

COMPSCI 223: Computational Microeconomics

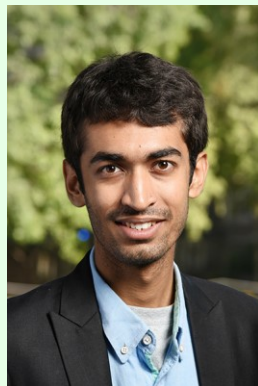
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<https://www2.cs.duke.edu/courses/spring18/compsci223/>

TAs: Harsh Parikh and Hanrui Zhang



CS-ECON@DUKE

Exploring the Intersection of Computer Science and Economics

[Home](#)[Schedule](#)[Past Talks](#)[People](#)[Mini-retreat](#)[Reading Group](#)

Who Are We?

We are a group of Duke University faculty, postdocs, and students interested in the intersection of computer science and economics (and the social sciences more broadly) and the impact of this interplay on decisions in information technology and digital business. This includes applying techniques from computer science and optimization to economics -- for example, using computation to design market clearing mechanisms and to implement efficient allocation and pricing in them -- as well as applying techniques from economics to computer science -- for example, designing incentives for users of networked computer systems and social networks.

Contacts

For organizational questions about the seminar series:

- [Yuan Deng](#)
- [Catherine Moon](#)

For other matters, contact the relevant faculty member(s):

- [Atila Abdulkadiroglu](#) (Econ)
- [Vincent Conitzer](#) (CS)



CS-Econ Talks

- [Upcoming Talks](#)
- [Past Talks](#)

Related Seminars

- [AI Group](#) (CS)
- [Algorithms Seminar](#) (CS)
- [Decision Sciences Seminar](#) (Fuqua)
- [Duke Robotics, Intelligence, and Vision \(DRIV\) Seminar](#) (CS)

► For Prospective Students

► Degree Programs

► M.A. Economics

► M.A. Analytical Political
Economy

M.S. Economics &
Computation

M.S. Quantitative Financial
Economics

► For Current Students

► EcoTeach: Student Services
Center

M.S. Economics & Computation

The joint field of economics and computer science has emerged from two converging intellectual needs: Computer science has become increasingly important for economists working with big data to address complex questions. Students interested in learning about computational mechanism design with applications to economics are ideal candidates for this program. Students whose interest is more generally focused on data analytics across a broad range of fields may also be interested in Duke's [Master of Quantitative Management](#) (MQM) program, offered at the Fuqua School of Business, and/or Duke's new [Master in Interdisciplinary Data Science](#) (MIDS) program, which is accepting its first class in Fall 2018.

The MSEC program combines the strengths of the Departments of Economics and [Computer Science](#) to educate students in these important computational skills linked to economics, and to prepare them for Ph.D. studies or careers in economics, finance, government, and business. Reflecting this strong interdisciplinary relationship, Duke University [ranks No. 5 for research in economics and computation](#), according to CSRankings.org.

This program is designed to meet the needs of students with varied levels of exposure to either field, but a strong quantitative background is recommended.

History



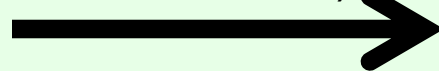
*John von
Neumann*

computer architecture
(von Neumann
architecture)



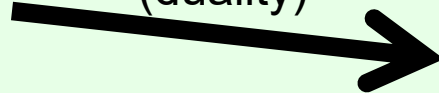
***Computer Science
& Engineering***

game theory
(minimax theorem)

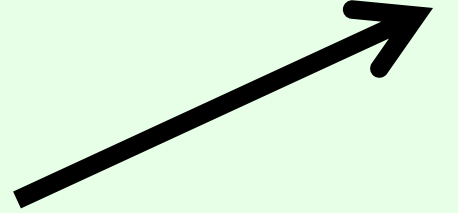
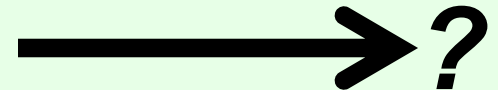
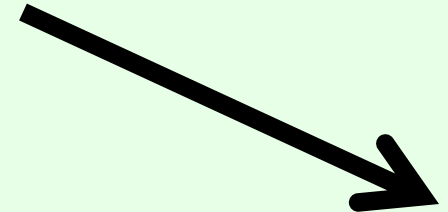


Economic Theory

linear programming
(duality)



***Mathematical
Optimization &
Operations
Research***

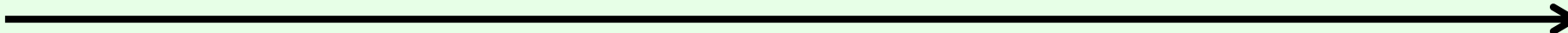


?

1900

1950

2000

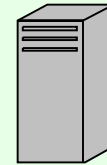


What is Economics?

