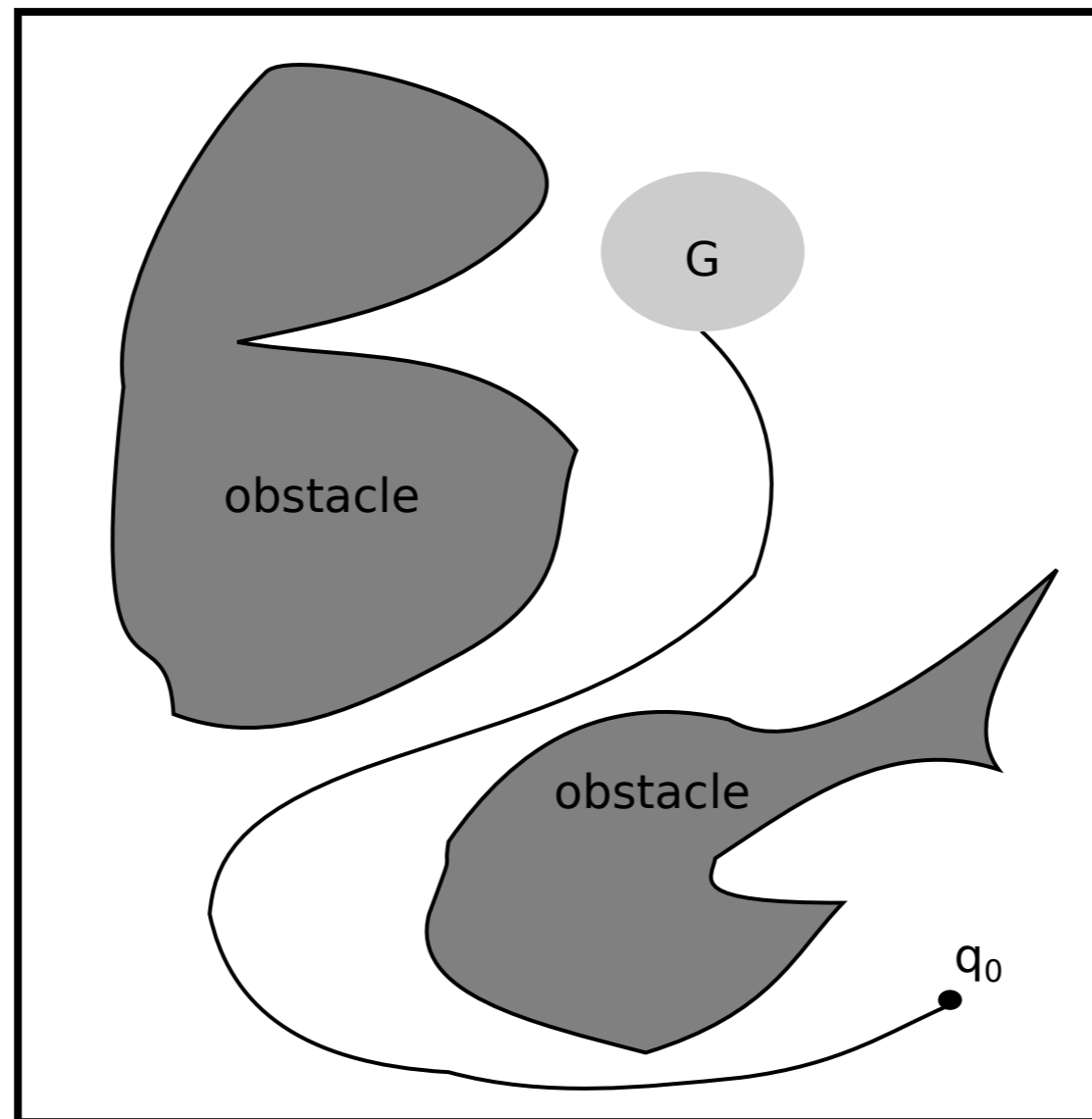


(images from Wikipedia)

# Planning

We wish to find a path through configuration space such that:

