Real Cameras and their Calibration

COMPSCI 527 — Computer Vision

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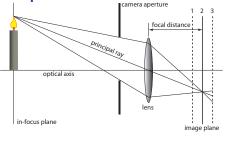
Outline

Real Cameras Depth of Field Distortion

2 Camera Calibration A Camera Model Parameter Optimization Lab Setup and Imaging

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Depth of Field

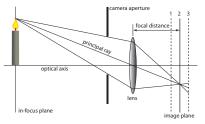




- Focal *length*: focal *distance* when an object at ∞ is in focus
- Focal length is a lens property
- Focal distance can be changed by rotating the focusing ring
- Nothing to do with zoom, which changes focal length
- Alas, f is often used for either focal distance or focal length

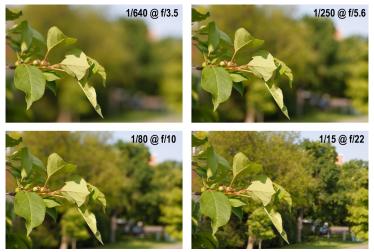
Changing Depth of Field

- Aperture: diameter of the hole in front of the lens
- Measured in *stops*, or *f*-numbers $n = \frac{f}{a}$ (*a* is aperture diameter, *f* is focal length)
- Area (light flux) is proportional to square of diameter
- Small aperture (big *f*-number) ⇒ great depth of field
- A shallow depth of field is sometimes desirable





Depth of Field and Exposure



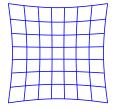
http://www.boostyourphotography.com/2014/10/depth-of-field.html

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Lens Distortion









barrel







\leftarrow distortion

not distortion:



85mm @ 200cm

35mm @ 85cm

16mm @ 40cm

12mm @ 30cm

8mm @ 20cm

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Real Cameras and their Calibration

Camera Calibration

- Cameras have *intrinsic parameters*: focal distance, pixel size, principal point, lens distortion parameters
- ... and *extrinsic parameters*: Rotation, translation relative to some world reference system
- Camera calibration is a combination of lab measurements and algorithms aimed at determining both types of parameters
- We do not calibrate for finite depth of field (stop down the aperture, flood the scene with light)

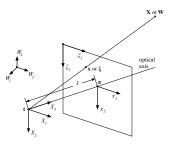
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Calibration as Learning

- Many variants, the general idea is the same
- Looks very much like machine learning:
 - Make a parametric model of what a camera does: Inputs are world points W in world coordinates, outputs are image points ξ in image pixel coordinates ("predictor architecture")
 - Collect a sufficiently large set *T* of input-output pairs (W_n, ξ_n) ("training set")
 - **3** "Loss function" measures discrepancy between $\hat{\xi}_n$ predicted by model and ξ_n measured in image
 - 4 Fit the parameters to T by numerical optimization ("training")
- We even have generalization requirements: The parameters should be correct for pairs (W, ξ) not in T
- We already know how to do 3, 4. Need to figure out 1, 2.

Camera Model

$$\begin{split} \mathbf{X} &= R \left(\mathbf{W} - \mathbf{t} \right) \\ \mathbf{x} &= p(\mathbf{X}) = \frac{1}{X_3} \begin{bmatrix} X_1 \\ X_2 \end{bmatrix} \\ \mathbf{y} &= d(\mathbf{x}) \quad \text{(lens distortion)} \\ \boldsymbol{\xi} &= S\mathbf{y} + \pi \\ S &= f \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix} \\ \text{Can only determine} \\ products f s_x \text{ and } f s_y, \\ \text{not } f, s_x, s_y \text{ individually} \end{split}$$





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Lens Distortion Model

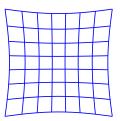
• Distortion is radial around the principal point:

 $\mathbf{y} = d(\mathbf{x}) = \delta(r) \mathbf{x}$ where $r = \|\mathbf{x}\|$

- Radial distortion function $\delta(\cdot)$ is nonlinear
- Must be analytical everywhere (Maxwell). Implication:
 - Restrict to x axis: $\delta(r(\mathbf{x})) = \delta(|x|)$
 - Odd powers of |x| have a cusp at the origin
 - Therefore, $\delta(r) = 1 + k_1 r^2 + k_2 r^4 + \dots (k_0 \neq 1 \text{ can be folded into } f)$
- Large powers of *r* only affect peripheral areas and cannot be determined well
- Typically, $\delta(r) = 1 + k_1 r^2 + k_2 r^4$







Camera Parameters

$$\mathbf{X} = R(\mathbf{W} - \mathbf{t})$$

$$\mathbf{x} = \rho(\mathbf{X}) = \frac{1}{X_3} \begin{bmatrix} X_1 \\ X_2 \end{bmatrix}$$

$$\mathbf{y} = \mathbf{x} (1 + k_1 \|\mathbf{x}\|^2 + k_2 \|\mathbf{x}\|^4)$$

$$\boldsymbol{\xi} = S\mathbf{y} + \pi$$

- Extrinsic parameters: *R*, t (6 degrees of freedom)
- Intrinsic parameters: π , $f s_x$, $f s_y$, k_1 , k_2 (6 numbers)

$$oldsymbol{\xi} = oldsymbol{c}(oldsymbol{W};oldsymbol{p})$$
 where $oldsymbol{p} \in \mathbb{R}^{12}$

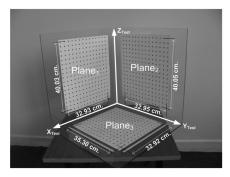
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Data Fitting

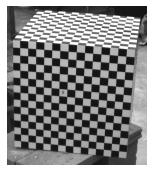
- Collect input-output pairs $(\mathbf{W}_n, \boldsymbol{\xi}_n)$ for n = 1, ..., N $\hat{\boldsymbol{\xi}} = \mathbf{c}(\mathbf{W}; \mathbf{p})$ where $\mathbf{p} \in \mathbb{R}^{12}$ $\mathbf{p}^* = \arg\min_{\mathbf{p}} \boldsymbol{e}(\mathbf{p})$ where $\boldsymbol{e}(\mathbf{p}) = \frac{1}{N} \sum_{n=1}^{N} \|\boldsymbol{\xi}_n - \mathbf{c}(\mathbf{W}_n; \mathbf{p})\|^2$ • c is poplinger
- *e* is nonlinear
- To initialize: clamp $k_1 = k_2 = 0$, solve a linear system
- Approximate because of clamping and because the residual is different from e(p)
- Use any optimization algorithm to refine

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Calibration Target



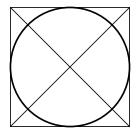
http://www.mdpi.com/1424-8220/9/6/4572/htm

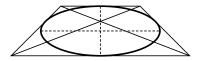


Duke Computer Vision Lab

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Circles are Problematic





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Calibration Protocol Summary

- Place calibration target in front of camera (fill the image)
- Measure image coordinates (with software help?)
- Make a file with $(\mathbf{W}_n, \boldsymbol{\xi}_n)$ pairs
- Fit parameters by numerical optimization
- Redo if you touch the lens or the camera!



versela for Distortion Only