- “the social science that studies the production, distribution, and consumption of goods and services.” [\[Wikipedia, Jan. 2018\]](#)
- Some key concepts:
 - Economic **agents** or **players** (individuals, households, firms, bots, ...)
 - Agents’ current **endowments** of goods, money, skills, ...
 - Possible **outcomes** ((re)allocations of resources, tasks, ...)
 - Agents’ **preferences** or **utility functions** over outcomes
 - Agents’ **beliefs** (over other agents’ utility functions, endowments, production possibilities, ...)
 - Agents’ possible **decisions/actions**
 - **Mechanism** that maps decisions/actions to outcomes

An economic picture

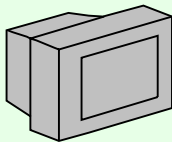
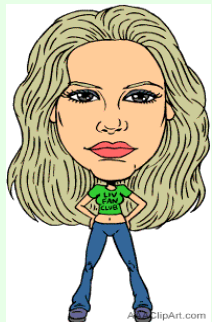
$$v(\text{server}) = 200$$



\$ 800

$$v(\text{monitor}) = 100$$

$$v(\text{laptop}) = 400$$



\$ 600

$$v(\text{laptop}) = 200$$

$$v(\text{server}, \text{monitor}) = 400$$



\$ 200



After trade (a more efficient outcome)

$$v(\text{server}) = 200$$



\$ 1100

... but how do we
get here?
Unstructured trade?
Auctions?
Exchanges?

$$v(\text{monitor}) = 100$$

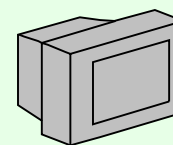
$$v(\text{laptop}) = 400$$



\$ 400

$$v(\text{laptop}) = 200$$

$$v(\text{server}, \text{monitor}) = 400$$



\$ 100



Some distinctions in economics

- **Descriptive** vs. **normative** economics
 - Descriptive:
 - seeks only to describe real-world economic phenomena
 - does not care if this is in any sense the “right” outcome
 - Normative:
 - studies how people “should” behave, what the “right” or “best” outcome is
- **Microeconomics** vs. **macroeconomics**
 - Microeconomics: analyzes decisions at the level of individual agents
 - deciding which goods to produce/consume, setting prices, ...
 - “bottom-up” approach
 - Macroeconomics: analyzes “the sum” of economic activity
 - interest rates, inflation, growth, unemployment, government spending, taxation, ...
 - “big picture”

What is Computer Science?

- “the study of automating algorithmic processes that scale. A computer scientist specializes in the theory of computation and the design of computational systems.” [Wikipedia, Jan. 2018]
- A **computational problem** is given by a function f mapping inputs to outputs
 - For integer x , let $f(x) = 0$ if x is prime, 1 otherwise
 - For initial allocation of resources + agent utilities x , let $f(x)$ be the (re)allocation that maximizes the sum of utilities
- An **algorithm** is a fully specified procedure for computing f
 - E.g., sieve of Eratosthenes
 - A **correct algorithm** always returns the **right** answer
 - An **efficient algorithm** returns the answer **fast**
- Computer science is also concerned with building **larger artifacts** out of these building blocks (e.g., personal computers, spreadsheets, the Internet, the Web, search engines, artificial intelligence, ...)

Resource allocation as a computational problem (*Part 1 of the course*)

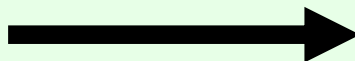
input

output

$$\begin{aligned} v(\text{server, monitor}) &= \$400 \\ v(\text{laptop}) &= \$600 \end{aligned}$$



$$\begin{aligned} &\text{server, monitor} \\ &\$ 800 \end{aligned}$$



$$\begin{aligned} &\text{laptop} \\ &\$ 750 \end{aligned}$$

$$\begin{aligned} v(\text{server, monitor}) &= \$500 \\ v(\text{laptop}) &= \$400 \end{aligned}$$



$$\begin{aligned} &\text{laptop} \\ &\$ 400 \end{aligned}$$



$$\begin{aligned} &\text{server, monitor} \\ &\$ 450 \end{aligned}$$

Here, gains from trade (\$300)
are divided evenly
(not essential)

Economic mechanisms

“true” input

agents’ bids

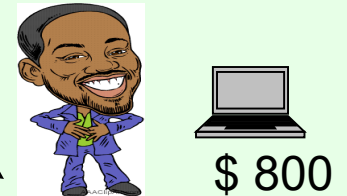
result

$$v(\text{server, monitor}) = \$400$$
$$v(\text{laptop}) = \$600$$

agent 1’s
bidding
algorithm

$$v(\text{server, monitor}) = \$500$$
$$v(\text{laptop}) = \$501$$

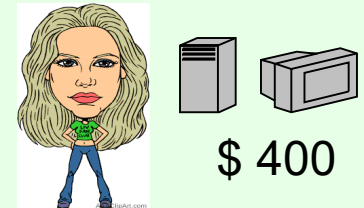
exchange
mechanism
(algorithm)



$$v(\text{server, monitor}) = \$500$$
$$v(\text{laptop}) = \$400$$

agent 2’s
bidding
algorithm

$$v(\text{server, monitor}) = \$451$$
$$v(\text{laptop}) = \$450$$



*Exchange mechanism designer
does not have direct access to
agents’ private information*