- Path feasible
- No collisions



a path in free space



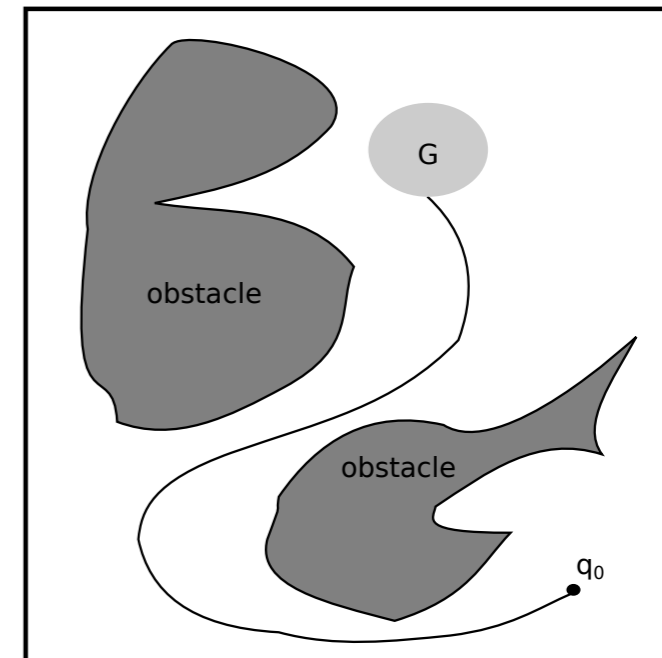
# Paths

Simple definition of a path:

- Sequence of points  $p = \{p_1, \dots, p_n\}$
- “Easy” to go between  $p_i$  and  $p_{i+1}$ .

**Solution** - path such that:

- $p_1 = \text{start}$
- $p_n$  inside goal
- No collision between any  $p_i$  and  $p_{i+1}$ .