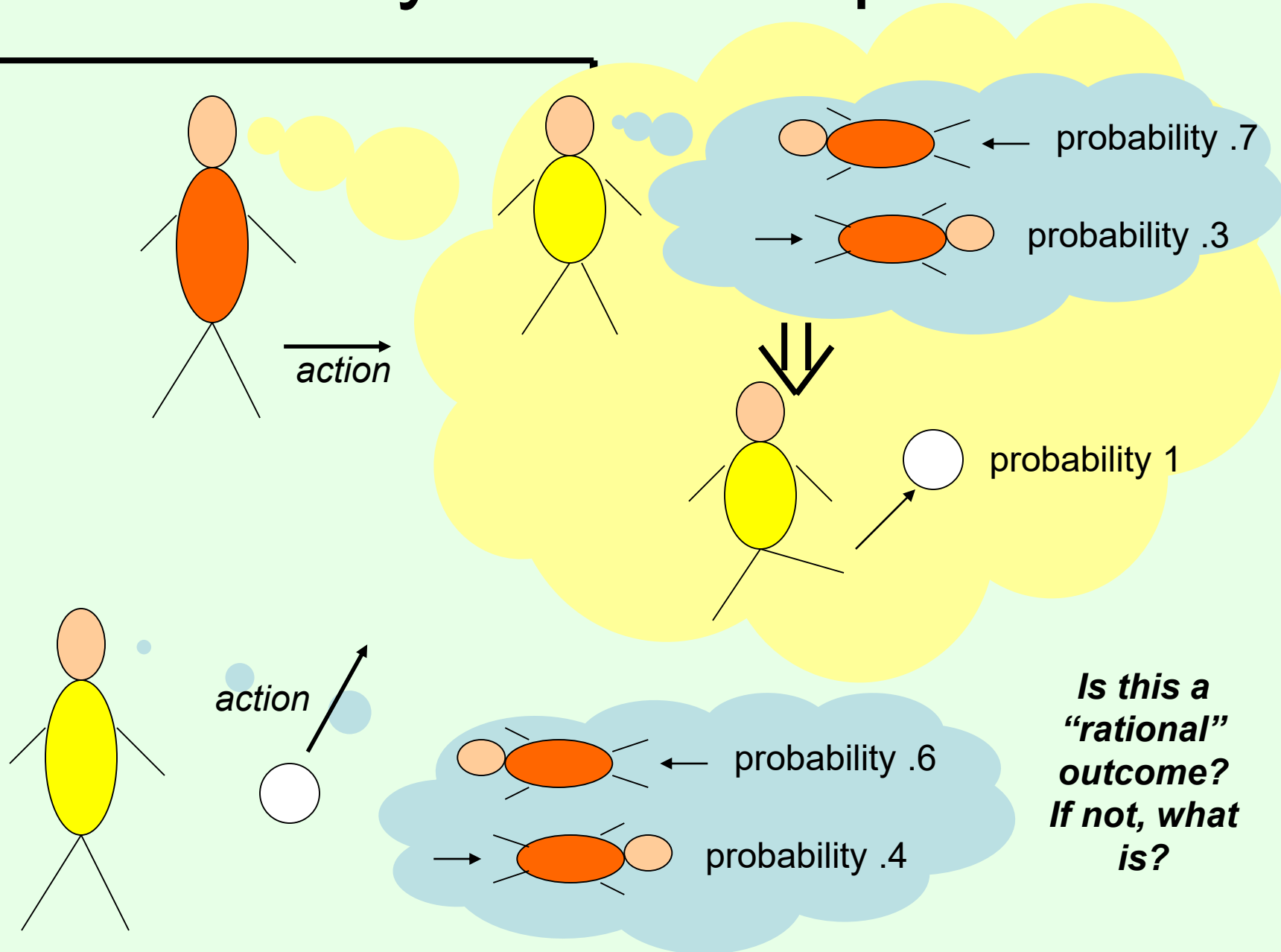
*Agents will selfishly respond to
incentives*

Game theory

(Part 2 of the course)

- Game theory studies settings where agents each have
 - different preferences (utility functions),
 - different actions that they can take
- Each agent's utility (potentially) depends on all agents' actions
 - What is optimal for one agent depends on what other agents do
 - Very circular!
- Game theory studies how agents can rationally form beliefs over what other agents will do, and (hence) how agents should act
 - Useful for acting as well as predicting behavior of others

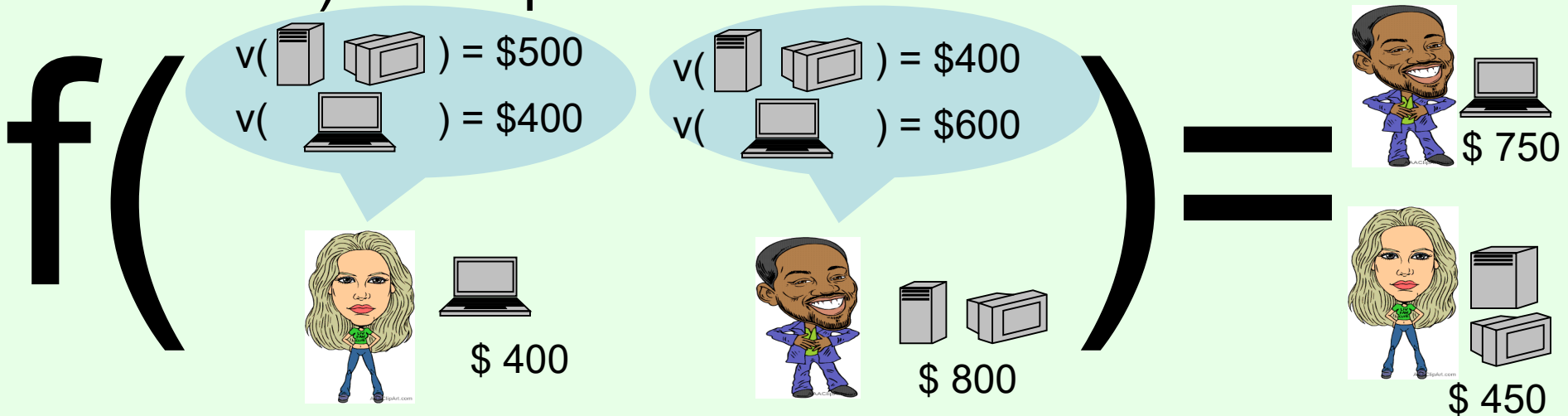
Penalty kick example



Mechanism design

(Part 3 of the course)

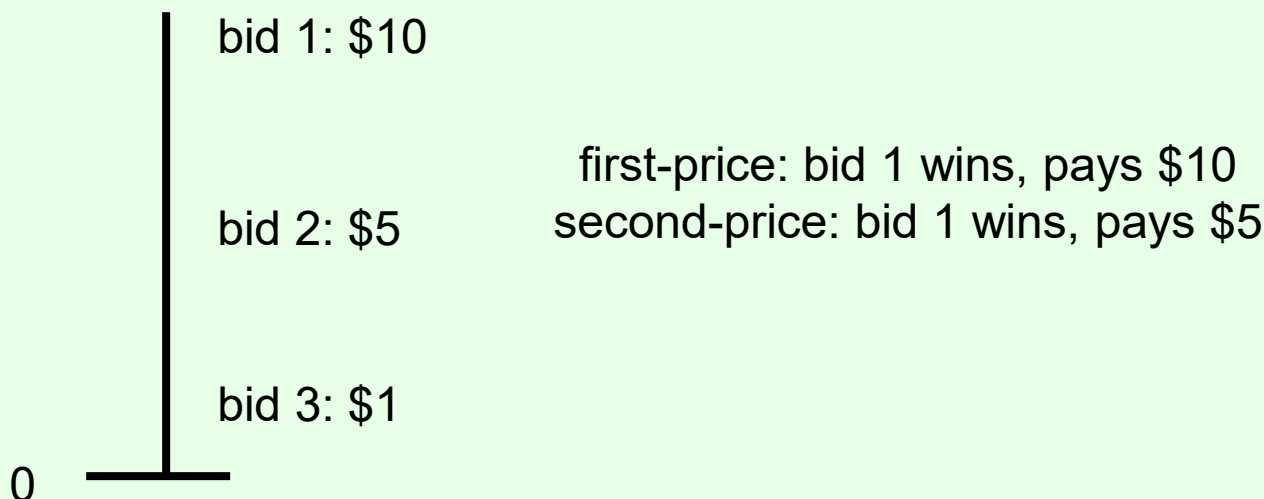
- **Mechanism** = rules of auction, exchange, ...
- A **function** that takes **reported preferences** (bids) as input, and produces **outcome** (allocation, payments to be made) as output



- The **entire function** f is **one** mechanism
- E.g., the mechanism from part 1: find allocation that maximizes (reported) utilities, distribute (reported) gains evenly
- Other mechanisms choose different allocations, payments

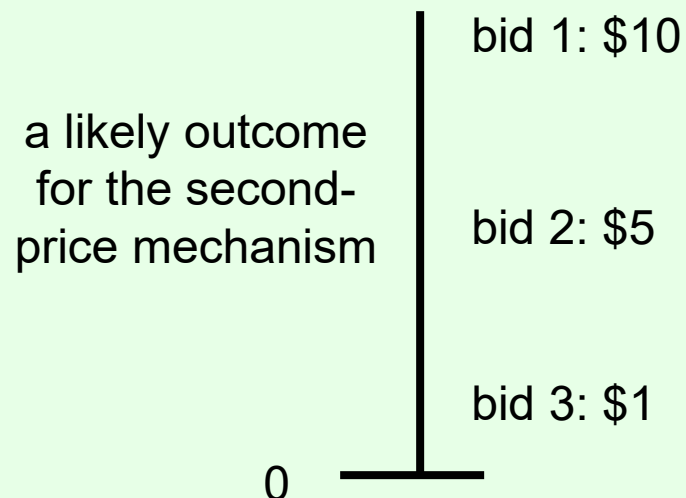
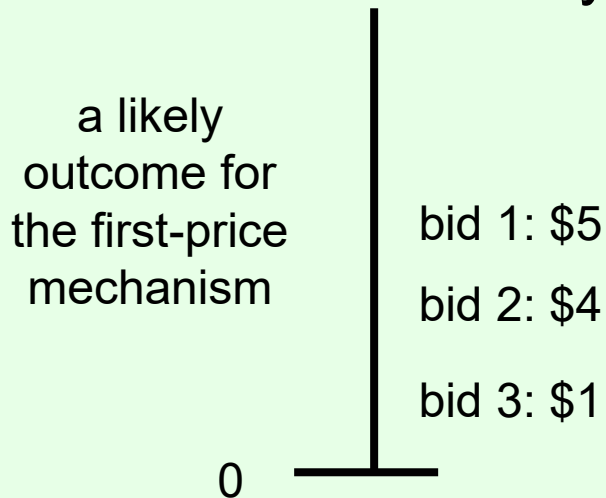
Example: (single-item) auctions