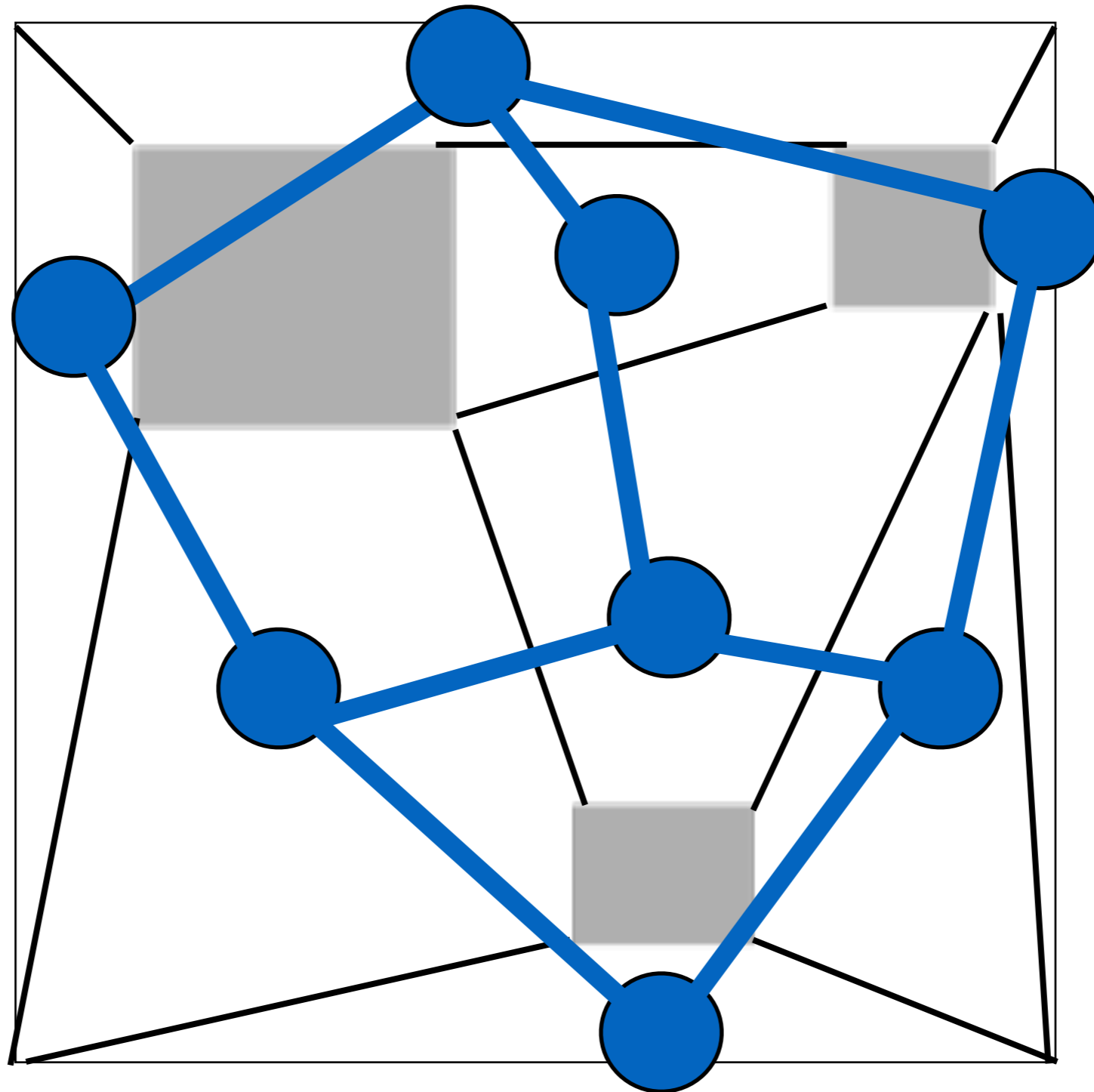
a path in free space

# Broad Approach: Visibility Graphs



1. Break *C-space* up into convex regions.
2. We know we can get from anywhere in a convex region to anywhere else with a straight line.