- **Sealed-bid** auction: every bidder submits bid in a sealed envelope
- **First-price** sealed-bid auction: highest bid wins, pays amount of own bid
- **Second-price** sealed-bid auction: highest bid wins, pays amount of second-highest bid



Which auction generates more revenue?

- Each bid depends on
 - bidder's **true valuation** for the item (utility = valuation - payment),
 - bidder's **beliefs** over what others will bid (\rightarrow game theory),
 - and... the **auction mechanism** used
- In a first-price auction, it does not make sense to bid your true valuation
 - Even if you win, your utility will be 0...
- In a second-price auction, (we will see later that) it always makes sense to bid your true valuation



Are there other auctions that perform better? How do we know when we have found the best one?

Mechanism design...

- Mechanism = game
- → we can use game theory to predict what will happen under a mechanism
 - if agents act strategically
- When is a mechanism “good”?
 - Should it result in outcomes that are good for the **reported** preferences, or for the **true** preferences?
 - Should agents ever end up **lying** about their preferences (in the game-theoretic solution)?
 - Should it always **generate the best allocation**?
 - Should agents ever **burn money**?(!?)
- Can we solve for the optimal mechanism?

How are we going to solve these problems? (*Part 0*)


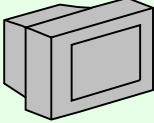
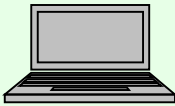
- This is **not** a programming course
- Will use optimization software
 - GNU Linear Programming Kit (GLPK)
 - Linear programming, mixed integer linear programming

Uses of LP, MIP in this course

	Linear programming	Mixed integer linear programming
Part 1 (expressive marketplaces)	Winner determination in auctions, exchanges, ... with partially acceptable bids	Winner determination in auctions, exchanges, ... without partially acceptable bids
Part 2 (game theory)	Dominated strategies Minimax strategies Correlated equilibrium Optimal mixed strategies to commit to	Nash equilibrium
Part 3 (mechanism design)	Automatically designing optimal mechanisms that use randomization	Automatically designing optimal mechanisms that do not use randomization

Other settings/applications

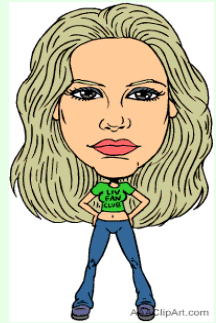
Combinatorial auctions (in Part 1)

Simultaneously for sale:  ,  , 



bid 1

$$v(\text{server icon} \text{ cabinet icon}) = \$500$$



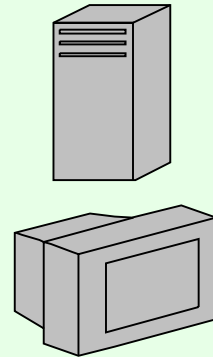
bid 2

$$v(\text{laptop icon} \text{ cabinet icon}) = \$700$$



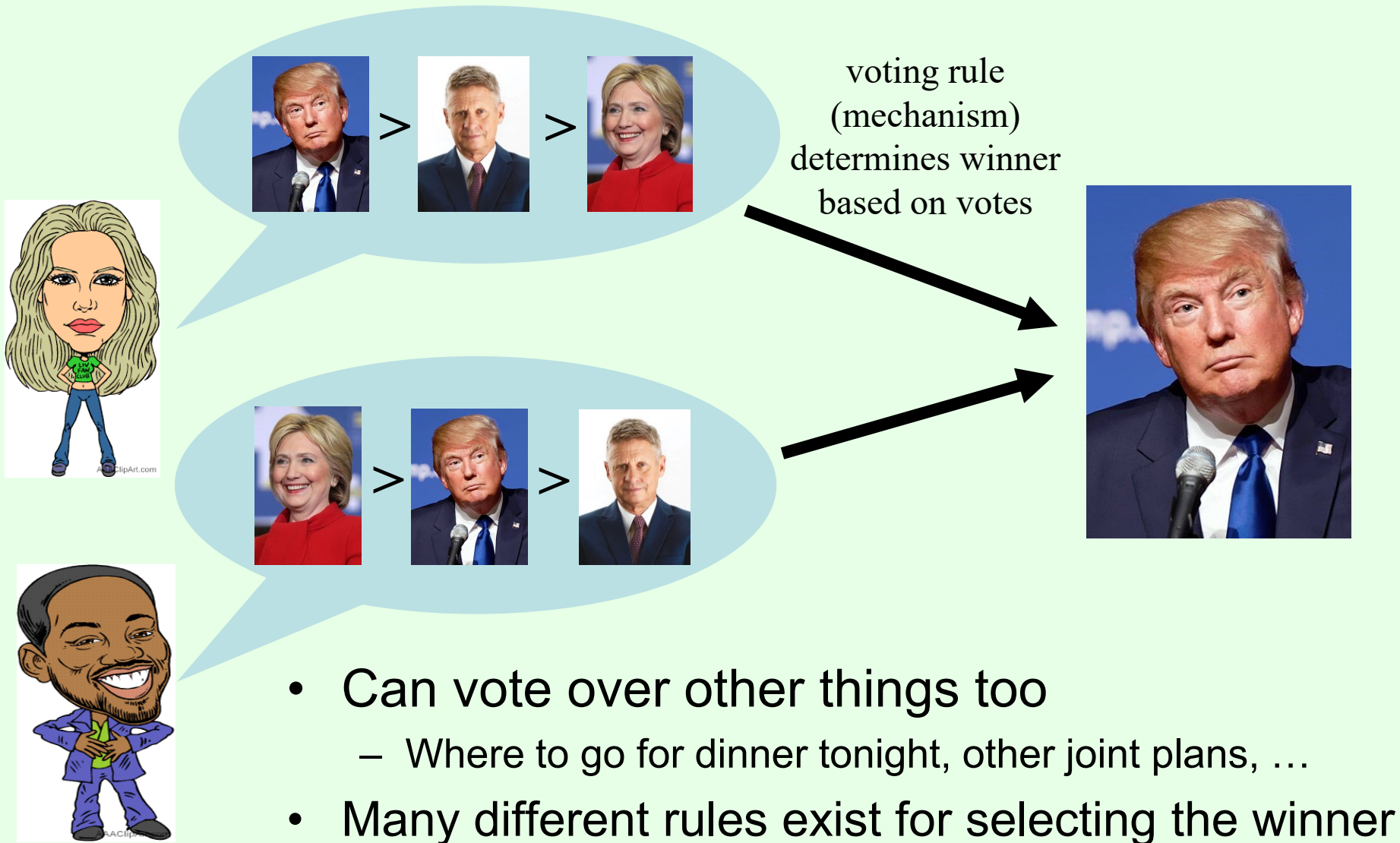
bid 3

$$v(\text{laptop icon}) = \$300$$

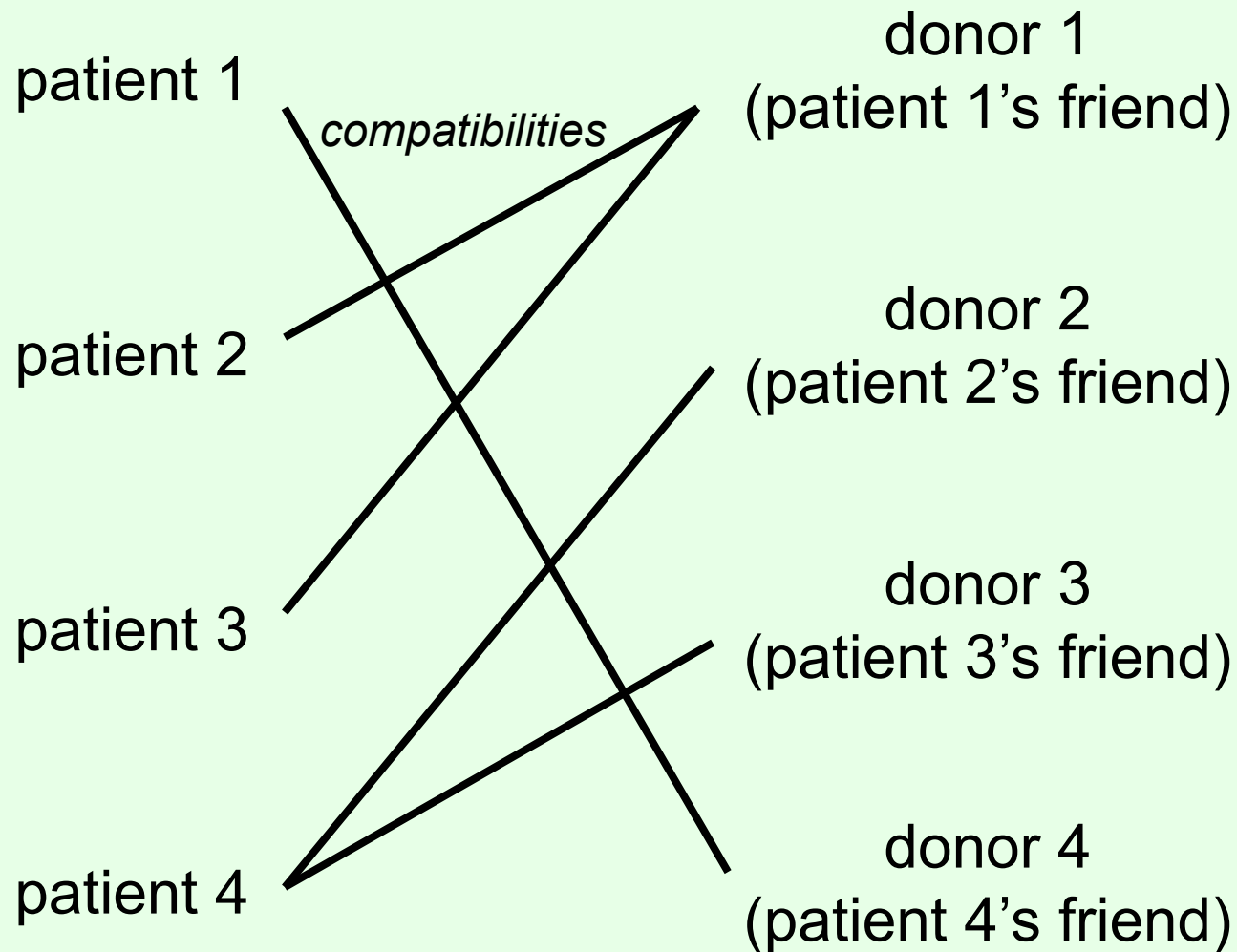


used in truckload transportation, industrial procurement, radio spectrum allocation, ...

Voting (in Part 1)



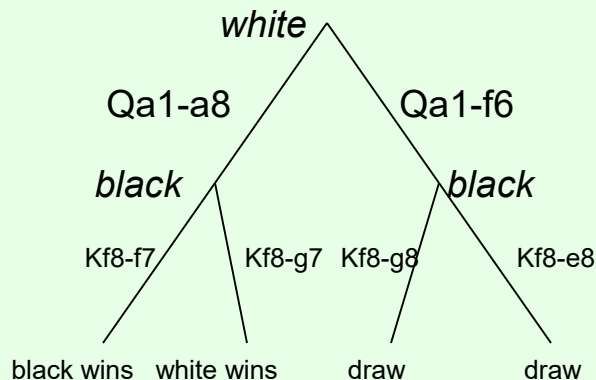
Kidney exchange (in Part 1)



Game playing & AI (in Part 2)

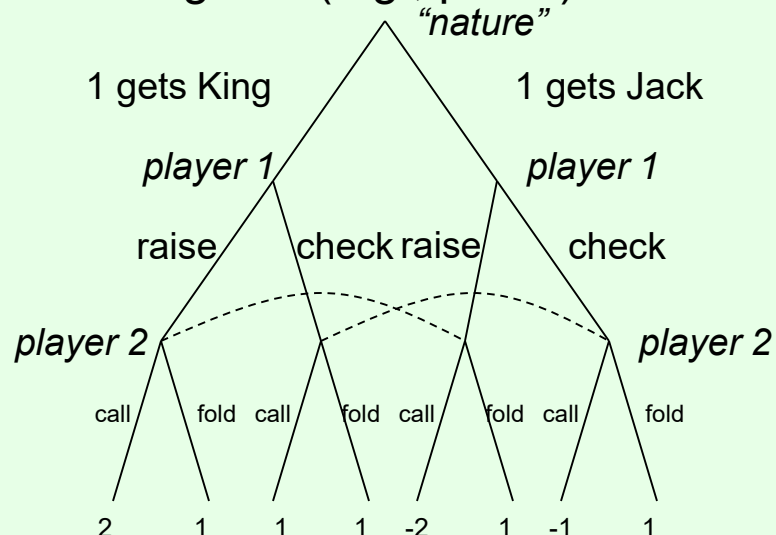
perfect information games:

no uncertainty about the state of the game (e.g. tic-tac-toe, chess, Go)



imperfect information games:

uncertainty about the state of the game (e.g., poker)



- Optimal play: value of each node = value of optimal child for current player (**backward induction**, minimax)
- For chess and Go, tree is too large
 - Use other techniques (heuristics, limited-depth search, alpha-beta, deep learning, ...)
- Top computer programs better than humans in chess, ~~not yet in Go~~

- Player 2 **cannot distinguish** nodes connected by dotted lines
 - Backward induction fails; need more sophisticated game-theoretic techniques for optimal play
- Small poker variants can be solved optimally
- Humans still better than top computer programs at full-scale poker (at least most versions?)
- Top computer (heads-up) poker players are based on techniques for game theory

Real-world security applications (in Part 2)



Milind Tambe's TEAMCORE group (USC)



Airport security

Where should checkpoints, canine units, etc. be deployed?

Federal Air Marshals

Which flights get a FAM?



US Coast Guard


Which patrol routes should be followed?

Wildlife Protection

Where to patrol to catch poachers or find their snares?