3. Build a graph: each node convex region, edge when they share a face.
4. Do search on the graph.

# Visibility Graphs



# Issues

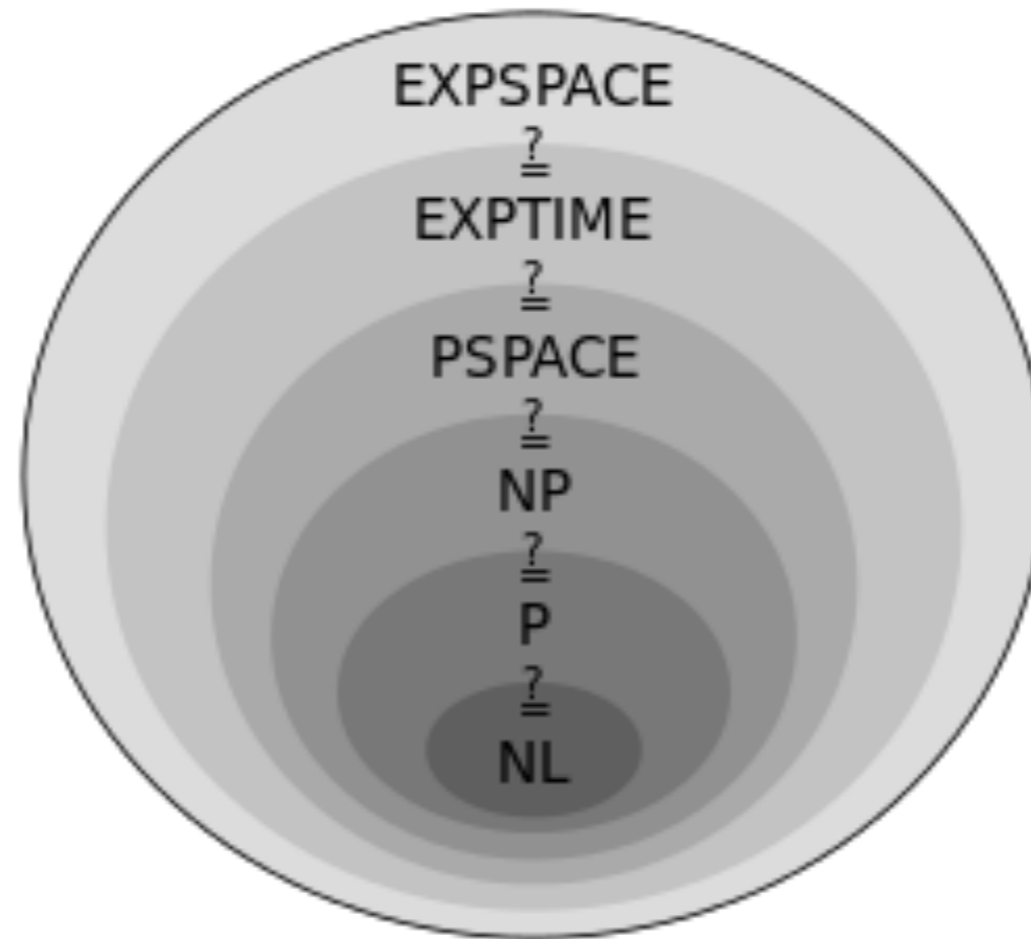
These are hard to use:

- Convex region numbers grow exponentially with dimension.
- Need analytical model of each obstacle *in C-space*.
- Need analytical model of C-space!

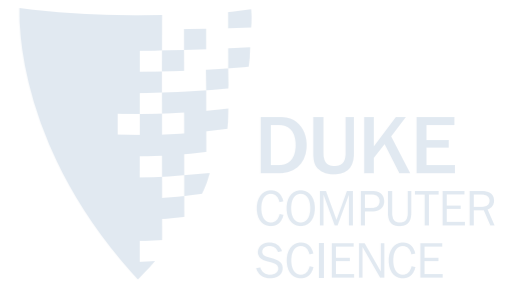
Consequently, these methods only used for very low- $d$  problems.

# Complexity

Issue: motion planning is P-SPACE complete (Reif, 1979).



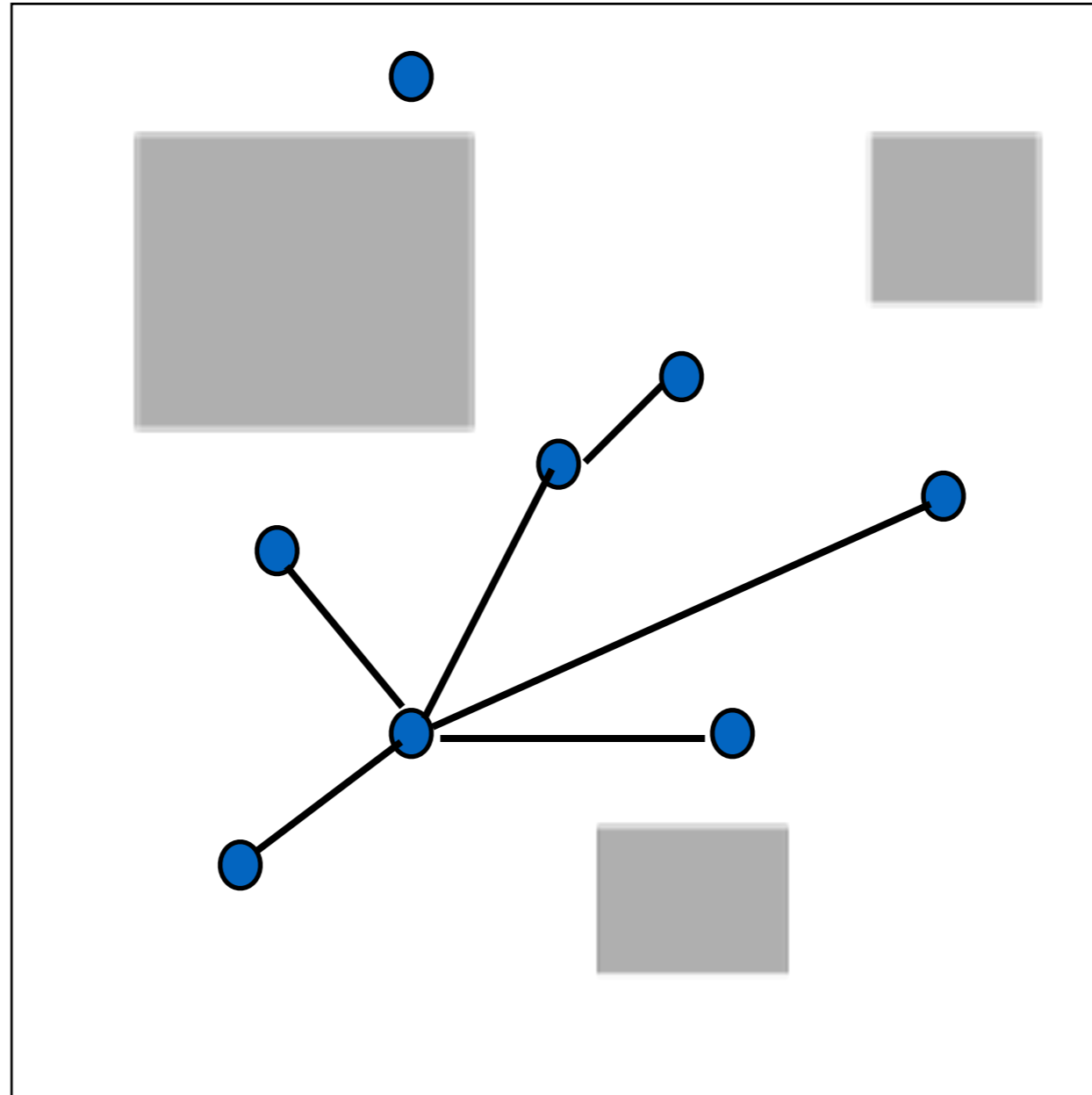
# Solution Family: RRTs



## Alternative solution:

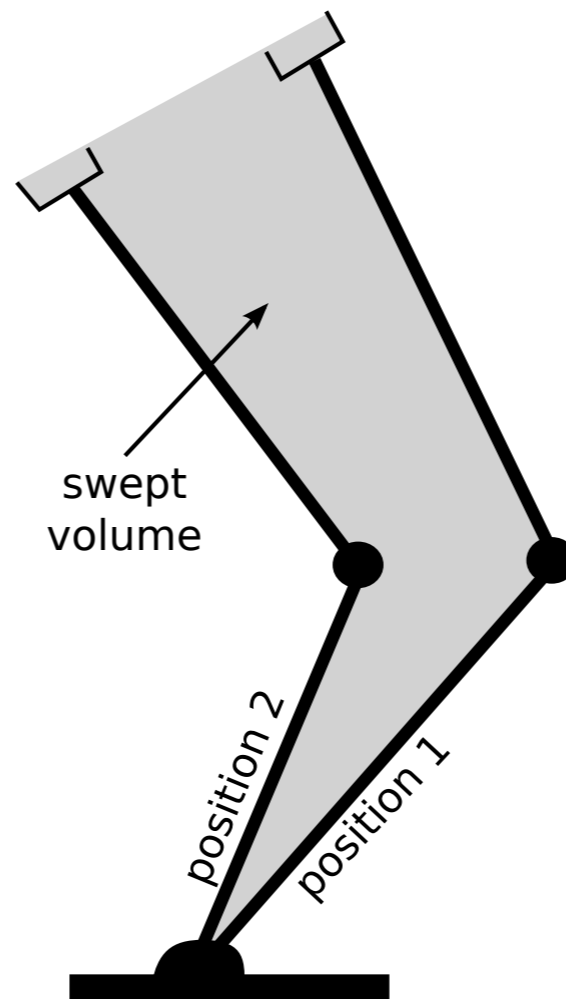
- Rely on randomized algorithms.
- Build *randomized trees* starting from the start state.
- High processing costs but probabilistic guarantees.

# RRTs



# RRTs

What does an edge between two nodes mean?