Prediction markets

 Closing Soon

U.S. Elections

U.S. Politics

World



Who will win the 2020 U.S. presidential election?

Market Type: **Linked**

End Date: **N/A**














Status: **Open**

Contracts









Rules

Chart

Trade shares from this page by clicking any price in bold. For more information on an individual prediction, click on the name or image.

PREZ.2020	Latest	Buy Yes	Sell Yes	Buy No	Sell No
 Donald Trump TRUM.PREZ.2020	31¢ + 1¢	33¢	31¢	69¢	67¢
 Bernie Sanders SAND.PREZ.2020	13¢ NC	13¢	12¢	88¢	87¢
 Joe Biden BIDE.PREZ.2020	10¢ NC	11¢	10¢	90¢	89¢
 Kamala Harris HARR.PREZ.2020	9¢ NC	10¢	8¢	92¢	90¢
 Kirsten Gillibrand GILL.PREZ.2020	9¢ + 1¢	9¢	8¢	92¢	91¢
 Mike Pence PENC.PREZ.2020	8¢ NC	8¢	7¢	93¢	92¢
 Elizabeth Warren WARR.PREZ.2020	7¢ + 1¢	7¢	6¢	94¢	93¢
 Cory Booker BOOK.PREZ.2020	7¢ NC	8¢	7¢	93¢	92¢
 John Kasich KASI.PREZ.2020	4¢ + 1¢	4¢	3¢	97¢	96¢
 Amy Klobuchar KLOB.PREZ.2020	4¢ NC	5¢	4¢	96¢	95¢
 Andrew Cuomo CUOM.PREZ.2020	3¢ NC	4¢	3¢	97¢	96¢
 Nikki Haley HALE.PREZ.2020	2¢ NC	3¢	2¢	98¢	97¢
 Paul Ryan RYAN.PREZ.2020	2¢ NC	3¢	2¢	98¢	97¢
 Mark Cuban CUBA.PREZ.2020	1¢ NC	2¢	1¢	99¢	98¢
Mark Zuckerberg ZUCK.PREZ.2020	1¢ NC	2¢	1¢	99¢	98¢

Financial securities (in Part 1)

- Tomorrow there must be one of   
- Agent 1 offers \$5 for a security that pays off \$10 if  or 
- Agent 2 offers \$8 for a security that pays off \$10 if  or 
- Agent 3 offers \$6 for a security that pays off \$10 if 
- Can we accept some of these at offers **at no risk?**

How to incentivize a weather forecaster (in Part 3)

$$\begin{aligned} P(\text{☀}) &= .5 \\ P(\text{☁☔}) &= .3 \\ P(\text{☁⚡}) &= .2 \end{aligned}$$

$$\begin{aligned} P(\text{☀}) &= .8 \\ P(\text{☁☔}) &= .1 \\ P(\text{☁⚡}) &= .1 \end{aligned}$$



- Forecaster's bonus can depend on
 - Prediction
 - Actual weather on predicted day
- Reporting true beliefs should maximize expected bonus

Sponsored search / ad auctions (in Part 3)

The screenshot shows a Google search interface with the query 'prediction markets proper scoring'. The search results include an advertisement for PredictIt, followed by several scholarly articles. The advertisement is highlighted with a black box. The scholarly articles are marked with green checkmarks.

Google

prediction markets proper scoring

All News Images Videos Shopping More Settings Tools

About 714,000 results (0.43 seconds)

A Political Prediction Market - Join PredictIt Today - predictit.org

Ad www.predictit.org/ ▼

Buy and sell shares on political outcomes with PredictIt. Let's Play Politics!
Predict & Trade · Safe and Secure · Unique Platform · Easy to Use
[About](#) · [Markets](#) · [Markets Analysis](#) · [Blog](#)

Scholarly articles for prediction markets proper scoring ✓

Prediction markets: Does money matter? - [Servan-Schreiber](#) - Cited by 337
Logarithmic **markets** coring rules for modular ... - [Hanson](#) - Cited by 275
... new understanding of **prediction markets** via no-regret ... - [Chen](#) - Cited by 81

[PDF] Geometric Charaterization of Proper Scoring Rules and Hanson ... - ... ✓

www.mit.edu/~pengshi/papers/2009-05-csurf-geometry.pdf ▼

One problem in implementing a **prediction market** is provid- ing liquidity, and ... a **proper scoring** rule can be a tedious process, and the re- lationship between ...

[PDF] Proper Scoring Rules with Additional Properties - MIT ✓

www.mit.edu/~pengshi/papers/2009-04-psr-characterization.pdf ▼

of market-scoring rules and **prediction markets**. In this pa- per, we present a geometric interpretation to a previously known characterization of **proper scoring** ...

[PDF] Logarithmic Market Scoring Rules for Modular ... - Robin Hanson ✓

hanson.gmu.edu/mktscore.pdf ▼

by R Hanson - 2002 - [Cited by 275](#) - [Related articles](#)
cannot even **predict** the direction in which others will disagree with them (Hanson, For a non-**proper**

- Choice of ads (if any) to show determined by:
 - Advertiser bid
 - Predicted likelihood of click