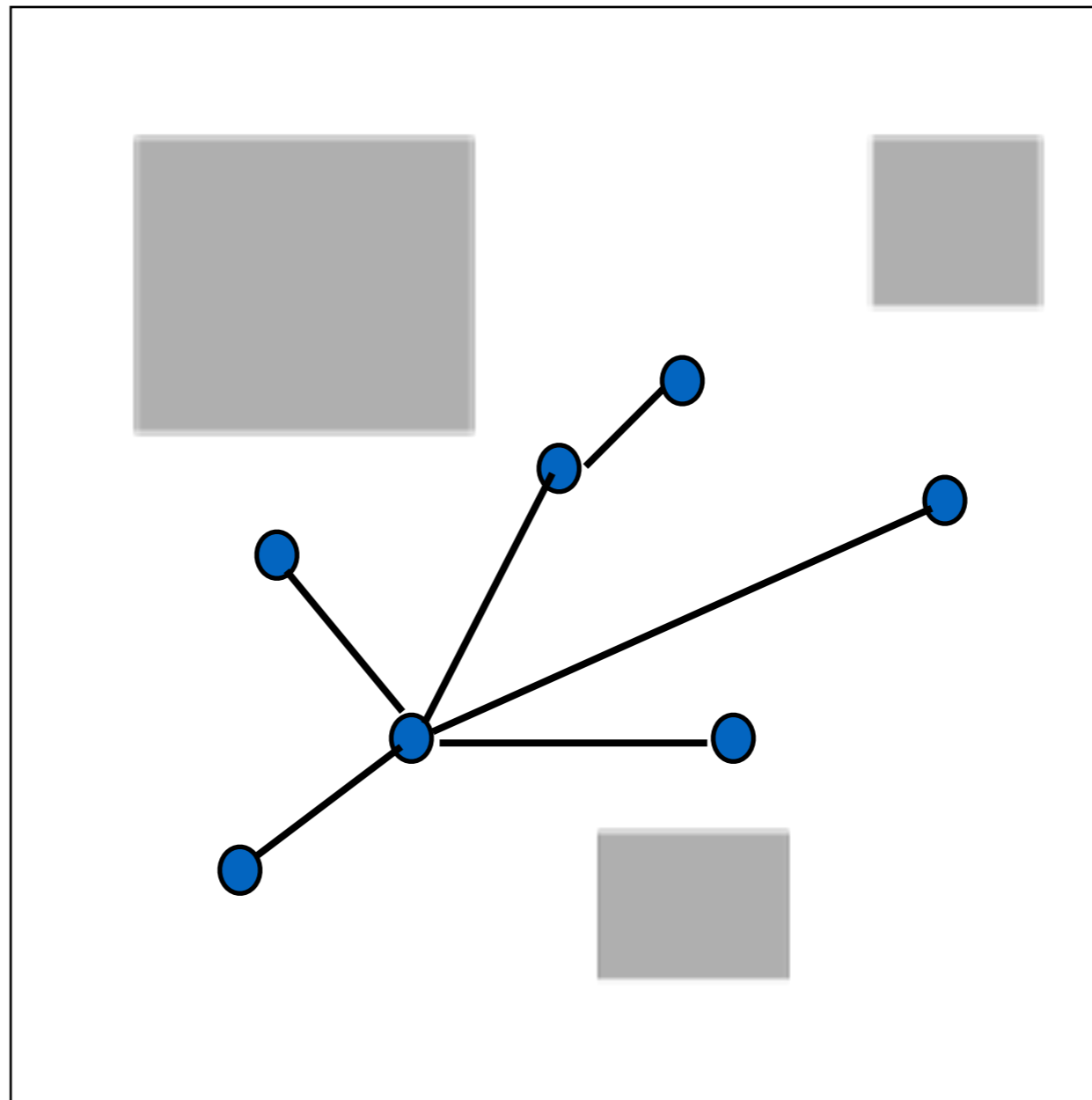
Must test: collision between *obstacle* and *swept volume*.  
*This can be done in 3-space.*



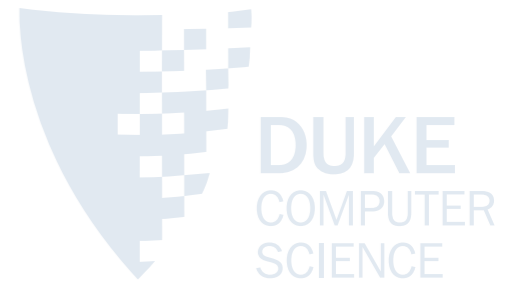
# RRT

Property: the tree *rapidly expands* to fill free space.

Why?



# Robot Motion Planning



**Absolutely critical for using robots in unstructured environments.**

**But:**

- **Fundamentally hard.**
- **Very well studied**
- **No real-time solutions.**

**(Watch this space.)**